

## 6.863J Natural Language Processing Lecture 20: the meaning of it all, #6

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### The Menu Bar

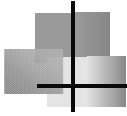
- Administrivia:

- Lab 4(a&b) out today – last lab before final project – due April 28

Agenda:

How to use language: discourse structure & anaphora

discourse representation structure,  
presuppositions, and language etiquette



ABSTRACT – CONCRETE

NONLIVING – LIVING

EDIBLE – INEDIBLE

IMMOBILE – MOBILE

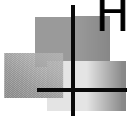
ANIMATE – INANIMATE

NONHUMAN – HUMAN

MALE – FEMALE

Hypernym: All X, car x implies vehicle x  
All x, concrete x implies not abstract x

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## Hypernyms and Wordnet

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## Discourse

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- Mia is a woman. She loves Vincent
- A man snorts. He collapses.
- Problems: complex post-processing & counter-intuitive readings
- Biggest problem: discourse is not just set of FOL sentences, glued together...

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## What is the glue?

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- Discourse anaphora
- John bought a book. It is a best-seller
- John bought a Porsche or a Prius. It is a best-seller
- John did not buy a Porsche. It is a best-seller
- John did not buy a five dollar shake. Vincent tasted it

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## More examples

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- Butch threw a vase at the wall
- It broke
- Butch walks into his modest kitchen. He opens the refrigerator. He takes out a milk and drinks it.
- Butch walks into his modest kitchen. He opens the refrigerator. He takes out a glass of iced tree and drinks it.

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## Discourse representation theory (DRT)

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- Semantic framework w/ a language to describe discourse
- Translate discourse to FO logic
- Compatible with lambda calculus approach

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## DRT overview

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- Uses language based on box-like structures called DRSs (discourse representation structures)
- Intuition: DRSs are pictures
- Another (nonrepresentational) view: DRSs are programs

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## And with this...

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- We can do most 'common' anaphora...
  
- But wait, there's more...

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## Why doesn't FOL logic work for discourse?

- Discourse is not simply the conjunction of first-order representations of individual sentences
- Why?
- Try this discourse: Mia is a cat. She loves Vincent.
- First sentence:  $\text{cat}(\text{mia})$
- Suppose free variable like pronoun, eg,  $\text{love}(x, \text{vincent})$
- Conjunction is:  $\text{cat}(\text{mia}) \wedge \text{love}(x, \text{vincent})$
- "she" is an anaphoric pronouns – refers back to mia

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## What to do?

- Answer 1: replace  $x$  with 'mia' – a post-processing step
- But this won't work – breaks down for:  
A cat sneezes. She collapses.
- First-order approach:  $\exists z(\text{cat}(z) \wedge \text{sneeze}(z) \wedge \text{collapse}(x))$
- Replace free variable  $x$  with  $z$
- This is truth-conditionally correct, but...
- Doesn't tell us the context in which subsequent utterances will be interpreted
- Instead of post-processing context conditions back in, make representation contain them at the start

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## DRT

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- Represent context
- Allow access to truth-conditional aspects

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## Context change potential

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- When we utter 'a man snorts' we don't simply make a claim about the world, we change the context in which subsequent utterances will be interpreted (hmm, like a frame....)
- Start a new discourse with the empty box



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## What's different about this?

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- Inter-sentential perspective from the start
- Top compartment holds discourse referents (note: these are not quite like variables...!)
- Bottom compartment holds conditions
- Top is like domain of a little model – the discourse model

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## Anaphoric pronoun

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- Introduces new discourse referent (eg, "y")
- Must be identified with a (previous) accessible discourse referent
- In the simple case,  $x=y$

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## Defining discourse representation languages (DRS)

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1. If  $x_1, \dots, x_n$  are discourse referents ( $n \geq 0$ ) and  $\gamma_1, \dots, \gamma_m$  ( $m \geq 0$ ) are conditions then

$x_1 \dots x_n$
$\gamma_1 \dots \gamma_m$

is a DRS

This defines the "box" – in simplest case, the empty universe with no conditions

A term is either a constant or a discourse referent

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## Defining discourse representation languages (DRS)

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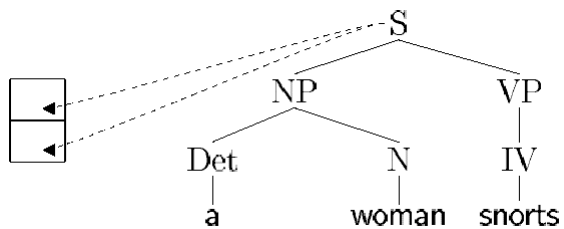
2. If  $R$  is a relation symbol of arity  $n$  and  $t_1, \dots, t_n$  are some terms, then  $R(t_1, \dots, t_n)$  is a condition
3. If  $t_1$  and  $t_2$  are terms, then  $t_1 = t_2$  is a condition
4. If  $B$  is a DRS, then  $\neg B$  is a condition
5. If  $B_1$  and  $B_2$  are DRSs, then  $B_1 \vee B_2$  is a condition
6. If  $B_1$  and  $B_2$  are DRSs, then  $B_1 \Rightarrow B_2$  is a condition
7. Nothing else is a DRS or a condition

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## The standard (top down) construction algorithm

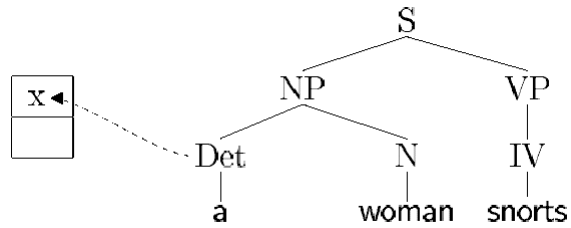
- Start w/ parse tree & feed info from initial sentence into a box, top-down, left-right
- Example: a woman snorts
- Step 1

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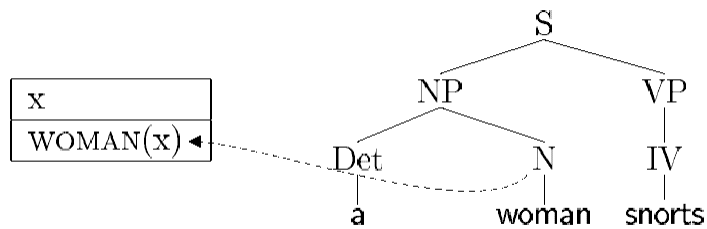
## Step 2 a...



What conditions attach to this discourse referent?  
Move to N node

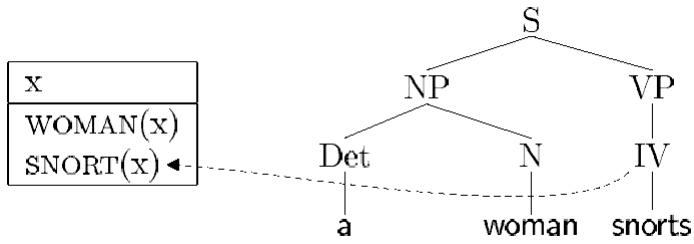
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## Step 3 `...woman...`



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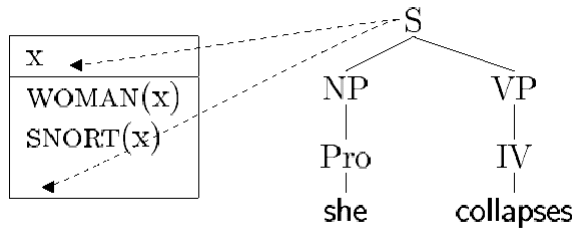
## Step 4 ...snorts...



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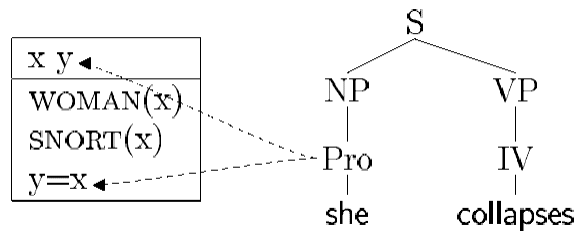
## 2<sup>nd</sup> sentence

Add info straight into box for the first...



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## Add new discourse referent...



(note that x is accessible to y  
What about every woman snorts. She collapses)

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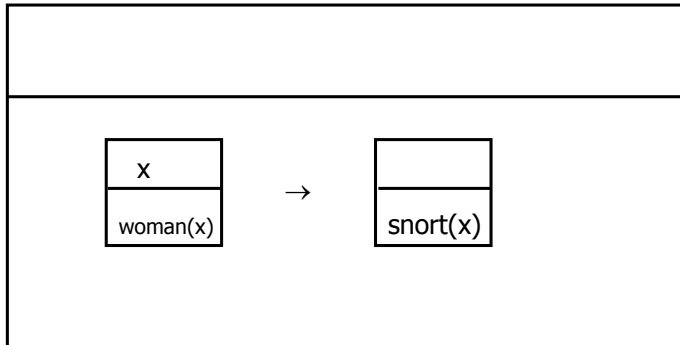
## Examples

- A woman snorts. She collapses
- x,y belong to the same universe, x is accessible to y
- Every woman snorts. ? She collapses
- In this case, we have:

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## Calculating accessibility

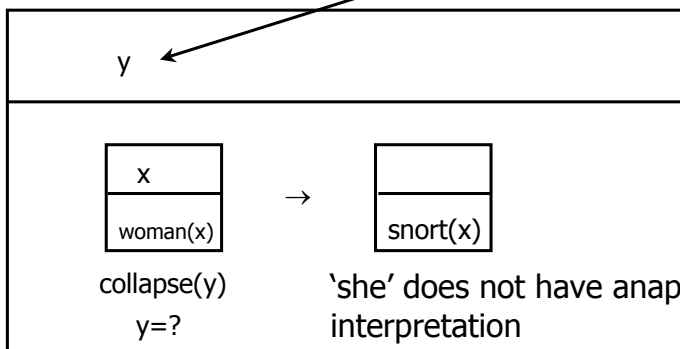
- Every woman snorts.



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## Calculating accessibility

- Every woman snorts. She collapses.



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## Pronouns, anaphora, accessibility

- John bought a book. It is a best-seller
- John bought a Porsche or a Prius. It is a best-seller
- John did not buy a Porsche. It is a best-seller
- John did not buy a five dollar shake. Vincent tasted it

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## Accessibility – the major constraint on anaphora

- ~~DRS  $B_1$  is accessible from DRS  $B_2$  iff  $B_1 = B_2$  or  $B_1$  subordinates  $B_2$~~
- $B_1$  subordinates  $B_2$  iff
  1.  $B_1$  immediately subordinates  $B_2$  or
  2. There is some DRS  $B$  s.t.  $B_1$  subordinates  $B$  and  $B$  subordinates  $B_2$
- $B_1$  immediately subordinates  $B_2$  iff
  1.  $B_1$  contains a condition of the form  $\neg B_2$ ; or
  2.  $B_1$  contains a condition of the form  $B_2 \vee B$  or  $B \vee B_2$  for some DRS  $B$ ; or
  3.  $B_1$  contains a condition of the form  $B_2 \Rightarrow B$ ; or
  4.  $B_1 \Rightarrow B_2$  is a condition in some DRS  $B$

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## Pronoun accessibility

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- Suppose a pronoun has introduced a new discourse referent  $y$  into the universe of some DRS  $B$ . Then we are only free to add the condition  $y=x$  to the condition set of  $B$  if  $x$  is accessible from  $y$

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## DRSs and FOL (with equality)

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- Can map any DRS to FOL statements
- Can do the reverse – FOL to DRS
- Method: by construction, piece by piece

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## Lost in translation: DRS to FOL

- Empty boxes
- Basic conditions & atomic formulas
- Complex conditions (negations and disjunctions)
- Implications
  - When antecedent is empty
  - When it is not

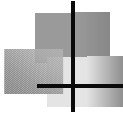
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## Non-empty boxes - translation

$x_1, \dots, x_n$
$\gamma_1$
$\cdot$
$\cdot$
$\cdot$
$\gamma_m$

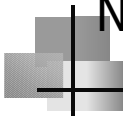
$$\left( \begin{array}{c} x_1, \dots, x_n \\ \gamma_1 \\ \cdot \\ \cdot \\ \cdot \\ \gamma_m \end{array} \right)^t = \exists x_1 \dots \exists x_n ((\gamma_1)^t \wedge \dots \wedge (\gamma_m)^t)$$

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$$\left( \begin{array}{c} \gamma_1 \\ \cdot \\ \cdot \\ \cdot \\ \gamma_m \end{array} \right) \Rightarrow \mathbf{K}^t = ((\gamma_1)^t \wedge \cdots \wedge (\gamma_m)^t) \rightarrow \mathbf{K}^t$$

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## Negations and disjunctions

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$$\begin{aligned} (\neg \mathbf{K})^t &= \neg(\mathbf{K})^t \\ (\mathbf{K}_1 \vee \mathbf{K}_2)^t &= (\mathbf{K}_1)^t \vee (\mathbf{K}_2)^t \end{aligned}$$

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## Translating $\Rightarrow$ nonempty universe

---

$x_1, \dots, x_n$
$\gamma_1$
$\cdot$
$\cdot$
$\cdot$
$\gamma_m$

$$\Rightarrow \mathbf{K}^t = \forall x_1 \dots \forall x_n ((\gamma_1)^t \wedge \dots \wedge (\gamma_m)^t) \rightarrow (\mathbf{K})^t$$

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## Antecedent has empty universe

---

$\gamma_1$
$\cdot$
$\cdot$
$\cdot$
$\gamma_m$

$$\Rightarrow \mathbf{K}^t = ((\gamma_1)^t \wedge \dots \wedge (\gamma_m)^t) \rightarrow \mathbf{K}^t$$

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## Translating DRSs to FOL (with equality)

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- Empty DRS is just T
- No conditions (empty bottom box) is

$$\exists x_1 \dots \exists x_n T$$

- Empty universe

$$(\gamma_1)^t \wedge \dots \wedge (\gamma_n)^t$$

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## From FOL to DRS

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$(\phi)^{dr}$

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# Atomic formulas

*Discourse Referents*

*Conditions*

$$(\tau_1 = \tau_2)^{dr}$$

*Conditions*

*Discourse Referents*

*Conditions*

$$\tau_1 = \tau_2$$

*Conditions*

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# Negation conversion

*Discourse Referents*

*Conditions*

$$(\neg\phi)^{dr}$$

*Conditions*

*Discourse Referents*

*Conditions*

$$\neg \begin{array}{|c|} \hline \phantom{\phi} \\ \hline \end{array}$$

$(\phi)^{dr}$

*Conditions*

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## Existential conversion

*Discourse Referents*

*Conditions*

$(\exists x\phi)^{dr}$

*Conditions*

$x,$  *Discourse Referents*

*Conditions*

$(\phi)^{dr}$

*Conditions*

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## DRSs and lambda calculus

- Use lambdas to represent missing info in DRSs, rather than first-order formulas
- Add merge operator
- Use this to state precisely what it means to fold in info from each sentence in turn
- Also needed for lexical entries

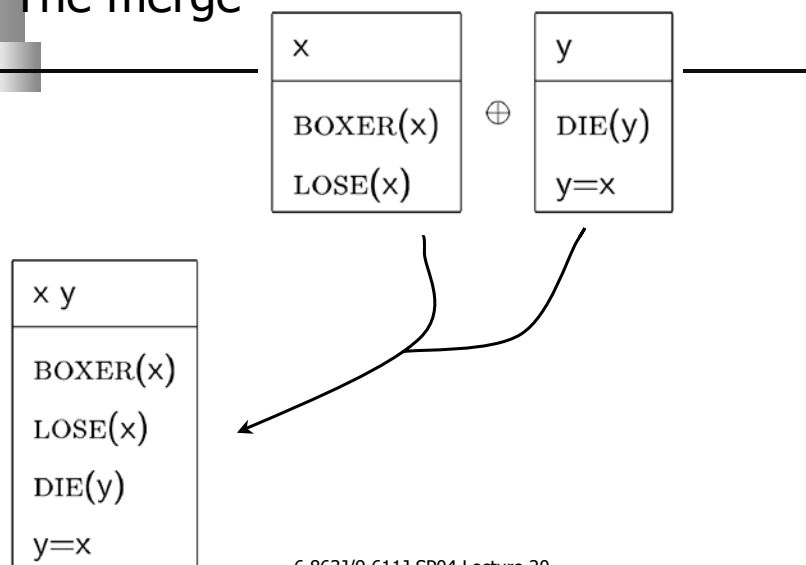
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## Building DRSs with lambda

- Use DRS language, add  $\lambda$ , application operator @, and a new operator, merge,  $\oplus$
- Result:  $\lambda$ -DRT
- Let's see...

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## The merge

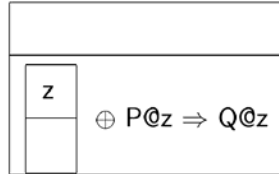


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## DRS and lambda comparison - determiners

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every:  $\lambda P. \lambda Q.$



Every:  $\lambda P. \lambda Q. \forall z(P@z \rightarrow Q@z)$

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## "every"

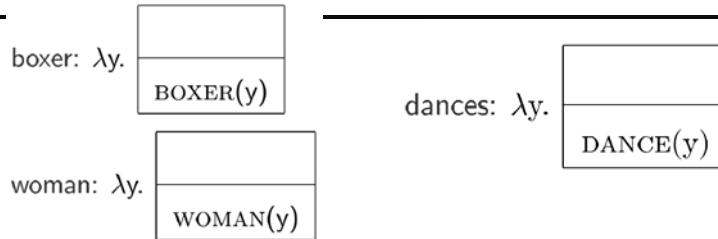
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- The abstracted variable P marks the missing restriction info; while Q marks the missing nuclear scope
- The quantificational force obtains by using a combination of the box and implicational sign, analogous to the universal quantifier and the implicational arrow in the other

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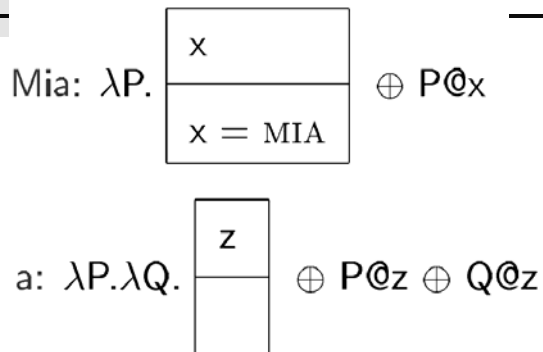


## Lexical items: Nouns, and Intrans V



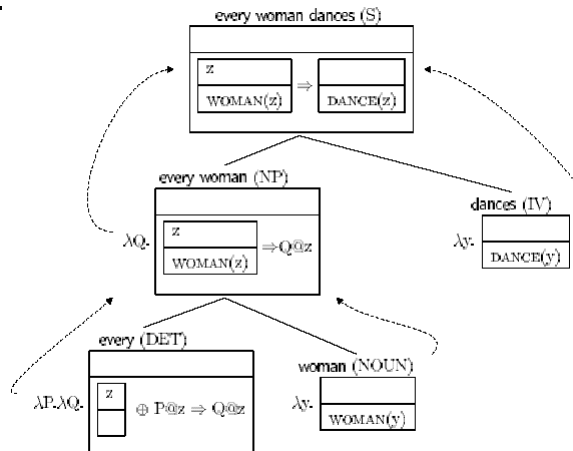
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## Proper names, Determiners



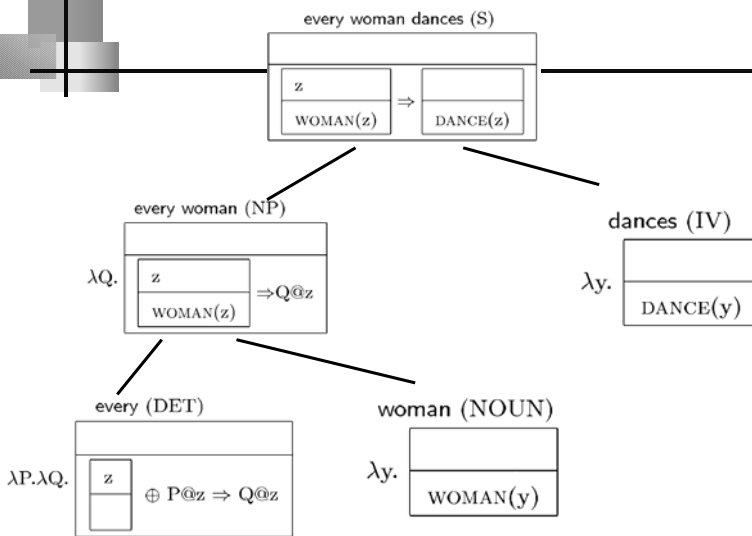
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# Every woman dances



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# Every woman dances



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## Examples

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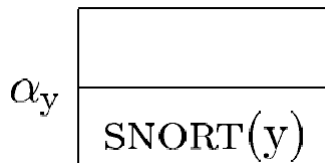
- Mia didn't order a five dollar shake. ?Vincent tasted it
- Why?
- Are these the only constraints?
- Butch threw a vase at the wall
- It broke
- Butch walks into his modest kitchen. He opens the refrigerator. He takes out a milk and drinks it.
- Cf: 'cup of coffee' – in "drink a cup of coffee"

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## Anaphoric pronouns

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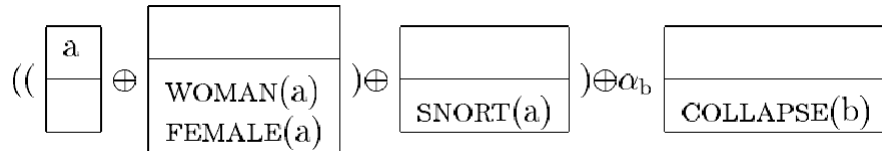
- She snorts
- Put this into box notation with an 'alpha' (for 'anaphoric' as follows:



Like a lambda...

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## Discourse: a woman snorts. She collapses



Must get rid of merges and the alphas to get a pure DRS – this is called resolution

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## Anaphora Resolution

- Input: a stack of DRSs; the first is the DRS under examination, the others all subordinating it
- Output: a copy of the input, but with the merges and pronouns resolved
- Pronoun resolution: Take a DRS from the accessible list and find a unification of the alpha-bound variable and an accessible discourse referent

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## Proper binding constraint

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- Vincent enters the restaurant and Jules watches him

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## Pronouns, anaphora, accessibility

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- John bought a book. It is a best-seller
- John bought a Porsche or a Prius. It is a best-seller
- John did not buy a Porsche. It is a best-seller
- John did not buy a five dollar shake. Vincent tasted it

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## We need more constraint...

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- Too many anaphora possibilities
- So we add notion of focus


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## Presuppositions

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- Jody has no cat. ? Jody loves her cat
- Jody has no cat ? Jody does not love her cat
  
- For these to be OK, presupposed that Jody has a cat...
- Is there a systematic way to compute what is presupposed?

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## Presupposition is not entailment...

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- The couple that won the dance contest was pleased
- The couple that did not win the dance contest was pleased
- Triggered by 'the' ?

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## Three problems with presuppositions

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- The binding problem
- The projection problem
- The accommodation problem

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## Binding

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- A boxer nearly escaped from his apartment
- What is the presupposition?
- Someone has an apartment
- In particular, it's possible: the boxer we are talking about has an apartment

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## Projection problem

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- Mia's cat is at the vet (presupposes that Mia has a cat)
- If Mia has a cat, then her cat is at the vet (does not presuppose that Mia has a cat)
- Answer: presuppositions introduce new 'anaphoric' DRSs (not just new discourse referents, like pronouns)

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## Presuppositions and DRT

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- Presuppositions are essentially very rich pronouns
- Like ordinary pronouns – use notion of accessibility
- But – they have more descriptive content
- So – they introduce new DRSs