# 6.863J Natural Language Processing Lecture 4: From finite state machines to part-of-speech tagging

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#### The Menu Bar

- Administrivia:
  - Schedule alert: Lab1 due next Monday (Feb 24)
  - Lab 2, handed out Feb 24; due the Weds after this – March 5
- Agenda:
- Kimmo its use and abuse
- Part of speech 'tagging' (with sneaky intro to probability theory that we need)
- Ch. 6 & 8 in Jurafsky

### What Kimmo is good for

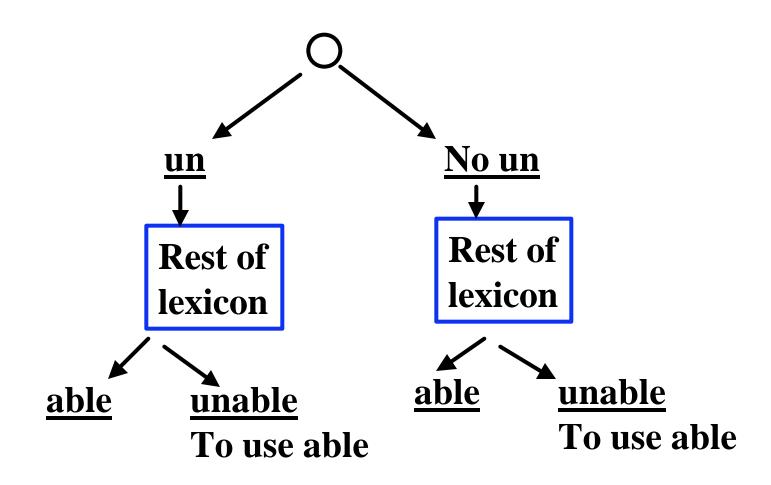
- Ideally: locally, purely concatenative phenomena (obviously, because fsa's)
- FSAs are based *purely* on an associative concatenation operation over strings (i.e., ((a+b)+c) = (a+(b+c)) where =+ concat
- Turkish word: uygarlas,tiramadiklarimizdanmis,sinizcasina

uygar+las,+tir+ama+dik+lar+imiz+dan+mis,+siniz+casina
(behaving) as if you are among those whom we could not
cause to become civilized

### What Kimmo is not good for

- So, this lets us think what the system might not be good for... let's look at English first....
- There seem to be some kinds of 'long distance' constraints...
- Prefix/suffix links: only some prefixes tied to some suffixes
  - Un----able
  - Undoable, uncanny, ?uncannyable, unthinkable, thinkable, readable, unreadable, unkind, \*unkindable
- So, we have to 'keep track' that the un is first or not – what does lexicon look like?

# Lexicon must be (grotesquely) duplicated



# This kind of duplication is a litmus test of something wrong

- Duplication: no relation between the two lexicons, but we know they're identical
- Principle AWP
- We will see this again and again
- Usually means we haven't carved (factored) the knowledge at the right 'joints'
- Solution? Usually more powerful machinery 'overlay' representations

### Not all long distance effects are a barrier...

- Phenomena: Vowel harmony
  - yourgun + sInIz → yorgunsunuz
  - Round vowels assimilate to round vowels; back vowels to back, etc. - all the way from left to right

 Can Kimmo do it? What would be your model?

# Parsing words with Kimmo is computationally intractable

- Intuition: what if the characters on the surface don't give any clues as to what 'features' they ought to have underlyingly? (e.g., whether a Noun or a Verb, as in police police police)
- This seems awfully close to the famous 3-SAT problem: is there an assignment of T(rue), F(alse) to the literals of an arbitray Boolean formula in 3-conjunctive normal form s.t. the formula evaluates to true?
- In fact, we can simulate this problem using Kimmo

#### 3-Sat

Given (arb) cnf formula, e.g.,

$$(\overline{x} \lor y \lor \overline{z}) \land (\overline{y} \lor q \lor p) \land (x \lor q \lor z)$$

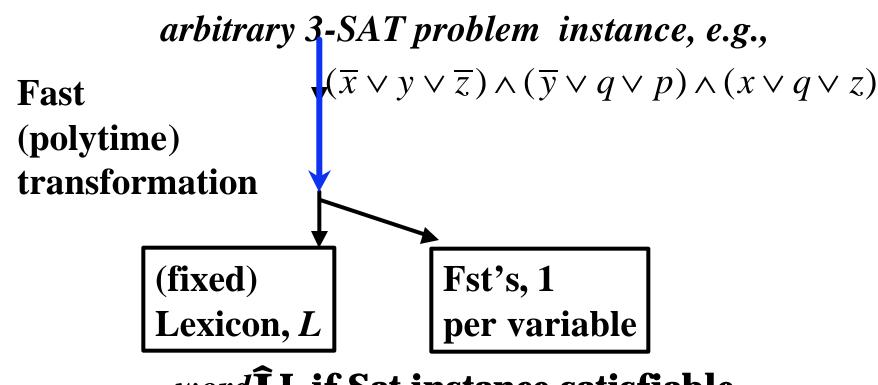
- We can't figure out quickly (in deterministic polynomial time) whether there is an assignment of true or false to literals x, y, z in order to make the formula eval to true just by inspecting the local surface string
- We could guess this in polynomial time i.e., Nondeterministic Polynomial, or NP time (time measured in length of the formula)

# Reduction of 3-Sat to Kimmo recognition problem

 For every 3-Sat problem, we can find (in poly time) a corresponding Kimmo word recognition problem where there's a valid word if the 3-Sat problem was satisfiable

 If Kimmo recognition could be done in det poly time (P) then so could 3-SAT

### The reduction



word I L if Sat instance satisfiable

If we could solve Kimmo recognition easily,

Then we could solve 3-Sat easily

### Why should we care?

- This is typical of a combination of 'agreement and ambiguity' that trickles through all of natural language
- The agreement part like Turkish vowel harmony
- The ambiguity part like the police police police example
- Suggests that speed won't come from the formalism <u>all by itself</u>

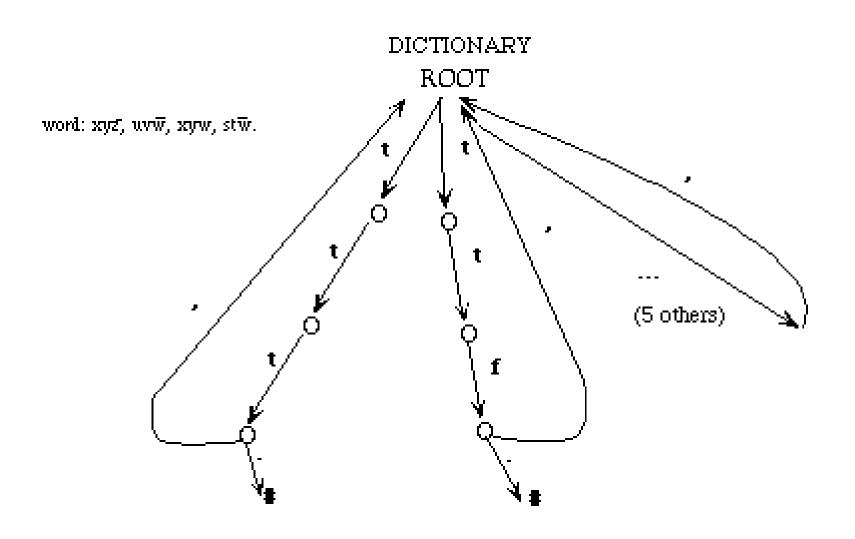
### Two components to 3-Sat

- The fact that an x that has a truth assignment in one place, must have the same truth assignment everywhere - what morphological process is that like?
- The fact that every triple must have at least 1 'T' underlyingly (so that the triple is true) - what morphological process is that like?

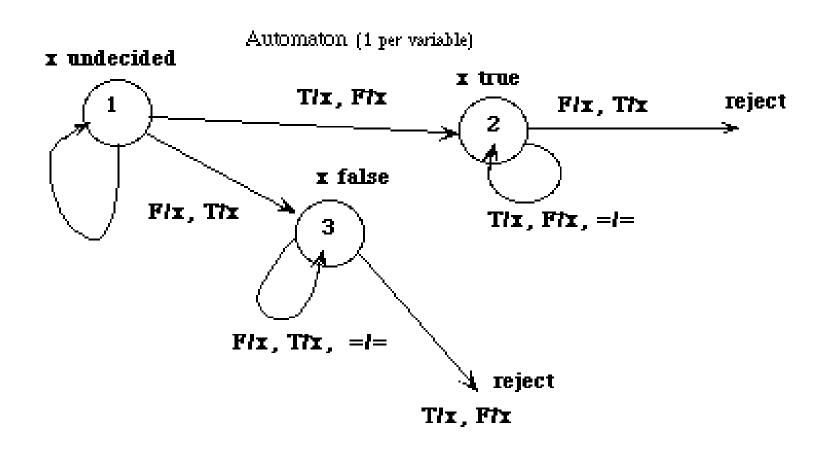
### Two components

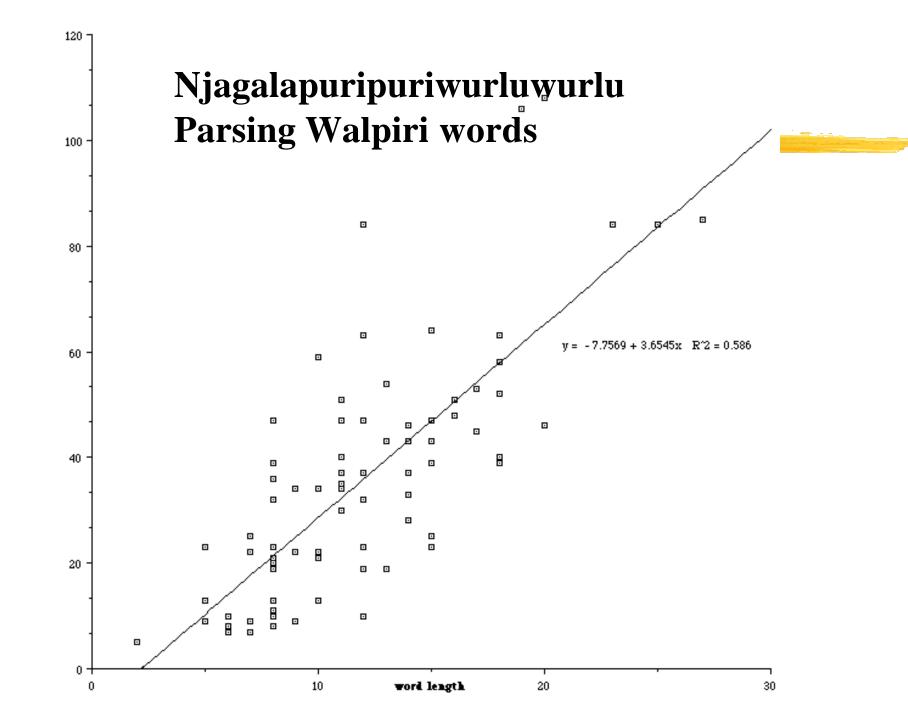
- Agreement: vowel harmony (if round at some point, round everywhere)
- Ambiguity: we can't tell what the underlying value of x is from the surface, but if there's at least one "t" per 'part of word', then we can spell out this constraint in dictionary
- Note that words (like Sat formulas) must be arbitrarily long... (pas de probleme)
- Dictionary is fixed...
- # of Vowel harmony processes corresponds to # of distinct literals

# Reduce until done – formula must eval to *true*



# Reduce until done: assignment consistency





# Then can be *indescribable* words (for an fst)

- Can we even do all natural languages?
- Example: Bambarra (African language in Mali)
- Words in form Noun+o+Noun, as in wuluowulo ='whichever dog'
- Also have repeated endings (like anti-anti...)
   wulu+nyini+la ='dog searcher'
   wulunyinina+ nyini+la ='one who searches for dog searchers'
- Fatal bite: combine with word o formation: wulunyininanyinila o wulunyininanyinila (arbitrarily long!)

### Paradigmatic example for NLP

- Morphophonemic parsing
- Given surface form, recover underlying form:

morpho-phonem-ic

### Two ways

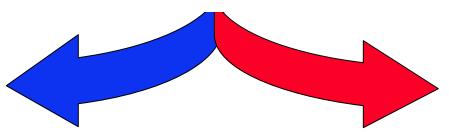
- Generative model concatenate then fix up joints
  - stop + -ing = stopping, fly + s = flies
  - Use a cascade of transducers to handle all the fixups
- Probabilistic model some constraints on morpheme sequences using prob of one character appearing before/after another
  - prob(ing | stop) vs. prob(ly| stop)
- (much more about prob in just one moment)

### Two ways of looking at language & the Great Divide

 Text understanding vs. Information Retrieval (IR)

 Info retrieval example: name extraction; how does Google correct "Britney Speers"

# The Great Divide in NLP: the red pill or the blue pill?



"Knowledge
Engineering" approach
Rules built by hand w/
K of Language
"Text understanding"

"Trainable Statistical"
Approach
Rules inferred from lots
of data ("corpora")
"Information retrieval"

### The big picture II

- In general: 2 approaches to NLP
- Knowledge Engineering Approach
  - Grammars constructed by hand
  - Domain patterns discovered by human expert via introspection & inspection of 'corpus'
  - Laborious tuning
- Automatically Trainable Systems
  - Use statistical methods when possible
  - Learn rules from annotated (or o.w. processed) corpora

# What is part of speech tagging & why?

INPUT: the lead paint is unsafe

Output: the/Det lead/N paint/N is/V unsafe/Adj

Or: BOS the lyric beauties of Schubert 's Trout Quintet: its elemental rhythms and infectious melodies: make it a source of pure pleasure for almost all music listeners./

### Tagging for this...

```
The/DT lyric/JJ beauties/NNS of/IN
Schubert/NNP 's/POS Trout/NNP Quintet/NNP
--/:
its/PRP$ elemental/JJ rhythms/NNS
and/CC infectious/JJ melodies/NNS
--/: make/VBP it/PRP
a/DT source/NN of/IN pure/JJ pleasure/NN
for/IN almost/RB all/DT music/NN listeners/NNS ./.
```

### (Next step: bracketing...)

```
[The/DT lyric/JJ beauties/NNS]
of/IN
[ Schubert/NNP 's/POS Trout/NNP Quintet/NNP ]
--/:
[its/PRP$ elemental/JJ rhythms/NNS]
and/CC [infectious/JJ melodies/NNS]
--/: make/VBP [ it/PRP ]
[ a/DT source/NN ] of/IN [ pure/JJ pleasure/NN ]
for/IN almost/RB [all/DT music/NN listeners/NNS]./.
```

### What's it good for?

- Tags = parts-of-speech (but see later)
- Uses:
  - text-to-speech (how do we pronounce "lead"?)
  - can write regexps like Det Adj\* N\* over the output
  - preprocessing to speed up parser (but a little dangerous)
  - if you know the tag, you can back off to it in other tasks
  - Back-off: trim the info you know at that point

# An exemplar for the divide: "tagging" text

- Input: the lead paint is unsafe
   Output: the/Det lead/N paint/N is/V unsafe/Adj
- Can be challenging:
  - I know that
  - I know that block
  - I know that blocks the sun
- new words (OOV= out of vocabulary); words can be whole phrases ("I can't believe it's not butter")

### What are tags?

- Bridge from words to parsing but not quite the morphemic details that Kimmo provides (but see next slide)
- Idea is more divide-and-conquer and depends on task
- "Shallow" analysis for "shallow parsing"

### More sophisticated – use features

- Word form:  $A^+ \rightarrow 2^{(L,C1,C2,...,Cn)} \rightarrow T$ 
  - He always books the violin concert tickets early.
    - books → {(book-1,Noun,PI,-,-),(book-2,Verb,Sg,Pres,3)}
    - tagging (disambiguation): ... → (Verb,Sg,Pres,3)
  - ...was pretty good. However, she did not realize...
    - However → {(however-1,Conj/coord,-,-,-), (however- 2,Adv,-,-,-)}
    - tagging: ...  $\rightarrow$  (Conj/coord,-,-,-)

### Why should we care?

- The first statistical NLP task
- Been done to death by different methods
- Easy to evaluate (how many tags are correct?)
- Canonical finite-state task
  - Can be done well with methods that look at local context
  - Though should "really" do it by parsing!
- Sneaky: Introduce probabilistic models paradigmatic contrast investigated in Lab 2.

### Why should we care?

- "Simplest" case of recovering surface, underlying form via statistical means
- We are modeling p(word seq, tag seq)
- The tags are hidden, but we see the words
- Is tag sequence X likely with these words?

### Two approaches

 Noisy Channel Model (statistical) – what's that?? (we will have to learn some statistics)

Deterministic baseline tagger composed with a cascade of fixup transducers
 These two approaches will the guts of Lab 2 (lots of others: decision trees, ...)

### Example tagsets

- 87 tags Brown corpus
- Three most commonly used:
- 1. Small: 45 Tags Penn treebank (Medium size: 61 tags, British national corpus
- 2. Large: 146 tags

Big question: have we thrown out the right info? Impoverished? How?

### Brown/Upenn corpus tags

	Tag	Description	Example	Tag	Description	Example
	CC	Coordin. Conjunction	and, but, or	SYM	Symbol	+,%, &
	CD	Cardinal number	one, two, three	TO	"to"	to
	DT	Determiner	a, the	UH	Interjection	ah, oops
	EX	Existential 'there'	there	VB	Verb, base form	eat
	FW	Foreign word	mea culpa	VBD	Verb, past tense	ate
	IN	Preposition/sub-conj	of, in, by	VBG	Verb, gerund	eating
	JJ	Adjective	yellow	VBN	Verb, past participle	eaten
	JJR	Adj., comparative	bigger	VBP	Verb, non-3sg pres	eat
	JJS	Adj., superlative	wildest	VBZ	Verb, 3sg pres	eats
	LS	List item marker	1, 2, One	WDT	Wh-determiner	which, that
	MD	Modal	can, should	WP	Wh-pronoun	what, who
	NN	Noun, sing. or mass	llama	WP\$	Possessive wh-	whose
	NNS	Noun, plural	llamas	WRB	Wh-adverb	how, where
	NNP	Proper noun, singular	IBM	\$	Dollar sign	\$
S	NNPS	Proper noun, plural	Carolinas	#	Pound sign	#
	PDT	Predeterminer	all, both	66	Left quote	(' or ")
	POS	Possessive ending	'S	"	Right quote	(' or '')
	PP	Personal pronoun	I, you, he	(	Left parenthesis	([,(,{,<)
	PP\$	Possessive pronoun	your, one's	)	Right parenthesis	$(],),\},>)$
	RB	Adverb	quickly, never	,	Comma	,
	RBR	Adverb, comparative	faster		Sentence-final punc	(.!?)
	RBS	Adverb, superlative	fastest	:	Mid-sentence punc	(:;)
	RP	Particle	up, off			·

J. text, p. 297 Fig 8.6 1M words 60K tag counts

### Current performance

Input: the lead paint is unsafe

Output: the/Det lead/N paint/N is/V unsafe/Adj

- How many tags are correct?
  - About 97% currently
  - But baseline is already 90%
    - Baseline is performance Homer Simpson algorithm:
    - Tag every word with its most frequent tag
    - Tag unknown words as nouns
- How well do people do?

```
correct tags
        Det Noun Prep Noun Prep Det Noun
  Verb
/directed
            cortege of autos through the dunes
         a
        Det Noun Prep Noun Prep Det Noun
  Verb
        Noun Verb
             Adj
                       some possible tags for
              Prep
                       each word (maybe more)
```

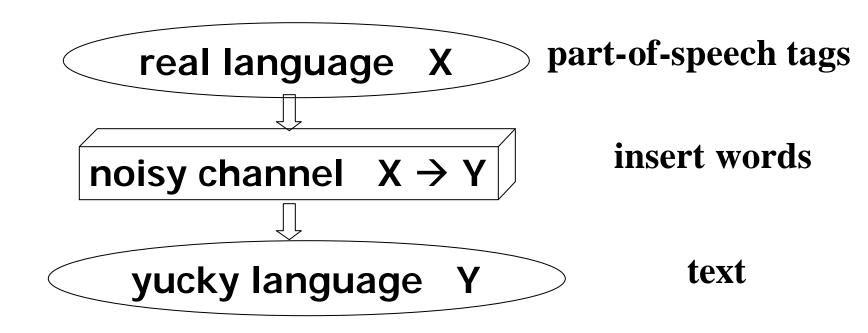
correct tags Det Noun Prep Noun Prep Det Noun Verb cortege of autos through the dunes *directed* a Det Noun Prep Noun Prep Det Noun Noun Verb Adi some possible tags for Prep each word (maybe more)

correct tags Verb Det Noun Prep Noun Prep Det Noun a cortege of autos through the dunes Bill directed\ Det Noun Prep Noun Prep Det Noun loun Verb Adi some possible tags for each word (maybe more) Prep

correct tags Det Noun Prep Noun Prep Det Noun Verb cortege of autos through the dunes *directed* a Det Noun Prep Noun Prep Det Noun Noun Verb Adi some possible tags for Prep each word (maybe more)

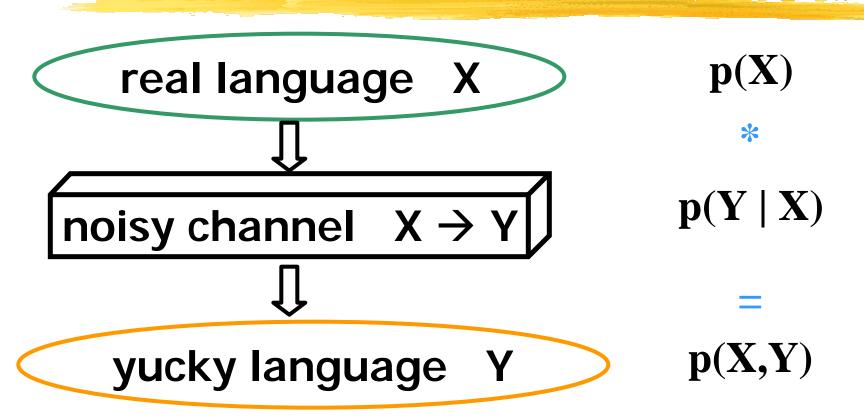
## Finite-state approaches

Noishy Chunnel Muddle (statistical)



want to recover X from Y

## Noisy channel – and prob intro

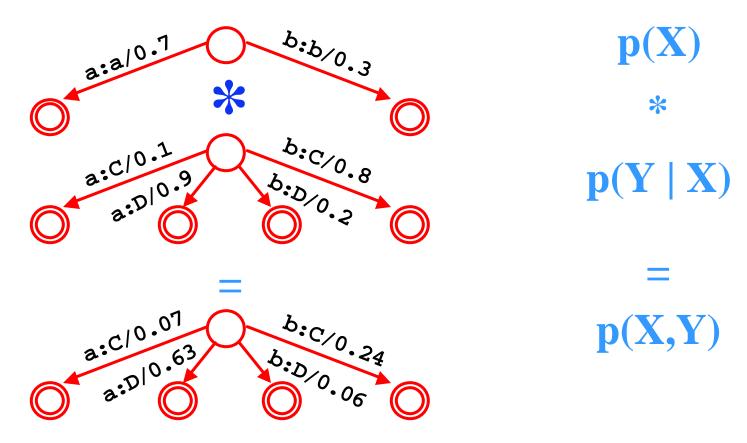


choose sequence of tags X that maximizes p(X | Y) [oops... this isn't quite correct... need 1 more step]

## Noisy channel maps well to our fsa/fst notions

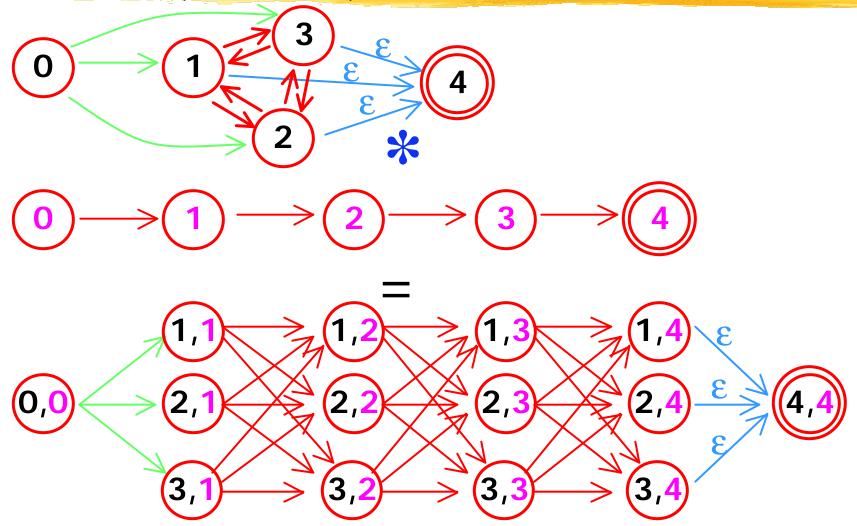
- What's p(X)?
- Ans: p(tag sequence) i.e., some finite state automaton
- What's p(Y|X)?
- Ans: transducer that takes tags→words
- What's P(X,Y)?
- The joint probability of the tag sequence, given the words (well, gulp, almost... we will need one more twist – why? What is Y?)

# The plan modeled as composition (x-product) of finite-state machines



Note p(x,y) sums to 1.

Cross-product construction for fsa's (or fst's)



#### Pulled a bit of a fast one here...

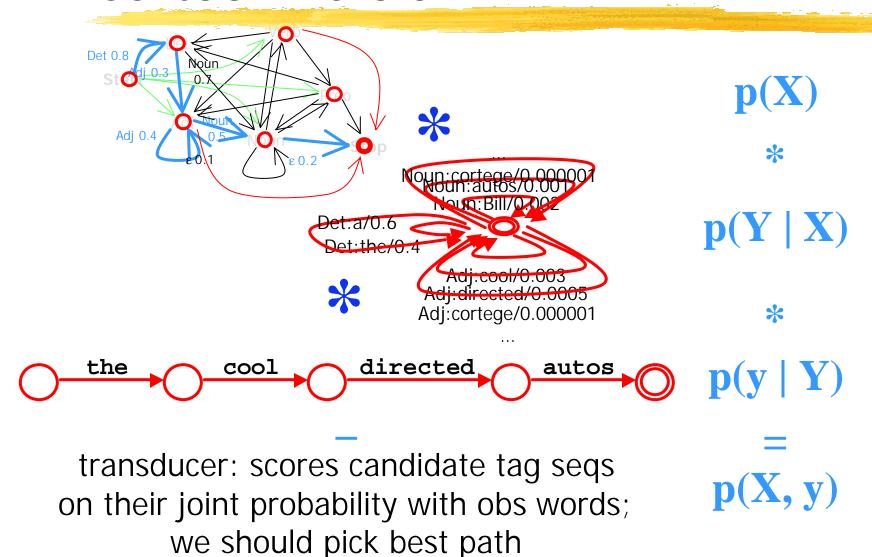
- So far, we have a plan to compute P(X,Y) but is this correct?
- Y= all the words in the world
- X= all the tags in the world (well, for English)
- What we get to see as input is yÎY not Y!
- What we want to compute is REALLY this:

want to recover  $x\hat{I}X$  from  $y\hat{I}Y$  choose x that  $\underline{maximizes} p(X | y)$  so...

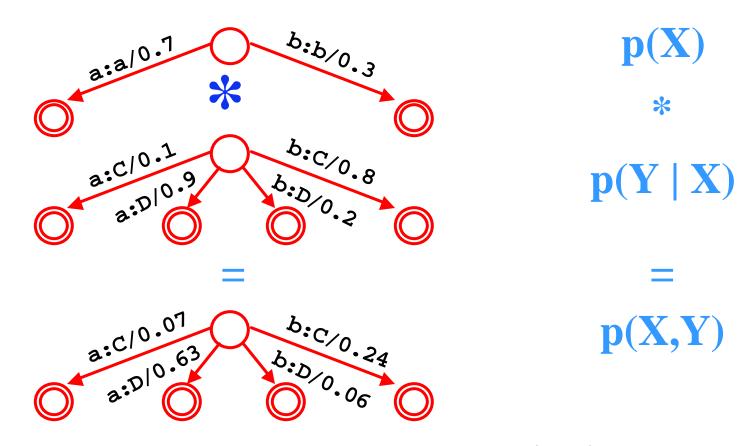
## The real plan...

```
\mathbf{p}(\mathbf{Y} \mid \mathbf{X})
                                                        *
                                                \mathbf{p}(\mathbf{y} \mid \mathbf{Y})
Find x that maximizes
this quantity
```

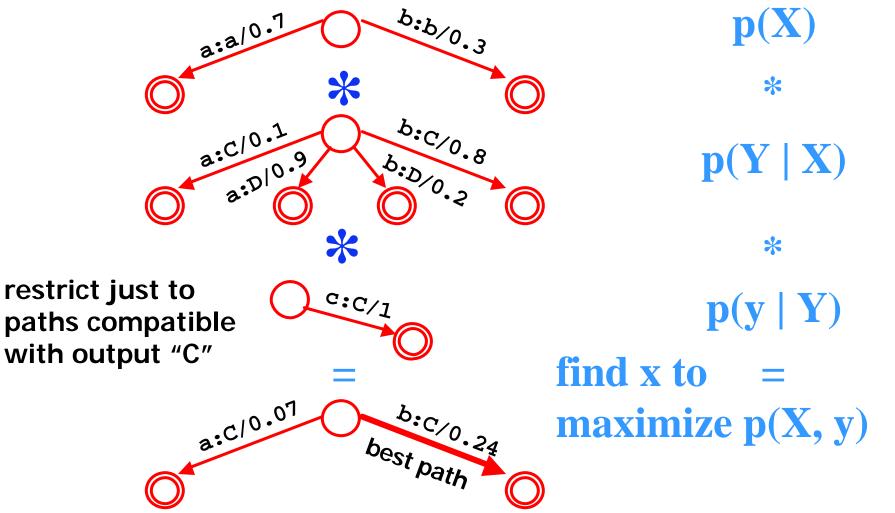
#### Cartoon version



# The plan modeled as composition (product) of finite-state machines



Note p(x,y) sums to 1. Suppose y="C"; what is best "x"? We need to factor in one more machine that models the actual word sequence, y



### The statistical view, in short:

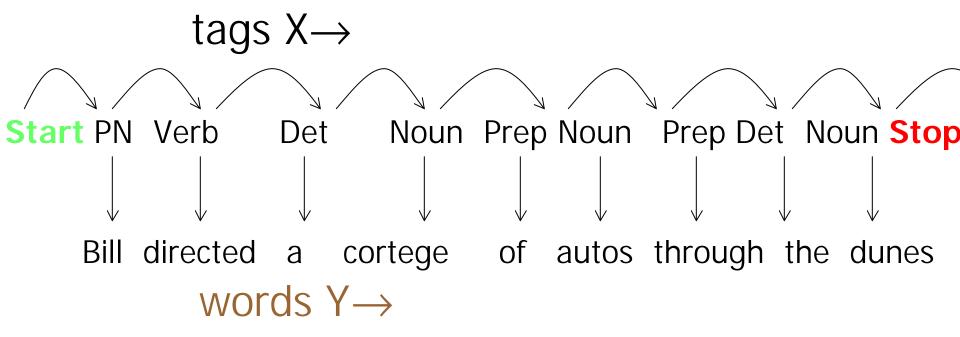
- We are modeling p(word seq, tag seq)
- The tags are hidden, but we see the words
- What is the most likely tag sequence?
- Use a finite-state automaton, that can emit the observed words
- FSA has limited memory
- AKA this Noisy channel model is a "<u>Hidden</u> <u>Markov Model</u>" -

## Put the punchline before the joke

Bill directed a cortege of autos through the dunes

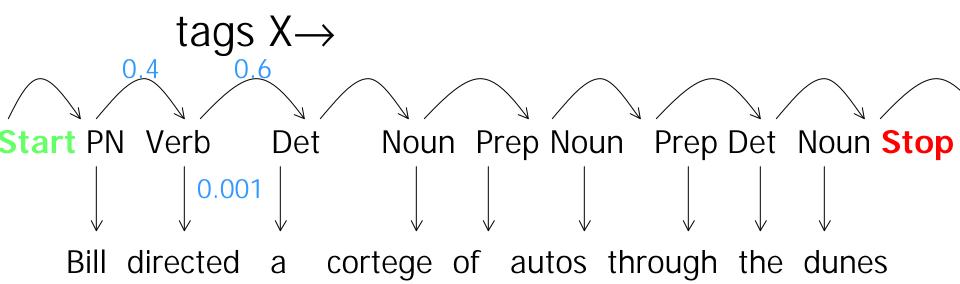


# Punchline – recovering (words, tags)



Find tag sequence X that maximizes probability product

## Punchline – ok, where do the pr numbers come from?

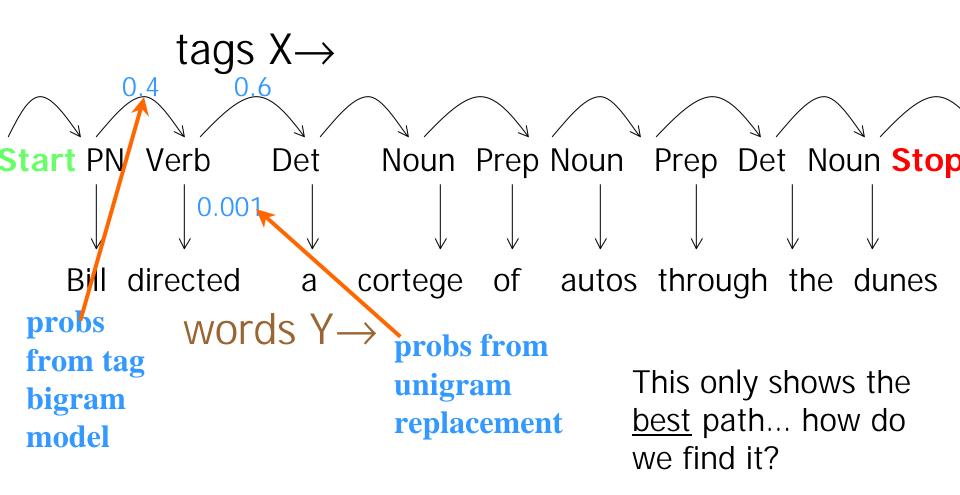


the tags are not observable & they are states of some fsa We estimate transition probabilities between states We also have 'emission' pr's from states

En tout: a <u>Hidden Markov Model</u> (HMM)

words  $Y \rightarrow$ 

# Our model uses <u>both</u> *bigrams* & unigrams:



## What are unigrams and bigrams?

- Letter or word frequencies: 1-grams
  - useful in solving cryptograms: ETAOINSHRDLU...
- If you know the previous letter: 2-grams
  - "h" is rare in English (4%; 4 points in Scrabble)
  - but "h" is common after "t" (20%)
- If you know the previous 2 letters: 3-grams
  - "h" is really common after " " "t" etc. ...

#### In our case

- Most likely word? Most likely tag t given a word
   w? = P(tag|word)
- Task of predicting the next word
- Woody Allen:

"I have a gub"

In general: predict the N<sup>th</sup> word (tag) from the preceding N-1 word (tags) aka N-gram

Homer Simpson: just use the current word (don't look at context) = unigram (1-gram)

## How far should we go?

- "long distance\_\_\_\_"
- Next word? Call?
- p(w<sub>n</sub>|w
- Consider special case above
- Approximation says that
   | long distance call|/|distance call| ≈ |distance call|/|distance|
- If context 1 word back = bigram
- But even better approx if 2 words back: *long distance*\_\_\_\_\_ Not always right: long distance runner/long distance call
- Further you go: collect long distance\_\_\_\_\_

## 3-gram

[Genmetheyesse orils of Ted you doorder [6], the Grily Capiduatent pildred and For thy werarme: nomiterst halt i, what production the Covers, in calt cations on wile ars, was name conch rom the exce of the man, Winetwentagaint up, and and All. And of Ther so i hundal panite days th the res of th rand ung into the forD six es, wheralf the hie soulsee, frelatche rigat. And the LOperact camen unismelight fammedied: and nople,

## 4-gram

[1] By the returall benefit han every familitant of all thou go? And At the eld to parises of the nursed by thy way of all histantly be the ~aciedfag . to the narre gread abrasa of thing, and vas these convuning clann com to one language; all Lah, which for the greath othey die. -

## 5-gram

[Gen 3:1] In the called up history of its opposition of bourgeOIS AND Adam to rest, that the existing of heaven; and land the bourgeoiS ANger anything but concealed, the land whethere had doth know ther: bury thy didst of Terature their faces which went masses the old society [2] is the breaks out of oppressor of all which, the prolETARiat goest, unto German pleast twelves applied in manner with these, first of this polities have all

## 3-word-gram

[Gen 4:25] And Adam gave naines to ail feudal, patriarchal, idyllic relations. It bas but -established new classes, new conditions of oppression, new forme of struggle in place of the West? The bourgeoisie keeps more and more splitting up into two great lights; the greater light to rule the day of my house is this Eliezer of Damascus.

How far can we go??

## Shakespeare in lub... The unkindest cut of all

- Shakespeare: 884,647 words or tokens (Kucera, 1992)
- 29,066 types (incl. proper nouns)
- So, # bigrams is 29,066<sup>2</sup> > 844 million. 1 million word training set doesn't cut it only 300,000 difft bigrams appear
- Use backoff and smoothing
- So we can't go very far...

## Where do these probability info estimates come from?

- Use tagged <u>corpus</u> e.g. "Brown corpus" 1M words (fewer token *instances*); many others – Celex 16M words
- Use <u>counts</u> (relative frequencies) as estimates for probabilities (various issues w/ this, these so-called <u>Maximum-Likelihood estimates</u> – don't work well for low numbers)
- Train on texts to get estimates use on new texts

## Bigrams, fsa's, and Markov models – take two

- We approximate p(tag| all previous tags)
   Instead of
   p(rabbit|Just then the white...) we use:
   P(rabbit|white)
- This is a <u>Markov assumption</u> where past memory is limited to immediately previous state – just 1 state corresponding to the previous word or tag

## Smoothing

- We don't see many of the words in English (uniqram)
- We don't see the huge majority of bigrams in English
- We see only a tiny sliver of the possible trigrams
- So: most of the time, bigram model assigns p(0) to bigram:
  - p(food|want) = |want food| /|want| = 0/whatever

But means event can't happen – we aren't warranted to conclude this... therefore, we must adjust...how?

## Simplest idea: add-1 smoothing

- Add 1 to every cell of
- P(food | want) = |want to|  $\div$  |want| = 1  $\div$  2931 = .0003

# Initial counts – Berkeley restaurant project

	I	want	to	eat	Chinese	food	lunch
I	8	1087	0	13	0	0	0
want	3	0	786	0	6	8	6
to	3	0	10	860	3	0	12
eat	0	0	2	0	19	2	52
Chinese	2	0	0	0	0	120	1
food	19	0	17	0	0	0	0
lunch	4	0	0	0	0	1	0

	I	want	to	eat	Chinese	food	lunch
Ι	.0023	.32	0	.0038	0	0	0
want	.0025	0	.65	0	.0049	.0066	.0049
to	.00092	0	.0031	.26	.00092	0	.0037
eat	0	0	.0021	0	.020	.0021	.055
Chinese	.0094	0	0	0	0	.56	.0047
food	.013	0	.011	0	0	0	0
lunch	.0087	0	0	0	0	.0022	0



## Old vs. New table

	I	want	to	eat	Chinese	food	lunch
I	.0023	.32	0	.0038	0	0	0
want	.0025	0	.65	0	.0049	.0066	.0049
to	.00092	0	.0031	.26	.00092	0	.0037
eat	0	0	.0021	0	.020	.0021	.055
Chinese	.0094	0	0	0	0	.56	.0047
food	.013	0	.011	0	0	0	0
lunch	.0087	0	0	0	0	.0022	0

	I	want	to	eat	Chinese	food	lunch
Ι	.0018	.22	.00020	.0028	.00020	.00020	.00020
want	.0014	.00035	.28	.00035	.0025	.0032	.0025
to	.00082	.00021	.0023	.18	.00082	.00021	.0027
eat	.00039	.00039	.0012	.00039	.0078	.0012	.021
Chinese	.0016	.00055	.00055	.00055	.00055	.066	.0011
food	.0064	.00032	.0058	.00032	.00032	.00032	.00032
lunch	.0024	.00048	.00048	.00048	.00048	.00096	.00048

## Changes

- All non-zero probs went down
- Sometimes probs don't change much
- Some predictable events become less predictable (P(to|want) [0.65 to 0.22])
- Other probs change by large factors ( P(lunch|Chinese) [0.0047 to 0.001]
- Conclusion: generally good idea, but effect on nonzeroes not always good – blur original model – too much prob to the zeros, we want less 'weight' assigned to them (zero-sum game, 'cause probs always sum to 0)

# Submenu for probability theory – redo n-grams a bit more formally

- Define all this p(X), p(Y|X), P(X,Y) notation
- p, event space, conditional probability & chain rule;
- Bayes' Law
- (Eventually) how do we estimate all these probabilities from (limited) text? (Backoff & Smoothing)

## Rush intro to probability

p(Paul Revere wins | weather's clear) = 0.9

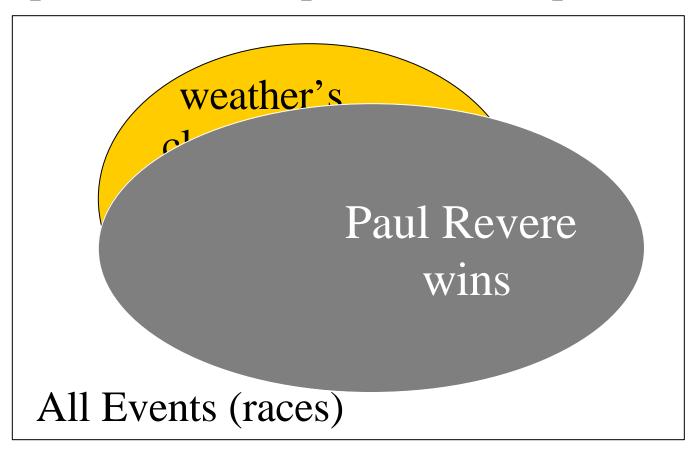
#### What's this mean?

p(Paul Revere wins | weather's clear) = 0.9

- Past performance?
  - Revere's won 90% of races with clear weather
- Hypothetical performance?
  - If he ran the race in many parallel universes ...
- Subjective strength of belief?
  - Would pay up to 90 cents for chance to win \$1
- Output of some computable formula?
  - But then which formulas should we trust?
     p(X | Y) versus q(X | Y)

#### p is a function on event sets

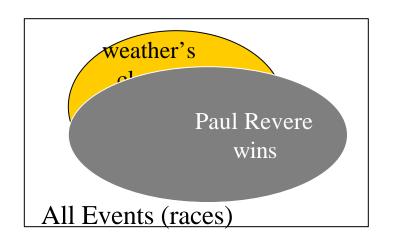
 $p(win | clear) \equiv p(win, clear) / p(clear)$ 



#### p is a function on event sets

$$p(win | clear) \equiv p(win, clear) / p(clear)$$
syntactic sugar
$$logical conjunction predicate selecting$$
of predicates
$$races where$$

$$weather's clear$$



p measures total probability of a set of events.

# Commas in p(x,y) mean conjunction – on the left...

p(Paul Revere wins, Valentine places, Epitaph shows | weather's clear)

what happens as we add conjuncts to left of bar?

- probability can only decrease
- numerator of historical estimate likely to go to zero:

# times Revere wins AND Val places... AND weather's clear # times weather's clear

## Commas in p(x,y)...on the right

p(Paul Revere wins | weather's clear, ground is dry, jockey getting over sprain, Epitaph also in race, Epitaph was recently bought by Gonzalez, race is on May 17, ...)

what happens as we add conjuncts to right of bar?

- probability could increase or decrease
- probability gets more relevant to our case (less *bias*)
- probability *estimate* gets less reliable (more *variance*)

# times Revere wins AND weather clear AND ... it's May 17 # times weather clear AND ... it's May 17

# Backing off: simplifying the right-hand side...

```
p(Paul Revere wins | weather's clear,
ground is dry, jockey getting over sprain, Epitaph
also in race, Epitaph was recently bought by Gonzalez,
race is on May 17, ...)
```

not exactly what we want but at least we can get a reasonable estimate of it!

try to *keep* the conditions that we suspect will have the most influence on whether Paul Revere wins

Recall 'backing off' in using just p(rabbit|white) instead of p(rabbit|Just then a white) – so this is a general method

## What about simplifying the lefthand side?

p(Paul Revere wins, Valentine places, Epitaph shows | weather's clear)

#### **NOT ALLOWED!**

but we can do something similar to help ...

We can FACTOR this information – the so-called "Chain Rule"

## Chain rule: factoring lhs

Makes perfect sense when read from bottom to top

Moves material to right of bar so it can be ignored

If this prob is unchanged by backoff, we say Revere was CONDITIONALLY INDEPENDENT of Valentine and Epitaph (conditioned on the weather's being clear). Often we just ASSUME conditional independence to get the nice product above.

### The plan: summary so far

automaton: p(tag sequence)

p(X)



"Markov Model"

transducer: tags → words

 $p(Y \mid X)$ 

"Unigram Replacement"



automaton: the observed words

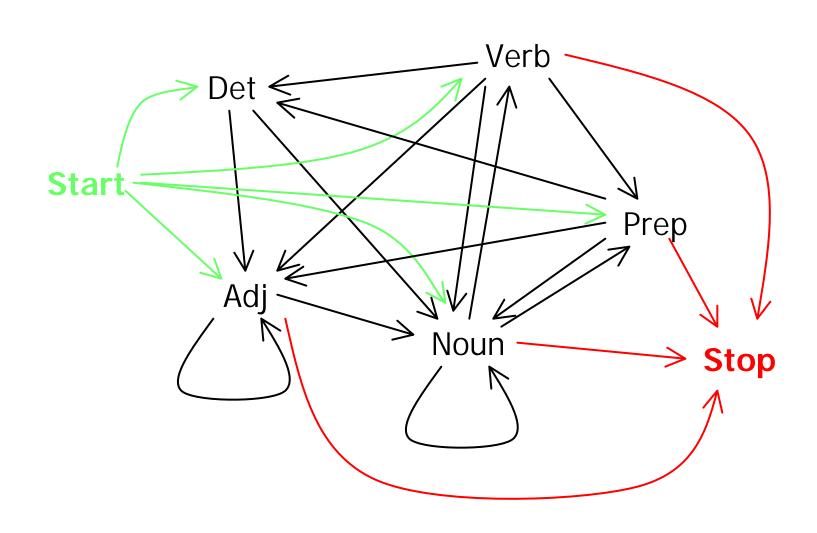
 $p(y \mid Y)$ 

"straight line"

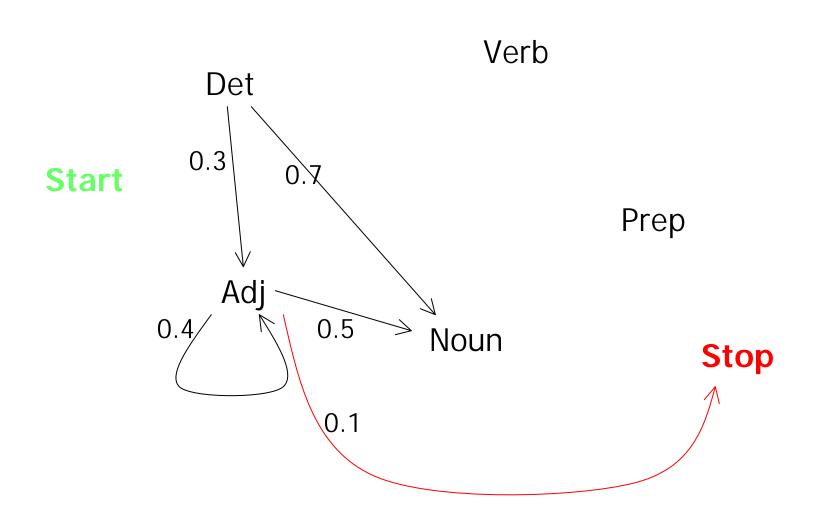
transducer: scores candidate tag seqs on their joint probability with obs words; pick best path

p(X, y)

# First-order Markov (bigram) model as fsa

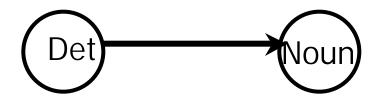


### Add in transition probs - sum to 1

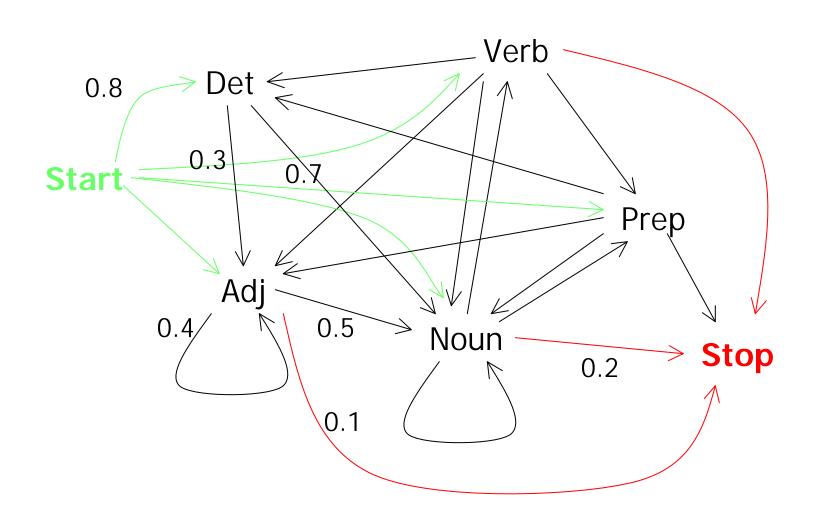


## Same as bigram



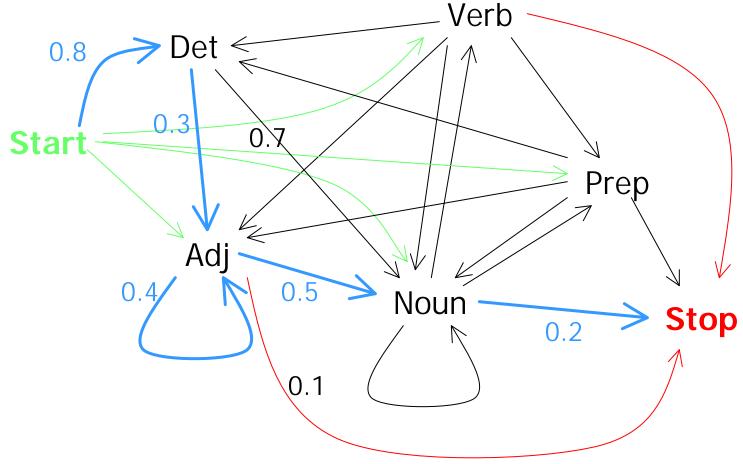


#### Add in start & etc.



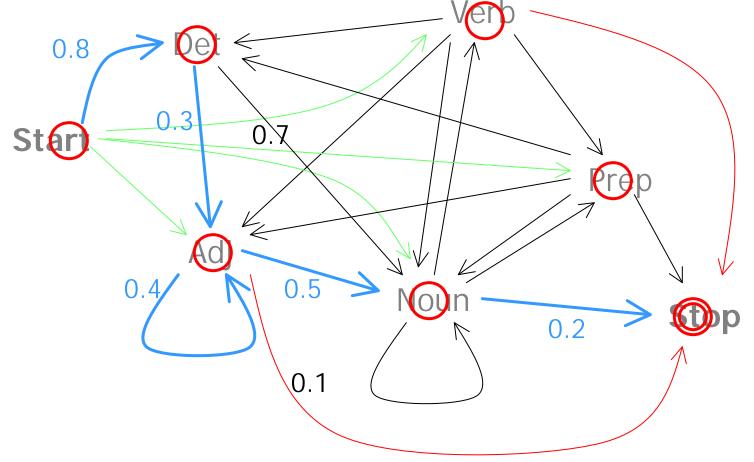
#### Markov Model

p(tag seq)



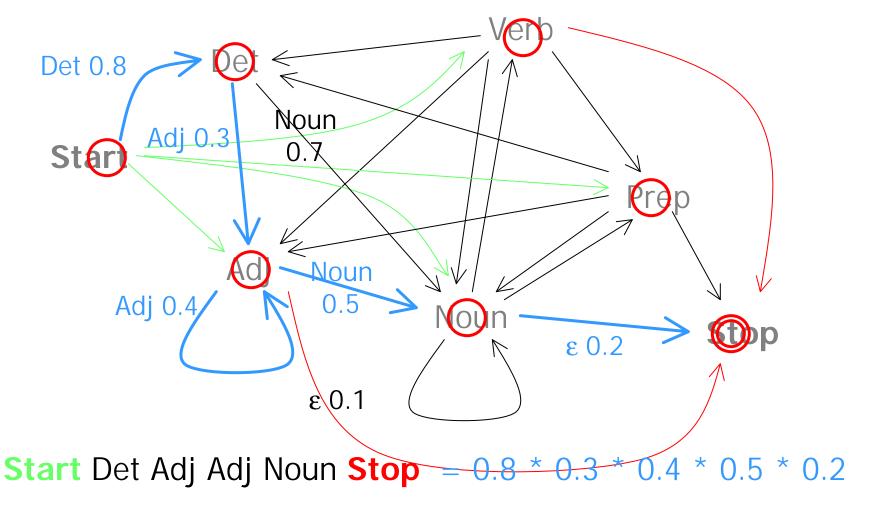
**Start** Det Adj Adj Noun **Stop** = 0.8 \* 0.3 \* 0.4 \* 0.5 \* 0.2

## Markov model as fsa p(tag seq)



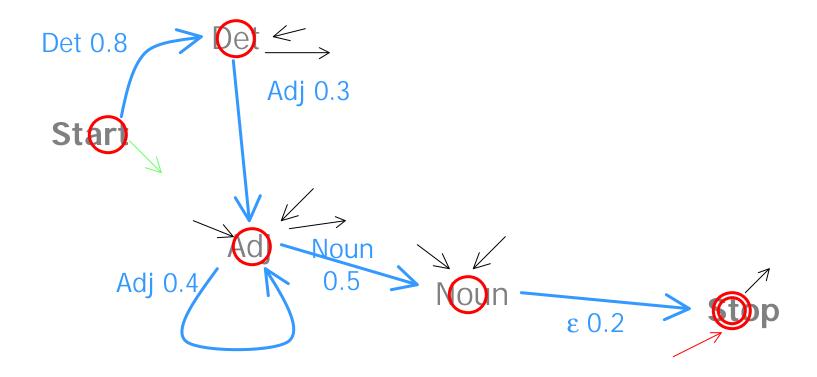
**Start** Det Adj Adj Noun **Stop** = 0.8 \* 0.3 \* 0.4 \* 0.5 \* 0.2

## Add 'output tags' (transducer) p(tag seq)



### Tag bigram picture

p(tag seq)

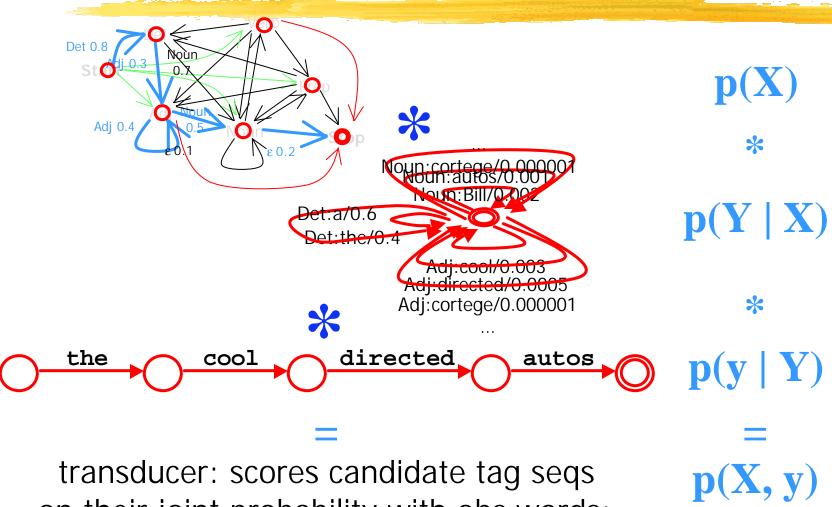


#### Our plan

automaton: p(tag sequence) "Markov Model"  $\mathbf{p}(\mathbf{Y} \mid \mathbf{X})$ transducer: tags → words "Unigram Replacement" automaton: the observed words  $\mathbf{p}(\mathbf{y} \mid \mathbf{Y})$ "straight line" transducer: scores candidate tag seqs p(X, y)on their joint probability with obs words;

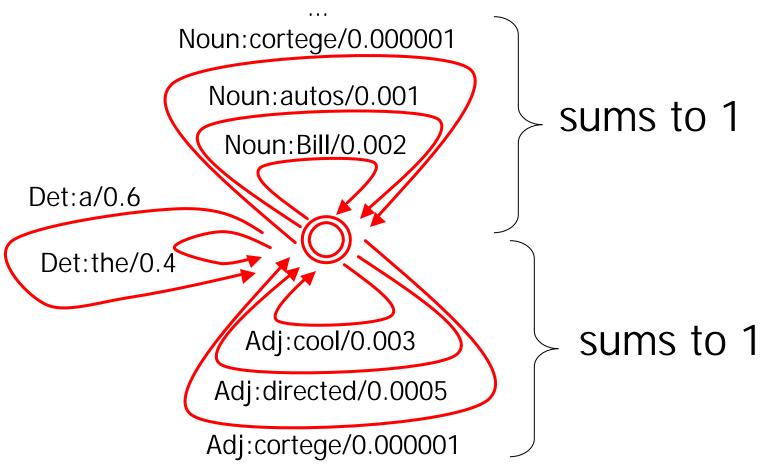
pick best path

#### Cartoon form again



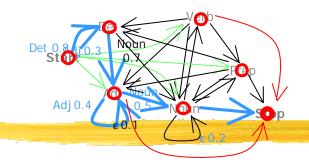
on their joint probability with obs words; we should pick best path

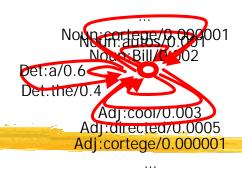
Next up: unigram replacement model p(word seq | tag seq)



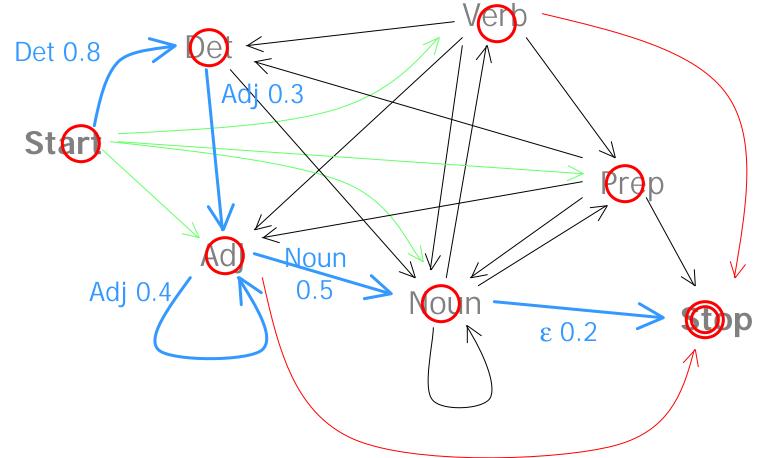
. . .

#### Compose

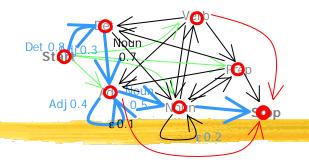


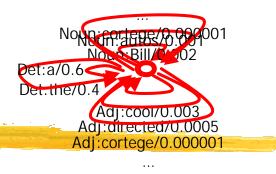


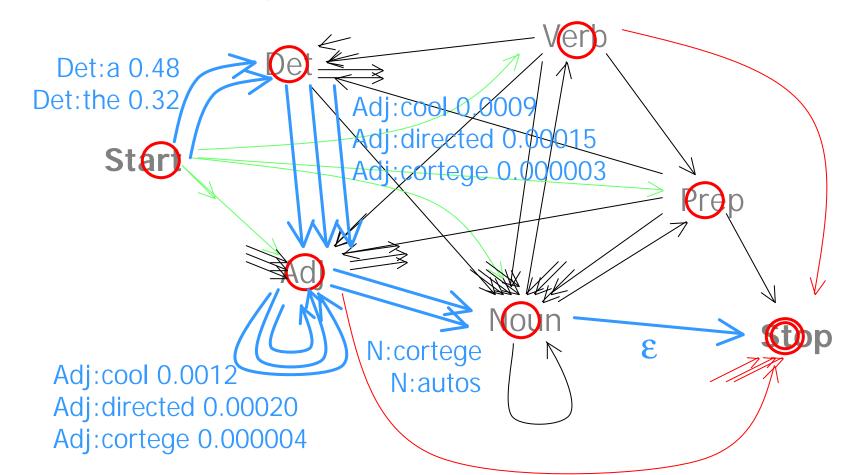
p(tag seq)



#### Compose







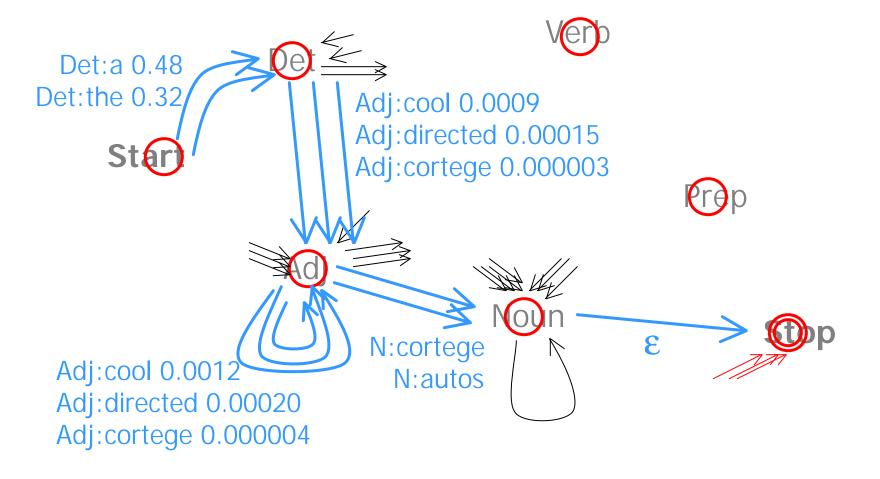
### Observed words as straight-line fsa

word seq



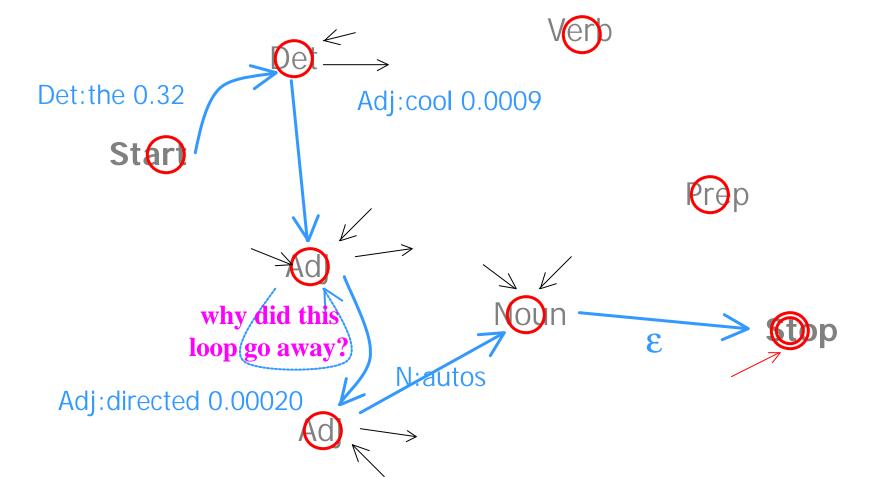
#### Compose with Othe





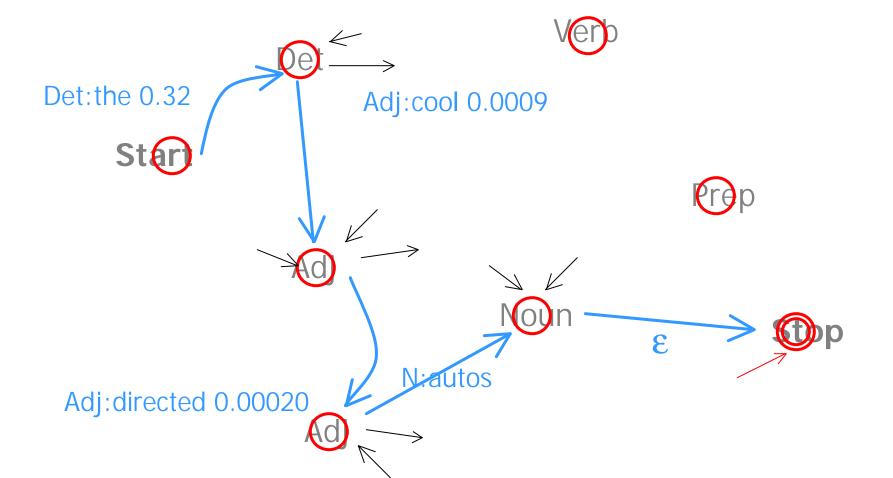
### Compose with





#### The best path:

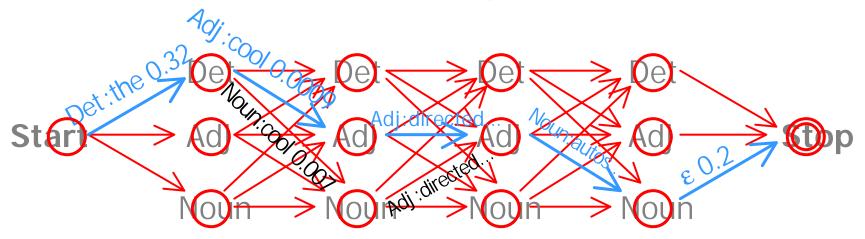
Start Det Adj Adj Noun Stop = 0.32 \* 0.0009\*0.00020... the cool directed autos



But...how do we find this 'best' path???

#### All paths together form 'trellis'

#### p(word seq, tag seq)

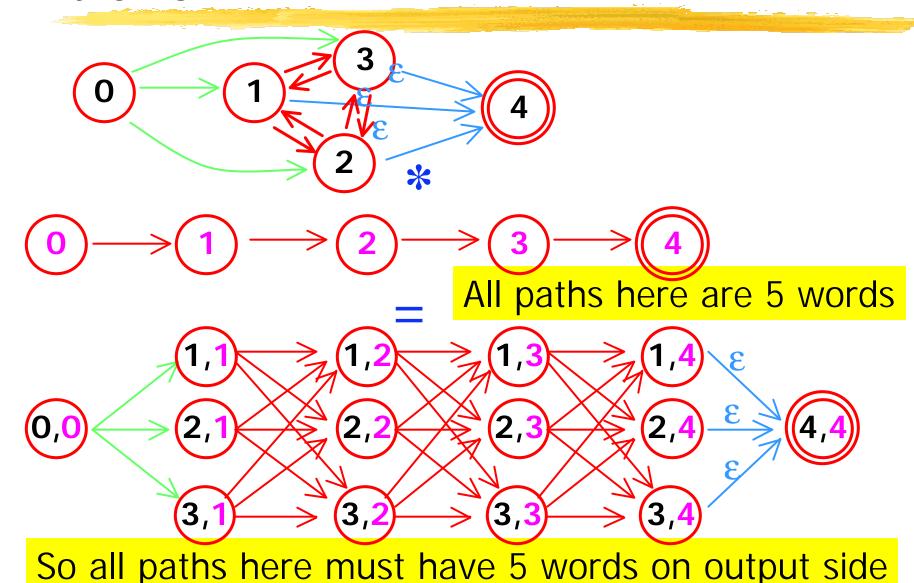


WHY?

#### The best path:

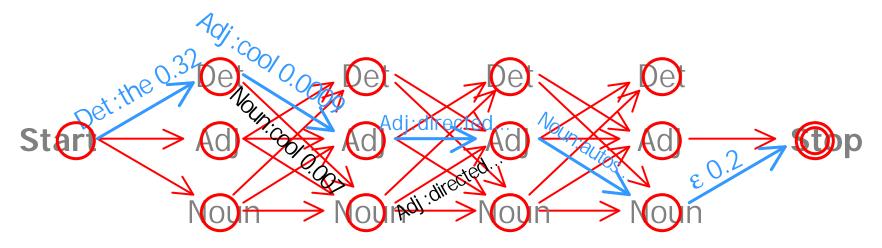
Start Det Adj Adj Noun Stop = 0.32 \* 0.0009 ... the cool directed autos

# Cross-product construction forms trellis



## Trellis isn't complete p(word seq, tag seq)

Lattice has no Det → Det or Det →Stop arcs; why?



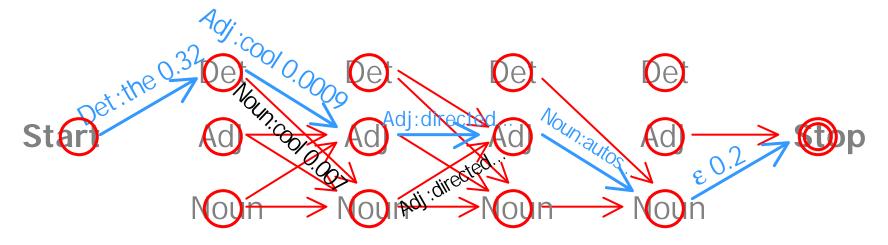
#### The best path:

```
Start Det Adj Adj Noun Stop = 0.32 * 0.0009 ... the cool directed autos
```

#### Trellis incomplete

p(word seq, tag seq)

Lattice is missing some other arcs; why?



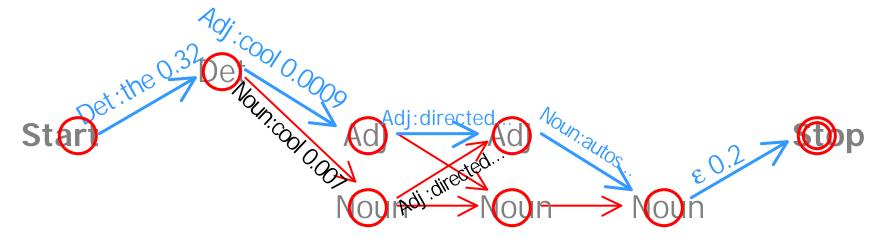
#### The best path:

```
Start Det Adj Adj Noun Stop = 0.32 * 0.0009 ... the cool directed autos
```

### And missing some states...

p(word seq, tag seq)

Lattice is missing some states; why?



#### The best path:

```
Start Det Adj Adj Noun Stop = 0.32 * 0.0009 ... the cool directed autos
```

Finding the best path from start to stop



- Use dynamic programming
- What is best path from Start to <u>each</u> node?
  - Work from left to right
  - Each node stores its best path from Start (as probability plus one backpointer)
- Special acyclic case of Dijkstra's shortest-path algorithm
- Faster if some arcs/states are absent

#### Method: Viterbi algorithm

- For <u>each</u> path reaching state s at step (word)
  t, we compute a path probability. We call the
  max of these <u>viterbi(s,t)</u>
- [Base step] Compute viterbi(0,0)=1
- [Induction step] Compute viterbi(s',t+1), assuming we know viterbi(s,t) for all s: path-prob(s'|s,t) = viterbi(s,t) \* a[s,s']

```
probability of path to \max path score * transition p s' through s for state s at time t s \rightarrow s'
```

```
viterbi(s',t+1) = \max_{s \text{ in STATES}} \text{ path-prob(s' | s,t)}
```

#### Method...

- This is almost correct...but again, we need to factor in the unigram prob of a state s' given an observed surface word w
- So the correct formula for the path probis:

```
path-prob(s'|s,t) = viterbi(s,t) * a[s,s'] * b_{s'}(o_t)
bigram unigram
```

### Or as in your text...p. 179

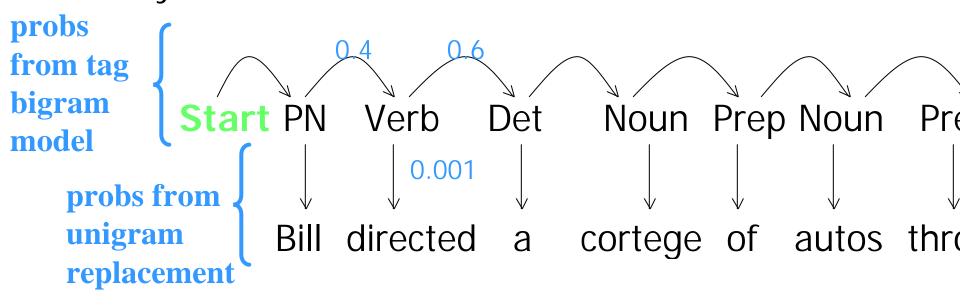
**function** VITERBI(observations of len T, state-graph) **returns** best-path

```
num-states \leftarrow NUM-OF-STATES(state-graph)
Create a path probability matrix viterbi[num-states+2,T+2]
viterbi[0,0] \leftarrow 1.0
for each time step t from 0 to T do
  for each state s from 0 to num-states do
     for each transition s' from s specified by state-graph
        new-score \leftarrow viterbi[s, t] * a[s,s'] * b_{s'}(o_t)
        if ((viterbi[s',t+1]=0) || (new-score > viterbi[s',t+1]))
           then
                   viterbi[s', t+1] \leftarrow new-score
                  back-pointer[s', t+1] \leftarrow s
```

Backtrace from highest probability state in the final column of *viterbi[]* and return path

#### Summary

- We are modeling p(word seq, tag seq)
- The tags are hidden, but we see the words
- Is tag sequence X likely with these words?
- Noisy channel model is a "Hidden Markov Model":



Find X that maximizes probability product

### Two finite-state approaches

Noisy Channel Model (statistical)

2. Deterministic baseline tagger composed with a cascade of fixup transducers

 PS: how do we evaluate taggers? (and such statistical models generally?)