6.863J Natural Language Processing Lecture 7: parsing with hierarchical structures – context-free parsing

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The Menu Bar

- Administrivia:
 - Schedule alert: Lab2 due Weds; Lab 3 out Monday (chunk parsing to 'real' parsing)
 - · Lab time today, tomorrow
 - Please read notes3.pdf, englishgrammar.pdf (on web)
- Agenda:
- Marxist analysis simple & post-modern
- What: hierarchical representations; constituents, representation
- <u>How:</u> constituent or 'context-free' parsing (next time – how to do it *fast*)
- Why: to extract 'meaning'

Motivation

- What, How, and Why
- What: word chunks behave as units, like words or endings (morphemes), like ing
- How: we have to recover these from input
- Why: chunks used to discover meaning
- Parsing: mapping from strings to structured representation

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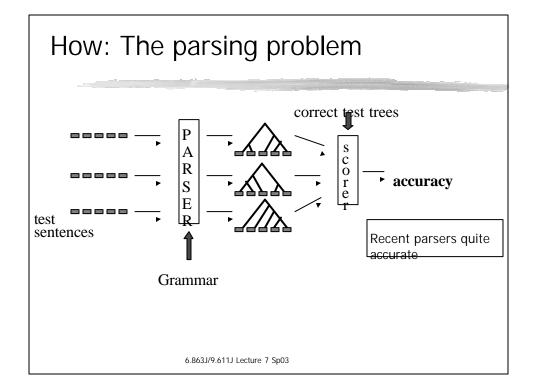
Programming languages

Designed that way!

Natural languages

printf "/charset %s", re_opcode_t *p - 1 == charset_not ? "^" : ""; assert p + *p < pend; for c = 0; c < 256; c++ if c / 8 < *p && p1 + c/8 & 1 << c % 8 Are we starting a range? if last + 1 == c && ! inrange putchar '-'; inrange = 1; Have we broken a range? else if last + 1 != c && inrange putchar last; inrange = 0; if ! inrange putchar c; last = c;

- No {} () [] to indicate scope & precedence
- Lots of overloading (arity varies)
- Grammar isn't known in advance!
- Context-free grammar not best formalism



Syntactic Parsing

- Declarative formalisms like CFGs define the legal strings of a language but don't specify how to recognize or assign structure to them
- Parsing algorithms specify how to recognize the strings of a language and assign each string one or more syntactic structures
- Parse trees useful for grammar checking, semantic analysis, MT, QA, information extraction, speech recognition...and almost every task in NLP

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Applications of parsing (1/2)

■ Machine translation (Alshawi 1996, Wu 1997, ...)

English Chinese

- Speech synthesis from parses (Prevost 1996)
 The government plans to raise income tax.
 The government plans to raise income tax the imagination.
- Speech recognition using parsing (Chelba et al 1998)
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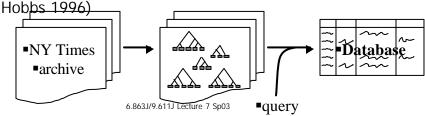
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Applications of parsing

- Grammar checking (Microsoft)
- Indexing for information retrieval (Woods 72-1997)

... washing a car with a hose ... vehicle maintenance

■ Information extraction (Keyser, Chomsky '62 to

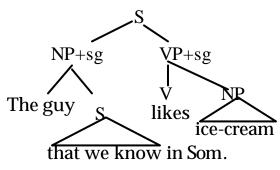


Why: Q&A systems (lab 4)

```
(top-level)
Shall I clear the database? (y or n) y
>John saw Mary in the park
OK.
>Where did John see Mary
IN THE PARK.
>John gave Fido to Mary
OK.
>Who gave John Fido
I DON'T KNOW
>Who gave Mary Fido
JOHN
>John saw Fido
OK.
>Who did John see
FIDO AND MARY
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```

Why: express 'long distance' relationships via adjacency

- The guy that we know in Somerville likes ice-cream
- Who did the guy who lives in Somerville see ___?



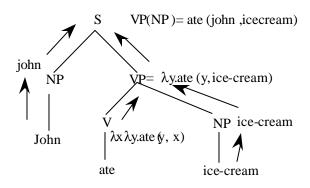
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Why: recover meaning from structure

John ate ice-cream \rightarrow ate(John, ice-cream)

- -This must be done from structure
- -Actually want something like $\lambda x \lambda y$ ate(x,y) How?

Why: recover meaning from structure



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Why: Parsing for the Turing Test

- Most linguistic properties are defined over hierarchical structure
- One needs to parse to see subtle distinctions

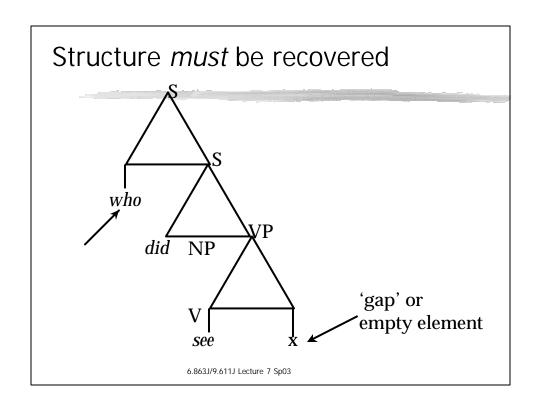
Sara likes her. (her ¹ Sara)

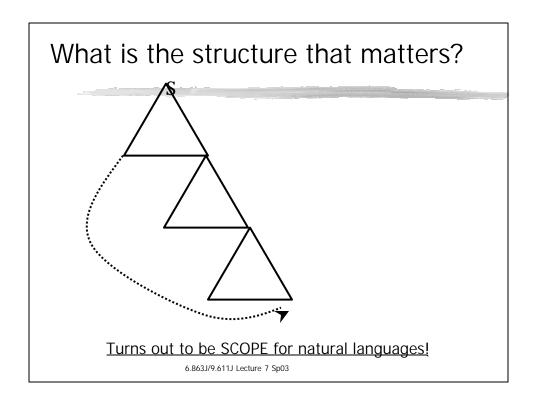
Sara thinks that someone likes her. $(her = or \ ^1 Sara)$

Sara dislikes anyone's criticism of her. $(her = Sara \text{ or } her \text{ }^1 Sara)$

Who did John see? \rightarrow For which x, x a person, likes(Bill, x)

Distinction here is based on *hierarchical structure* = <u>scope</u> in natural language

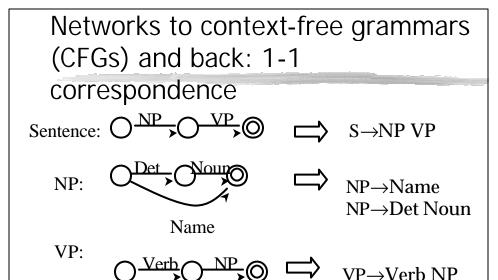




The elements

- What: hierarchical representations
 (anything with recursion) using phrases
 AKA "constituents"
- 2. How: context-free parsing (plus...)
- 3. Why: (meaning)

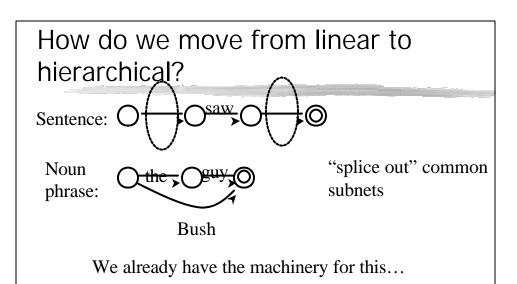
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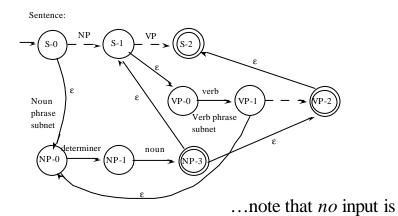
+ terminal expansion rules

Added information

- FSA represents pure *linear* relation: what can *precede* or (*follow*) what
- CFG/RTN adds a new predicate: dominate
- Claim: The dominance and precedence relations amongst the words exhaustively describe its syntactic structure
- When we parse, we are recovering these predicates



Use of epsilon transitions ('jump' arcs) – they consume <u>no</u> input



consumed during jump

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This will work... with one catch

- Consider tracing through "the guy ate the ice-cream"
- What happens when we get to the second noun phrase????
- Where do we return to?
- Epsilon transition takes us back to different points

What: Context-free grammars (CFG)

S(entence)→NP VP VP→V NP NP→Det N

 $N \to pizza, N \to guy, Det \to the$ } pre-terminals, lexical entries

 $V \rightarrow ate$

A context-free grammar (CFG):

Sets of <u>terminals</u> (either lexical items or parts of speech) Sets of <u>nonterminals</u> (the constituents of the language) Sets of <u>rules</u> of the form $A \rightarrow \alpha$ where α is a string of zero or more terminals and nonterminals

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Derivation by a context-free grammar:rewrite line by line

generation

1. <u>S</u>

2. NP \underline{VP} (via S \rightarrow NP VP)

3. NP V \underline{NP} (via VP \rightarrow V NP)

4. NP V Det \underline{N} (via NP \rightarrow Det N)

5. NP V $\underline{\text{Det}}$ pizza (via N \rightarrow pizza)

6. NP \underline{V} the pizza (via Det \rightarrow the)

7. NP ate the pizza (via $V \rightarrow ate$)

8. Det \underline{N} ate the pizza (via NP \rightarrow Det N)

9. Det guy ate the pizza (via $N \rightarrow guy$)

10. the guy ate the pizza (via Det \rightarrow the)

Context-free representation

- Is this representation adequate Not really...why?
- We'll start here, though & illustrate parsing methods – how to make parsing efficient (in length of sentence, size of grammar)
- Obvious methods are exponential; we want polynomial time (or, even linear time, or, even, real time...)
- Challenges: recursion, ambiguity, nondeterminism

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How: context-free parsing

- Parsing: assigning a correct hierarchical structure (or its derivation) to a string, given some grammar
 - The leaves of the hierarchical structure cover all and only the input;
 - The hierarchical structure ('tree') corresponds to a valid derivation wrt the grammar
- Note: 'correct' here means consistent w/ the input & grammar – NOT the "right" tree or "proper" way to represent (English) in any more global sense

Parsing

- What kinds of constraints can be used to connect the grammar and the example sentence when searching for the parse tree?
- Top-down (goal-directed) strategy
 - Tree should have one rot (grammar constraint)
- Bottom-up (data-driven) strategy
 - Tree should have, e.g., 3 leaves (input sentence constraint)

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The input

- For now, assume:
 - Input is not tagged (we can do this...)
 - The input consists of unanalyzed word tokens
 - All the words are known
 - All the words in the input are available simultaneously (ie, buffered)

How do we do this?

- Searching FSAs
 - Finding the right path through the automaton
 - · Search space defined by structure of FSA
- Searching CFGs
 - Finding the right parse tree among all possible parse trees
 - Search space defined by the grammar
- Constraints provided by the input sentence and the automaton or grammar

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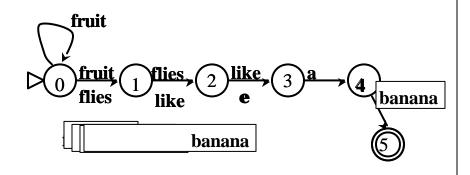
Marxist analysis: simple version

- Suppose just linear relations to recover
- Still can be ambiguity multiple paths
- · Consider:



Fruit flies like a banana

FSA, or linear Example



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State-set parsing for fsa

Compute initial state set, So Initialize:

1.
$$S_0 \leftarrow q_0$$

2.
$$S_0 \leftarrow \epsilon$$
-closure(S_0)

Loop:

Compute S_i from S_{i-1}

- 1. For each word w_i , i=1,2,...,n
- 2. $S_i \leftarrow \bigcup_{q \in S_{i-1}} \mathbf{d}(q, w_i)$ 3. $S_i \leftarrow \epsilon$ -closure(S_i)
- 4. if $S_i = \emptyset$ then halt & reject else continue

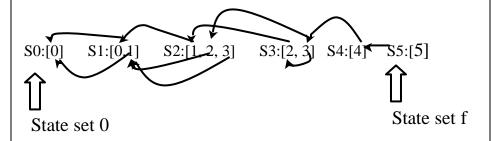
Final:

Accept/reject

1. If $q_f \in S_n$ then accept else reject

States in sequence dictate parse path:

States: $\{0\} \rightarrow \{0,1\} \rightarrow \{1,2,3\} \rightarrow \{2,3\} \rightarrow \{4\} \rightarrow \{5\}$ (final)



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State to state jumps...

- Progress (& ultimately parse) recorded by what state machine is in
- · Consider each transition as rule:

 $q_0 \rightarrow fruit \; q_1$, also loop: $q_0 \rightarrow fruit \; q_0$

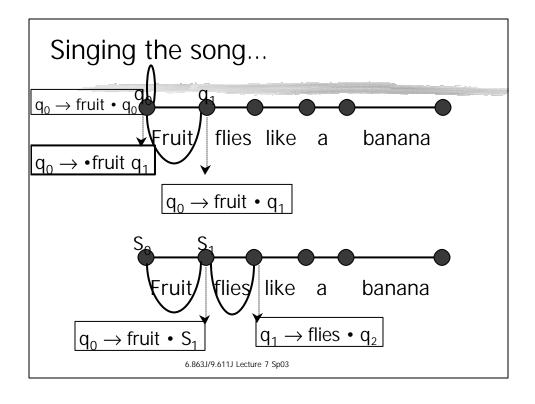
 $q_1 \rightarrow flies q_2$

 $q_2 \rightarrow$ like q_3 also epsilon transition: $q_2 \rightarrow q_3$

 $q_{\scriptscriptstyle 3} \to a \; q_{\scriptscriptstyle 4}$

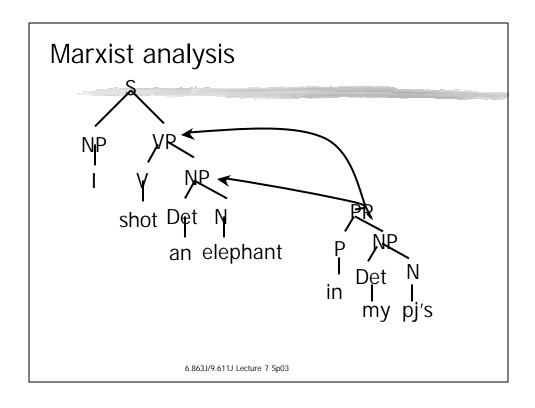
 $q_4 \rightarrow banana q_5$

 We can record progress path via 'bouncing ball' telling us how to sing the song...



But now we have a more complex Marxist analysis

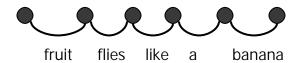
- I shot an elephant in my pajamas
- This is hierarchically ambiguous not just linear! (each possible hierarchical structure corresponds to a distinct meaning)



How can we extend this bouncing ball?

- Can't just be linear...
- How do we pack these possibilities together?
- We will augment... let's see how

From this...



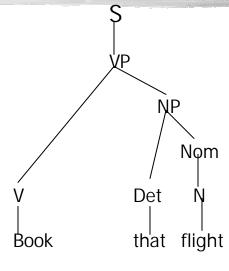
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Three senses of rules

- generation (production): $S \rightarrow NP VP$
- parsing (comprehension): $S \leftarrow NP VP$
- verification (checking): S = NP VP
- CFGs are <u>declarative</u> tell us what the well-formed structures & strings are
- Parsers are <u>procedural</u> tell us *how* to compute the structure(s) for a given string

S → NP VP	VP → V
S → Aux NP VP	Det → that this a
S → VP	N → book flight meal money
NP → Det Nom	V → book include prefer
NP → PropN	Aux → does
Nom → N Nom	Prep →from to on
Nom → N	PropN → Boston United
Nom → Nom PP	
VP → V NP 6.863J/9.611J Lec	ture 7 Sp03

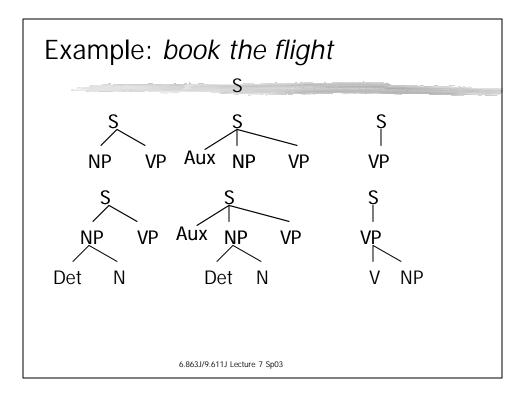
Parse Tree for 'Book that flight'



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Strategy 1: Top-down parsing

- Goal or expectation driven find tree rooted at S that derives input
- Trees built from root to leaves
- Assuming we build all trees in parallel:
 - Find all trees with root S (or all rules w/lhs S)
 - Next expand all constituents in these trees/rules
 - Continue until leaves are parts of speech (pos)
 - Candidate trees failing to match pos of input string are rejected (e.g. Book that flight can only match subtree 5)



Top-down strategy

- Depth-first search:
 - Agenda of search states: expand search space <u>incrementally</u>, exploring most recently generated state (tree) each time
 - When you reach a state (tree) inconsistent with input, backtrack to most recent unexplored state (tree)
- Which node to expand?
 - Leftmost or rightmost
- Which grammar rule to use?
 - · Order in the grammar

Top-down, left-to-right, depth-first

- Initialize agenda with 'S' tree and ptr to first word and make this current search state (cur)
- Loop until successful parse or empty agenda
 - Apply all applicable grammar rules to leftmost unexpanded node of cur
 - If this node is a POS category and matches that of the current input, push this onto agenda
 - · O.w. push new trees onto agenda
 - · Pop new cur from agenda
- Does this flight include a meal?

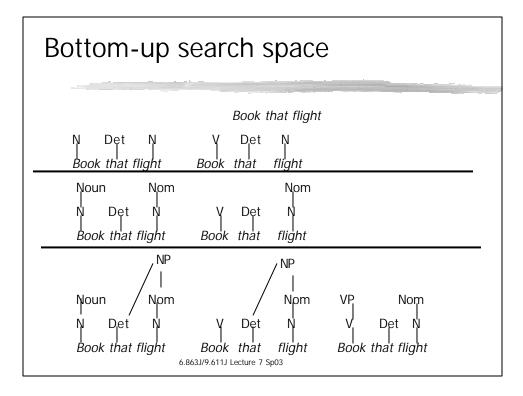
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Strategy 2: Bottom-up

- Parser begins with words of input and builds up trees, applying grammar rules w/rhs that match
 - · Book that flight

N Det N V Det N Book that flight Book that flight

- 'Book' ambiguous
- Parse continues until an S root node reached or no further node expansion possible



Comparing t-d vs. b-u

- <u>Top-Down parsers</u> never explore illegal parses (e.g. can't form an S) -- but waste time on trees that can never match the input
- <u>Bottom-Up parsers</u> never explore trees inconsistent with input -- but waste time exploring illegal parses (no S root)
- For both: how to explore the search space?
 - Pursuing all parses in parallel or ...?
 - · Which rule to apply next?
 - · Which node to expand next?

Problems...

- Left-recursion
- Ambiguity: multiple parses
- Principle AWP

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Left-recursion

- Rules of form: $X \rightarrow X \alpha$
- Example: \bigwedge NP \rightarrow NP 's NP | Name

John's brother's book
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Structural ambiguity

- Multiple legal structures
 - Attachment (e.g. I saw a man on a hill with a telescope)
 - Coordination (e.g. younger cats and dogs)
 - NP bracketing (e.g. Spanish language teachers)

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How to fix?

- Principle AWP! Dynamic programming...
- Create table of solutions to sub-problems (e.g. subtrees) as parse proceeds
- Look up subtrees for each constituent rather than re-parsing
- Since all parses implicitly stored, all available for later disambiguation
- Examples: Cocke-Younger-Kasami (CYK) (1960), Graham-Harrison-Ruzzo (GHR) (1980) and Earley (1970) algorithms

General method: Chart Parsing

- Note: parses share common constituents
- Build <u>chart</u> = graph data structure for storing partial & complete parses (AKA <u>well-formed</u> <u>substring table</u>)
- Graph:
 - · Vertices: used to delimit subsequences of the input
 - Edges (active, inactive)
 - Active = denote incompletely parsed (or found) phrase
 - Inactive = completely found phrase
 - Labels = name of phrase
- Note: chart *sufficient* to attain polynomial time parsability = $O(n^3 |G|)$, |G| = 'size' of grammar, no matter what strategy we use

How do we build the chart?

- Idea: as parts of the input are successfully parsed, they are entered into chart
- Like memoization
- Can use any combo strategy of t-d, b-u, or in between to build the edges
- Annotate edges as they are built w/ the corresponding dotted rule
- Parser is a combination of chart + strategy

Chart parsing

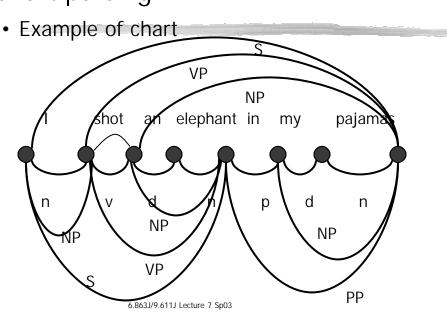


Chart parsing

- Think of chart entries as sitting between words in the input string keeping track of states of the parse at these positions
- For each word position, chart contains the set of states representing all partial parse trees generated to date

Chart parsing

- Chart entries represent three type of constituents (phrases):
 - · predicted constituents
 - in-progress constituents
 - completed constituents

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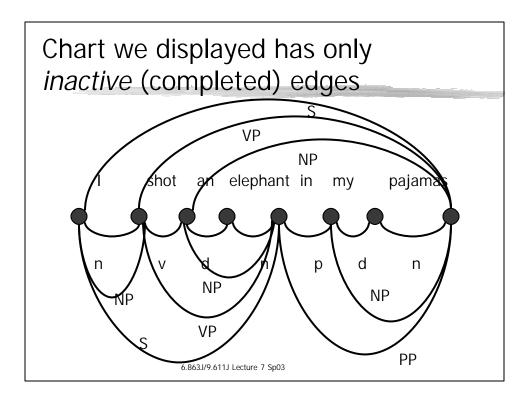
Representing complete (inactive) vs. incomplete (active) edges

- · Complete: full phrase found, e.g., NP, VP
- So: corresponding rule something like
 - NP→NP PP ("an elephant in my pajamas")
 - $S \rightarrow NP VP$ ("I saw an elephant")
 - NP → Det N ("an elephant")
- Representation: use "dot" in rule to denote progress in discovering LHS of the rule:

 $NP \rightarrow \bullet$ Det NP = I've just started to find an NP ("predict")

 $NP \rightarrow Det \cdot NP = Found a Det in input, now find NP$

 $NP \rightarrow Det NP \bullet = Completed phrase (dot at end)$



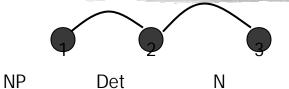
Complete (Inactive) vs. Inprogress (active) edges

- Completed edges correspond to "having found a phrase" so really should be labeled with info like NP \rightarrow Det NP •
- We should go back & annotate our chart like this
- These edges are "inactive" because there is no more processing to be done to them
- Incomplete or "active" edges: work in progress,
 i.e., NP→• Det NP or NP → Det NP
- We build up the chart by extending active edges, gluing them together – let's see how

Note correspondence between "dotted rules" & states in corresponding fsa - isomorphic

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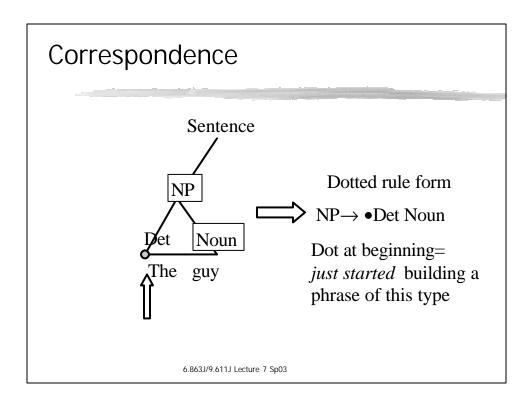
Dotted rule – fsa correspondence

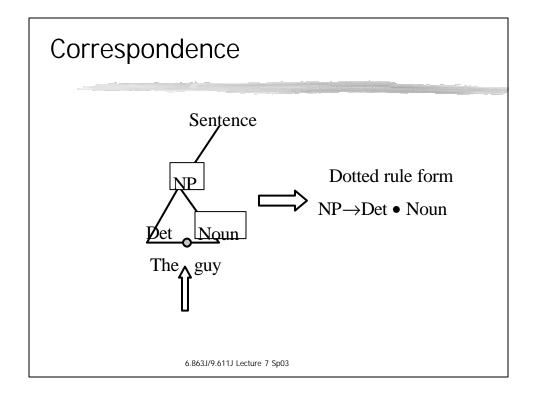


 $NP \rightarrow \bullet Det N = being in State 1$

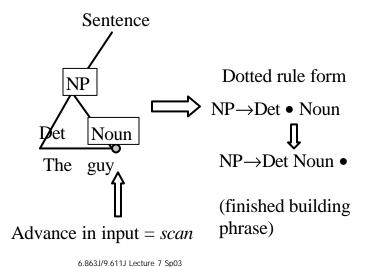
 $NP \rightarrow Det \cdot N = being in State 2$

 $NP \rightarrow Det N \cdot = being in State 3$





Correspondence



Representing the edges

- O Book 1 that 2 flight 3
 S → VP, [0,0] (predicting VP)
 NP → Det Nom, [1,2] (finding NP)
 VP → V NP •, [0,3] (found VP)
- [x,y] tells us where a phrase begins (x) and where the dot lies (y) wrt the input – how much of the phrase is built so far
- So, a FULL description of a chart edge is:
 Edge Label, [start node, current progress dot pos]

 e.g.,

 $NP \rightarrow Det \cdot Nom, [1,2]$

Set of dotted rules encodes state of parse

- = all states parser could be in after processing *i* tokens
- We now have almost all the ingredients...

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FSA, or linear Example fruit flies like e banana 6.863J/9.611J Lecture 7 Sp03

State-set parsing for fsa

Initialize: Compute initial state set, S₀

1. $S_0 \leftarrow q_0$

2. $S_0 \leftarrow \varepsilon$ -closure(S_0)

Loop: Compute S_i from S_{i-1}

1. For each word w_i , i=1,2,...,n

2. $S_i \leftarrow \bigcup_{q \in S_{i-1}} \boldsymbol{d}(q, w_i)$

3. $S_i \leftarrow \epsilon$ -closure(S_i)

4. if $S_i = \emptyset$ then halt & reject else continue

Final: Accept/reject

1. If $q_f \in S_n$ then accept else reject 6.863J/9.611J Lecture 7 Sp03

Use backpointers to keep track of the different paths (parses):

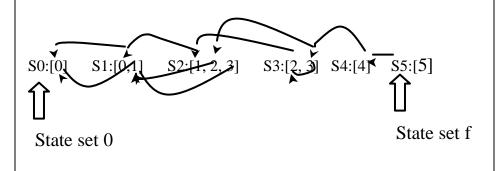


Chart parsing is the same, except...

- Notion of 'state set' is just more complicated – not just the state #, but also the # of the state we started building the phrase at = the return ptr
- Note this is what the chart graph structure encodes

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State set = chart after i words

• Given grammar G, input string $w=w_1 w_2 \dots w_n$

Note: we mark interword positions $_0w_1$ w_2 ... w_n

- <u>Initialize</u>: write down what can be in "start state set" S_0
- Loop: for each word w_i , compute S_i from S_{i-1}
- Final: see if final state is in last state set S_n

FTN Parser

Compute initial state set \$\sqrt{s}\$

1. $S_0 \leftarrow q_0$ 2. $S_0 \leftarrow \text{eta-closure}(S_0)$ $q_0 = [Start \rightarrow S, 0]$ eta-closure= transitive closure of jump arcs

CFG Parser

Compute initial state set \$1

1. $S_0 \leftarrow q_0$

2. $S_0 \leftarrow$ eta-closure (S_0) $q_0 = [Start \rightarrow S, 0, 0]$ eta-closure= transitive closure of Predict and Complete

For each word, w_i , 1=1,...,n

Loop:

Initialize:

Compute Sfrom Si-1 For each word, wi, $\hat{1}=1,...,n$ $S_i \leftarrow \cup \delta(q, w_i)$ $q \in S_{i-1}$

 $= \overset{q \in \bar{S}_{i-1}}{Scan(S_{i-1})}$

g=item $S_i \leftarrow e-closure(S_i)$ e-closure=

Compute S from Si-1

 $Si \leftarrow \cup \delta(q, w_i)$

closure(Predict, Complete)

Final:

Accept/reject: If $q_f \in S_n$ then accept; else reject $q = [Start \rightarrow S^{\bullet}, 0]$

 $S_i \leftarrow e\text{-closure}(S_i)$

Accept/reject:

If $q_f \in S_n$ then accept;

else reject

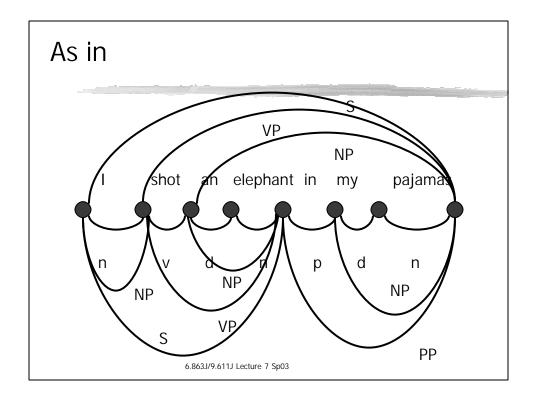
 $q = [Start \rightarrow S^{\bullet}, 0, n]$

Parsing procedure w/ chart

- Move through each set of states in order, applying one of three operators to each state:
 - predictor: add new active edges, predictions, to the chart
 - · scanner: read input and advance dot, add corresponding active edge to chart
 - completer: if dot at the right end of a rule, then see if we can glue two edges together to form a larger one

Note:

- Results (new edges) added to current or next set of states in chart
- No backtracking and no edges removed: keep complete history of parse
- When we get to the end, there ought to be an edge labeled S, extending from 0 to n (n= length of sentence)



Predictor ('wishor')

- Intuition: new states represent top-down expectations
- Applied when non part-of-speech non-terminals are to the right of a dot – until closure

```
S \rightarrow \bullet VP [i,i]
```

- Adds new states to current chart
 - One new state for each expansion of the nonterminal in the grammar

```
VP \rightarrow \bullet V [i,i]

VP \rightarrow \bullet V NP [i,i]
```

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Scanner (as in fsa)

- New states for predicted part of speech
- Applicable when part of speech is to the right of a dot

$$VP \rightarrow \bullet V NP [0,0] 'Book...'$$

- Looks at current word in input
- If match, adds dotted rule edge starting at next point over, e.g.,

$$VP \rightarrow V \cdot NP [0,1]$$

Just as with fsa's – jump to next point

Completer

- Intuition: parser has discovered a complete constituent, so must see if this completed edge can be pasted together with any preceding active edge to make a bigger one...
- E.g., NP[0, 2] & VP[2, 7] yields S[0,7]
- "Glue together" two edges
- Must do this until closure...

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Examples – will use v, v simple G

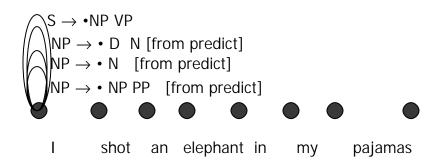
- S \rightarrow NP VP
- $VP \rightarrow V NP$
- $VP \rightarrow VNPPP$
- $NP \rightarrow D N$
- NP \rightarrow N
- NP \rightarrow NP PP
- $PP \rightarrow PNP$

Strategies w/ Chart

- Top-down
- Bottom-up
- Left-corner (what's that??)

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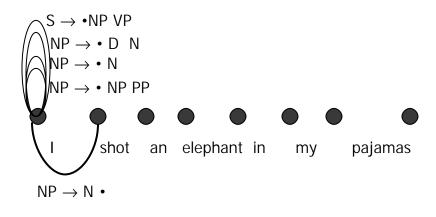
Example: Top-down w/ chart



State set S_0 - nothing more can be added, so scan next word

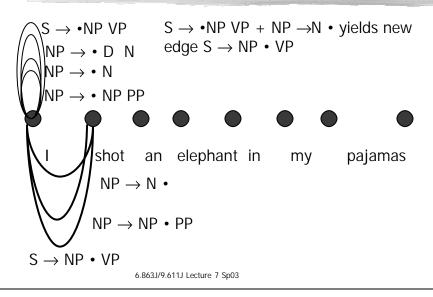
Note how top-down strategy can introduce rules unconnected to the input.. 6.863J/9.611J Lecture 7 Sp03

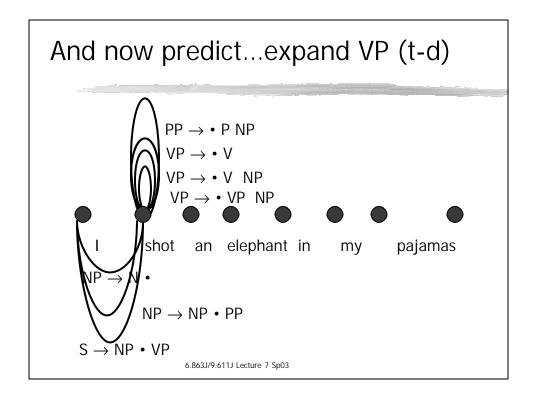
Scan to next word...follow the bouncing dot...

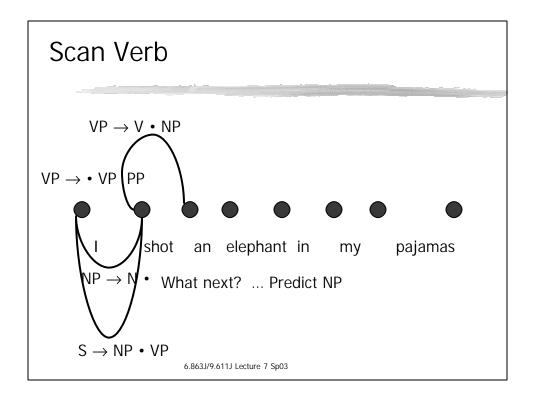


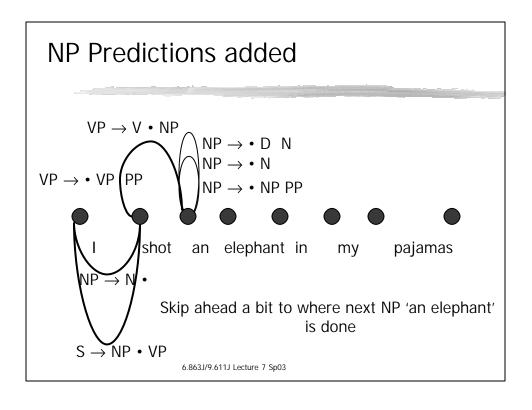
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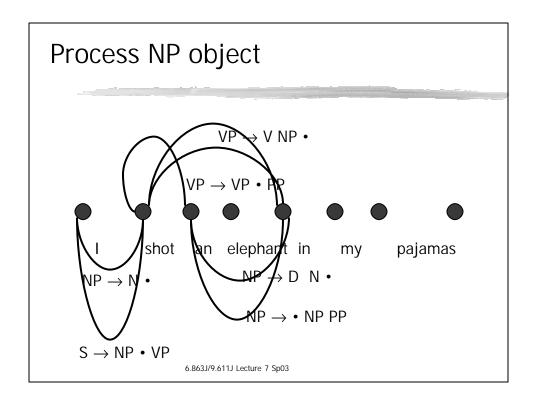
Dot at end...so we 'complete' NP











Enough...no more! Demo easier!