


# 6.863J Natural Language Processing

## Lecture 9: Writing grammars; feature-based grammars



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# The Menu Bar

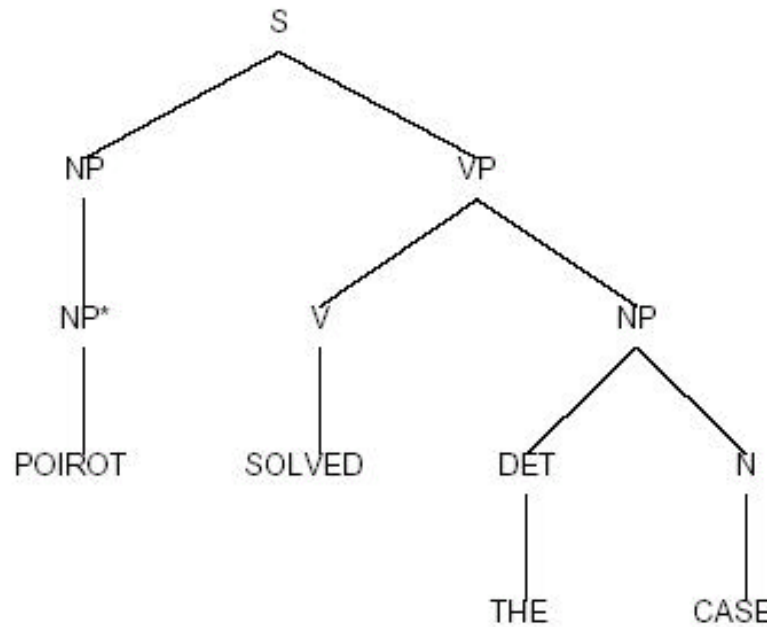
- **Administrivia:**
  - Schedule alert: Lab 3 out; due next Weds.
  - Lab time today, tomorrow
  - Please read notes3.pdf!!  
englishgrammar.pdf (on web)
- *Agenda:*
- Building grammars – basics to complex
- Limits of context-free grammars: the trouble with tribbles
- Foundation for the laboratory

# Grammars for natural languages



- Where do the rules come from?
- Roughly: read them off of parse trees...
- A “rule-based”, construction-based point of view
- Take ‘surface’ phrase patterns (mostly)
- But we still want to map to an *underlying* ‘logical’ form
- How do we start out?

# Reading rules from parse trees...



$S \rightarrow NP \ VP$

$VP \rightarrow V \ NP$

$NP \rightarrow Det \ N$

$NP \rightarrow N^*$

Can't we get a computer to do this?



# Key elements – part 1



- Establish basic phrase types: S, VP, NP, PP, ...
- Where do these come from???

# What *kinds* of phrases are there?



- Noun phrases, verb phrases, adjectival phrases ("green with envy"), adverbial phrases ("quickly up the hill"), prepositional phrases ("off the wall"), etc.
- In general: *grounded* on lexical items
- Shows us the *constraints* on context-free rules for *natural grammars*
- Example:

# Phrase types are constrained by lexical projection

Verb Phrase →

"is-a"

Verb

("kick the ball")

Noun Phrase

Prepositional Phrase →

("on the table")

Preposition

Noun Phrase

Adjective Phrase →

("green with envy")

Adjective

Prep. Phrase

Etc. ... what is the pattern?

# Function-argument relation



$XP \rightarrow X$  arguments, where  $X$  = Noun, Verb,  
Preposition, Adjective (all lexical categories  
in the language)

Like function-argument structure  
(so-called “Xbar theory”)

Constrains what grammar rules *cannot* be:

$\text{Verb Phrase} \rightarrow \text{Noun Noun Phrase}$

or even

$\text{Verb Phrase} \rightarrow \text{Noun Phrase Verb Noun Phrase}$

# English is function-argument form

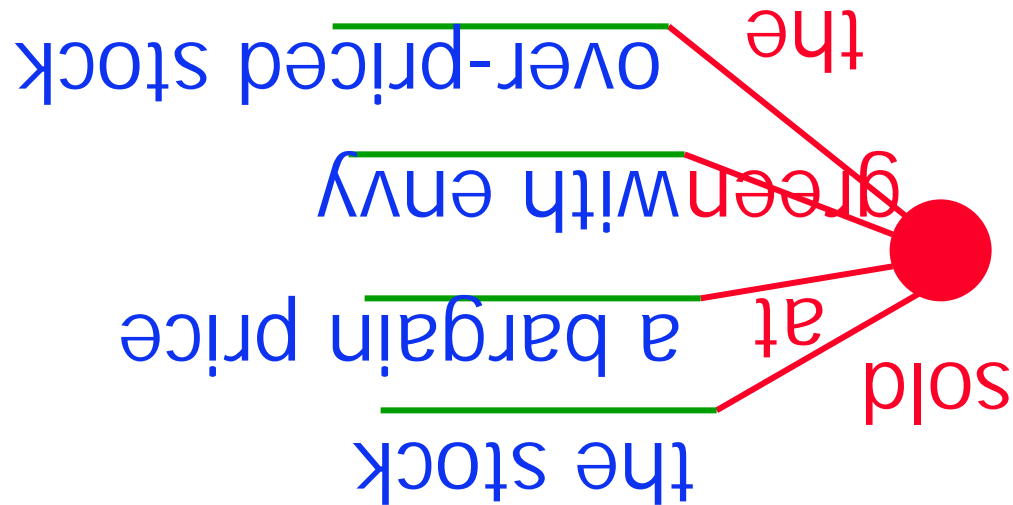
function

args



# Other languages are the mirror-inverse: arg-function

This is like Japanese



# Key elements – part 2



- Establish *verb subcategories*
- What are these?
  - Different verbs take different # arguments
  - 0, 1, 2 arguments ('complements')
  - Poirot thought; Poirot thought the gun; Poirot thought the gun was the cause.
  - Some verbs take certain sentence complements:
  - *I know who John saw/? I think who John saw* propositional types:
  - Embedded questions: *I wonder whether...*
  - Embedded proposition: *I think that John saw Mary*

# Key elements

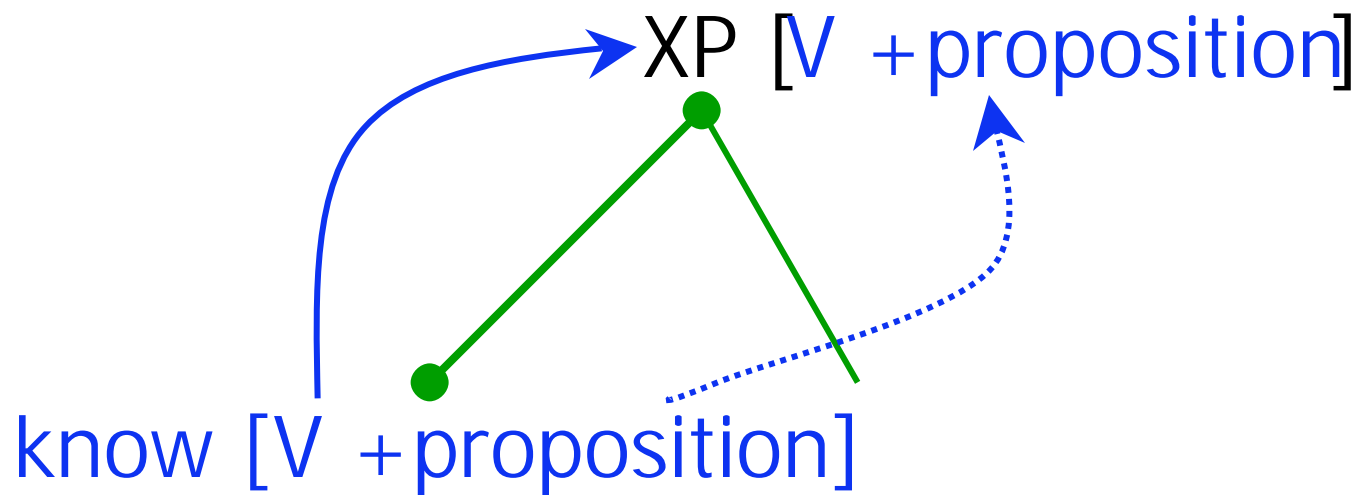


- Subtlety to this
- Believe, know, think, wonder, ...
  - ? I believe why John likes ice-cream
  - I know why John likes ice-cream
  - I believe that John likes ice-cream
  - I believe (that) John likes ice-cream
- # args, type: Verb subcategories
- How many subcategories are there?
- What is the structure?

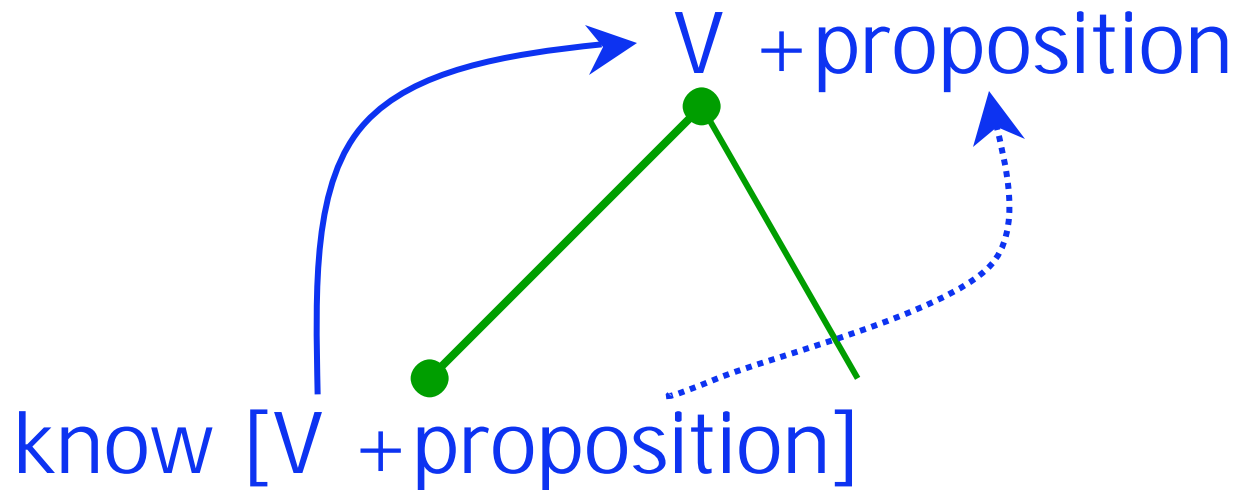


# Idea for phrases

- They are based on 'projections' of words (lexical items) – imagine features 'percolating' up

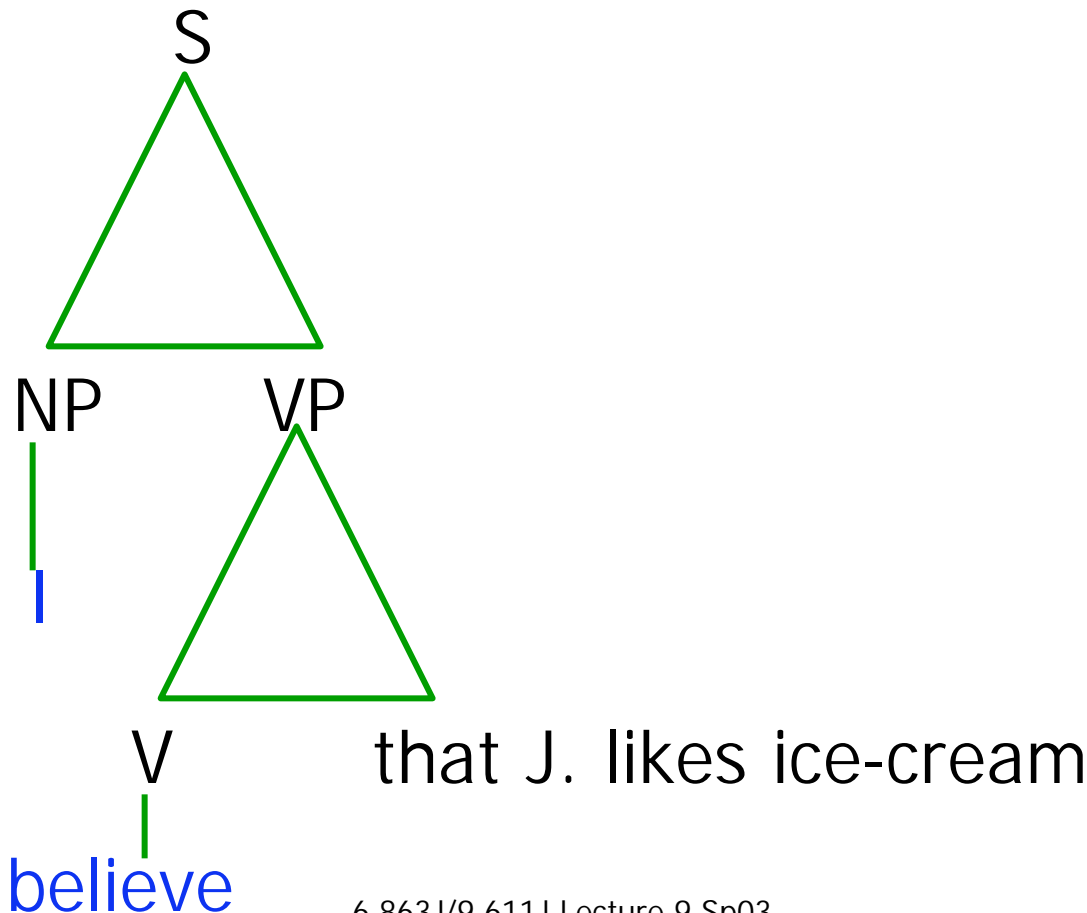


# Heads of phrases

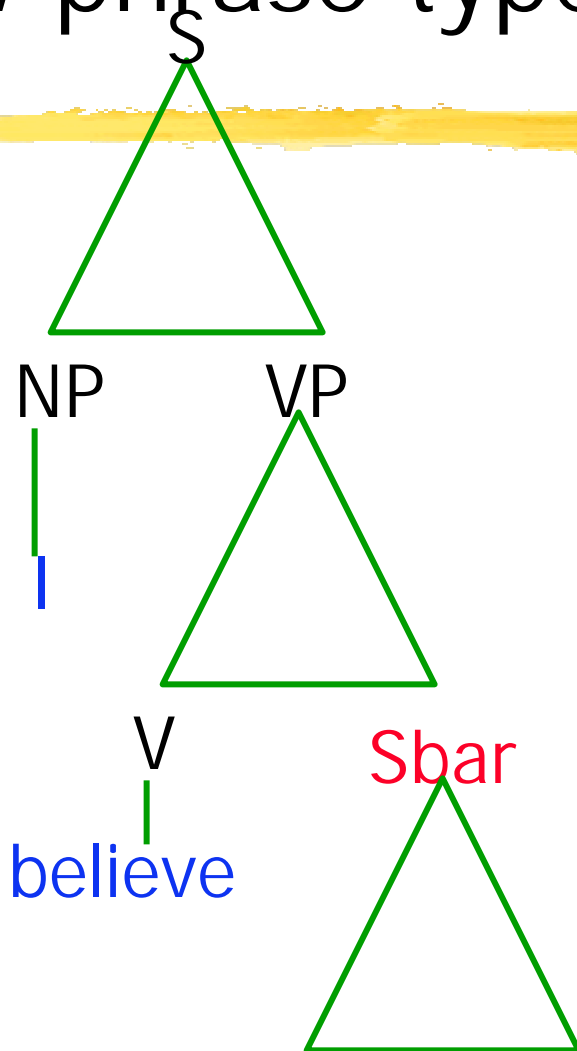


# The parse structure for 'embedded' sentences

I believe (that) John likes ice-cream

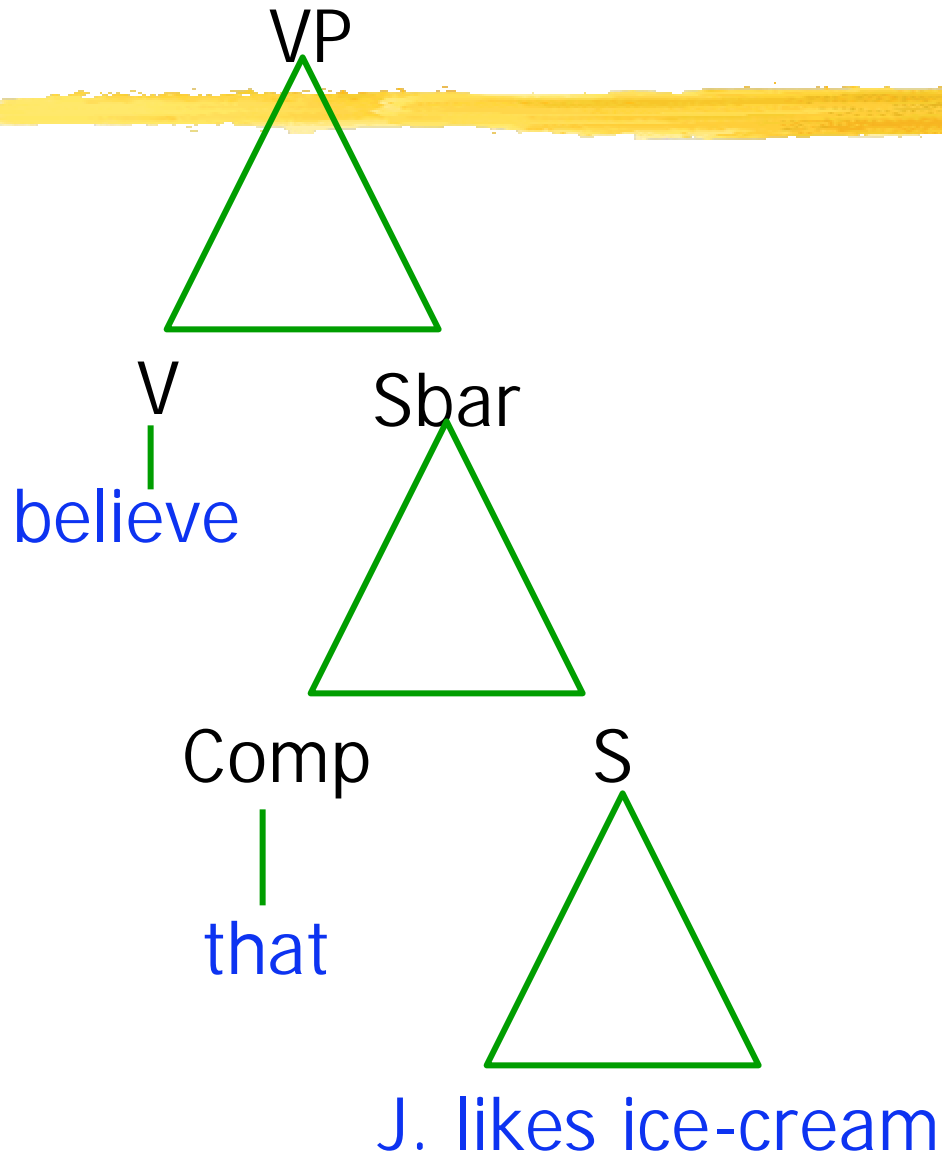


# New phrase type: S-bar

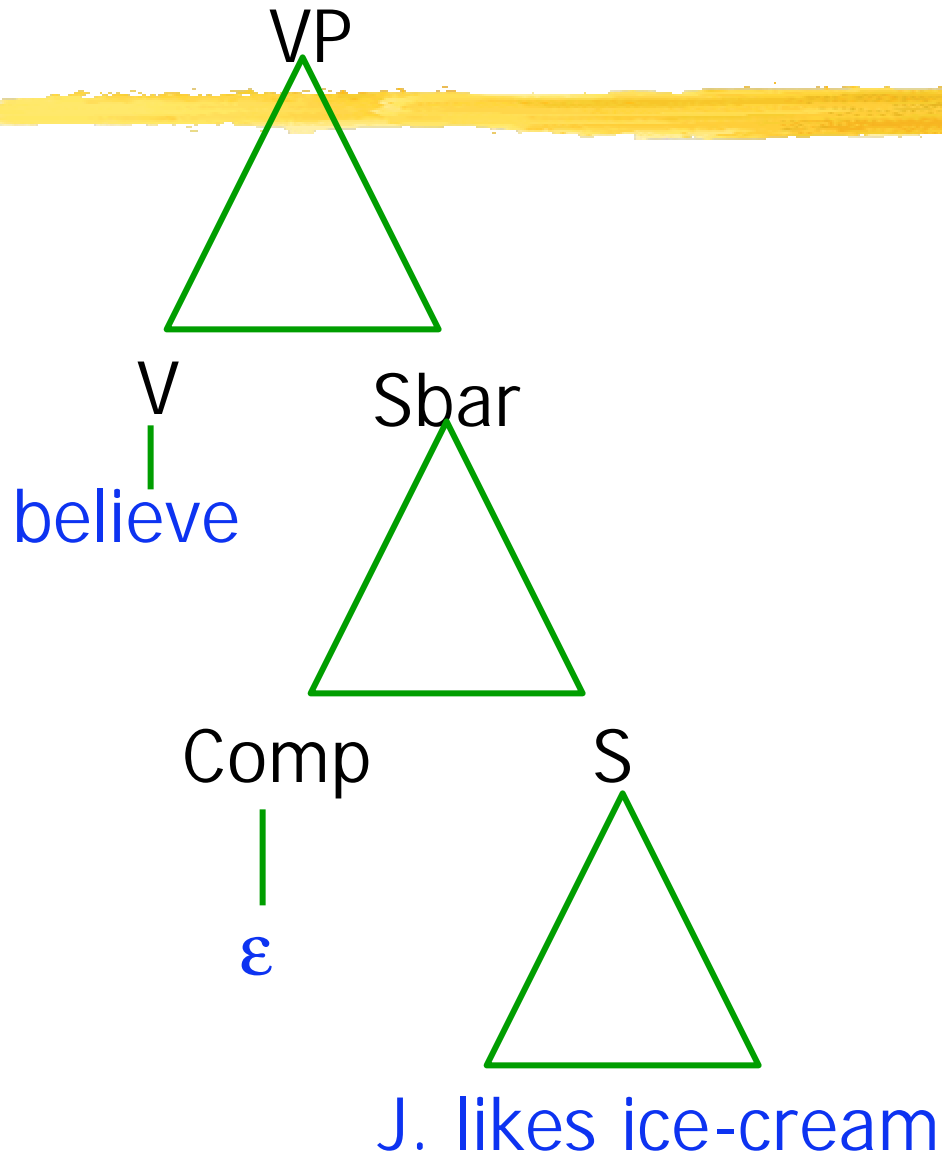


that J. likes ice-cream

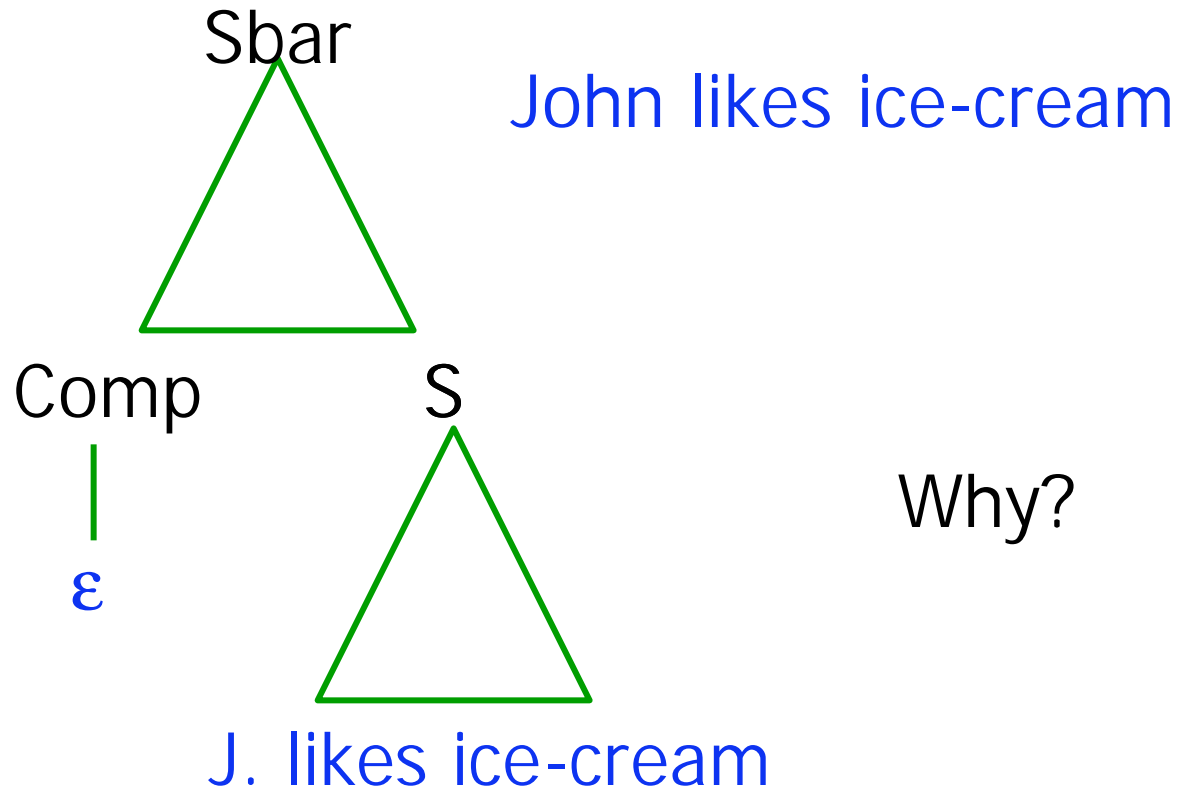
# Sbar



# Sbar



# In fact, true for all sentences...




# What rules will we need?



- (U do it..)



# Verb types - continued



- What about:

Clinton admires honesty/Honesty admires  
Clinton

How do we encode these in a CFG?

Should we encode them?

- Colorless green ideas sleep furiously
- Revolutionary new ideas appear  
infrequently

# Features



# The trouble with tribbles



**morphology** of a single word:

Verb[head=thrill, tense=present, num=sing, person=3,...] → thrills

**projection** of features up to a bigger phrase

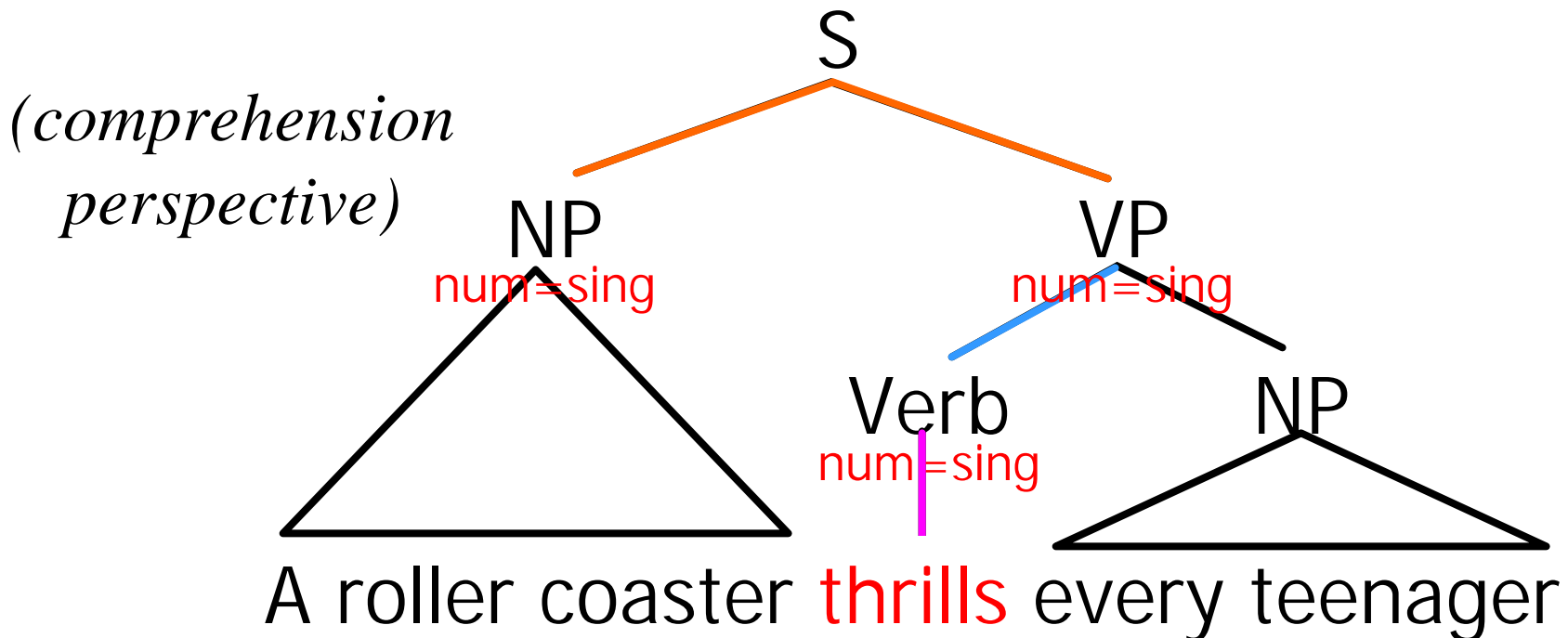
VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] → V[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] NP  
provided  $\alpha$  is in the set TRANSITIVE-VERBS

**agreement** between sister phrases:

S[head= $\alpha$ , tense= $\beta$ ] → NP[num= $\gamma$ ,...] VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...]  
provided  $\alpha$  is in the set TRANSITIVE-VERBS

# 3 Common Ways to Use Features

Verb[head=thrill, tense=present, num=sing, person=3,...] → **thrills**  
VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] → V[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] NP  
S[head= $\alpha$ , tense= $\beta$ ] → NP[num= $\gamma$ ,...] VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...]



# CFG Solution

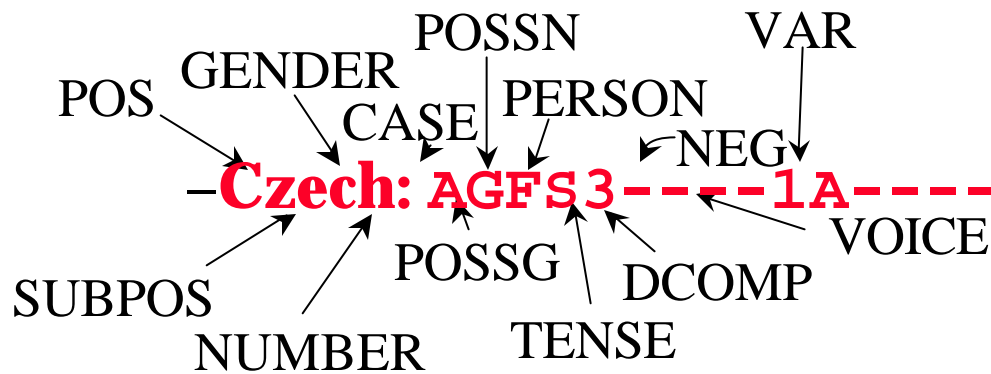


- Encode constraints into the non-terminals
  - Noun/verb agreement
    - $S \rightarrow SgS$
    - $S \rightarrow PIS$
    - $SgS \rightarrow SgNP\ SgVP$
    - $SgNP \rightarrow SgDet\ SgNom$
  - Verb subcategories:
    - $IntransVP \rightarrow IntransV$
    - $TransVP \rightarrow TransV\ NP$

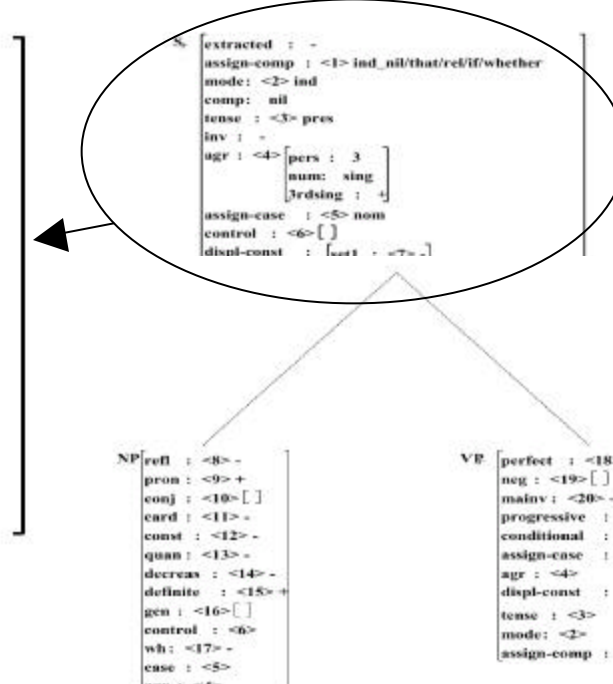


Problems with this – how much  
info?

# Agreement gets complex...

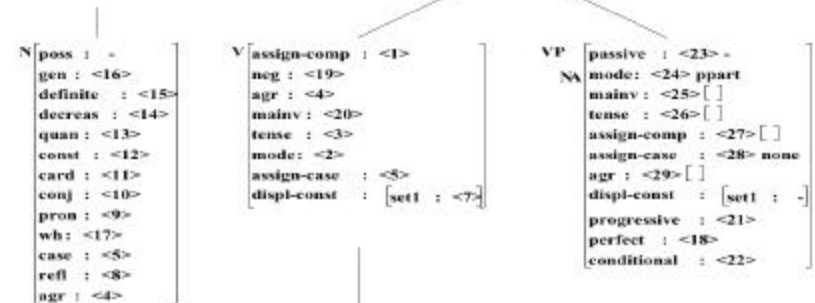


S<sub>7</sub> [ extracted : -  
 assign-comp : <1> ind\_nil/that/rel/if/whether  
 mode: <2> ind  
 comp: nil  
 tense : <3> pres  
 inv : -  
 agr : <4> [ pers : 3  
 num: sing  
 3rdsing : + ]  
 assign-case : <5> nom  
 control : <6> [ ]  
 displ-const : [ set1 : <7> - ]



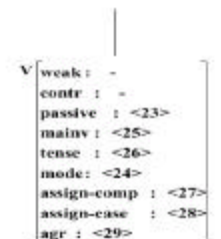
- Lots of features (tense, number, person, gaps, vowels, commas, wh, etc ...)

Heim!



He has

- Sorry, that's just how language is ...
- You know too much to write it down easily!



gone



# Other sentence types



- Questions:
  - Will John eat ice-cream?
  - Did John eat ice-cream?
- How do we encode this?

# `Empty' elements or categories



- Where surface phrase is displaced from its canonical syntactic position
- Examples:
  - The ice-cream was eaten vs.
  - John ate the ice-cream
  - What did John eat?
  - What did Bill say that that John thought the cat ate?
  - For What x, did Bill say... the cat ate x
  - Bush is too stubborn to talk to
  - Bush is too stubborn [x to talk to Bush]
  - Bush is too stubborn to talk to the Pope
  - Bush is too stubborn [Bush to talk to the Pope]

# More interesting clause types

- Apparently “long distance” effects:  
‘displacement’ of phrases from their ‘base’ positions
- 1. So-called ‘wh-movement’:  
*What did John eat ?*
- 2. Topicalization (actually the same)  
*On this day, it snowed two feet.*
- 3. Other cases: so-called ‘passive’:  
*The eggplant was eaten by John*
- How to handle this?

# We can think of this as 'fillers' and 'gaps'

- Filler= the displaced item
- Gap = the place where it belongs, as argument
- Fillers can be NPs, PPs, S's
- Gaps are *invisible*- so hard to parse! (we have to guess)
- Can be complex:

*Which book did you file\_\_ without\_\_ reading\_\_ ?*

*Which violins are these sonatas difficult to play\_\_ on\_\_*

# Gaps (“deep” grammar!)

- Pretend “kiss” is a pure transitive verb.
- Is “the president kissed” grammatical?
  - If so, what type of phrase is it?

- the sandwich that

- I wonder what

- What else has

the president kissed e

Sally said the president kissed e

Sally consumed the pickle with e

Sally consumed e with the pickle

# Gaps

- Object gaps:

- the sandwich that

- I wonder what

- What else has

the president kissed e

Sally said the president kissed e

Sally consumed the pickle with e

Sally consumed e with the pickle

[how could you tell the difference?]

- Subject gaps:

- the sandwich that

- I wonder what

- What else has

e kissed the president

Sally said e kissed the president

# Gaps

- All gaps are really the same – a missing XP:
  - the sandwich that
  - I wonder what
  - What else has
- the president kissed e  
Sally said the president kissed e  
Sally consumed the pickle with e  
Sally consumed e with the pickle  
e kissed the president  
Sally said e kissed the president

Phrases with missing NP:

**X[missing=NP]**

or just **X/NP** for short

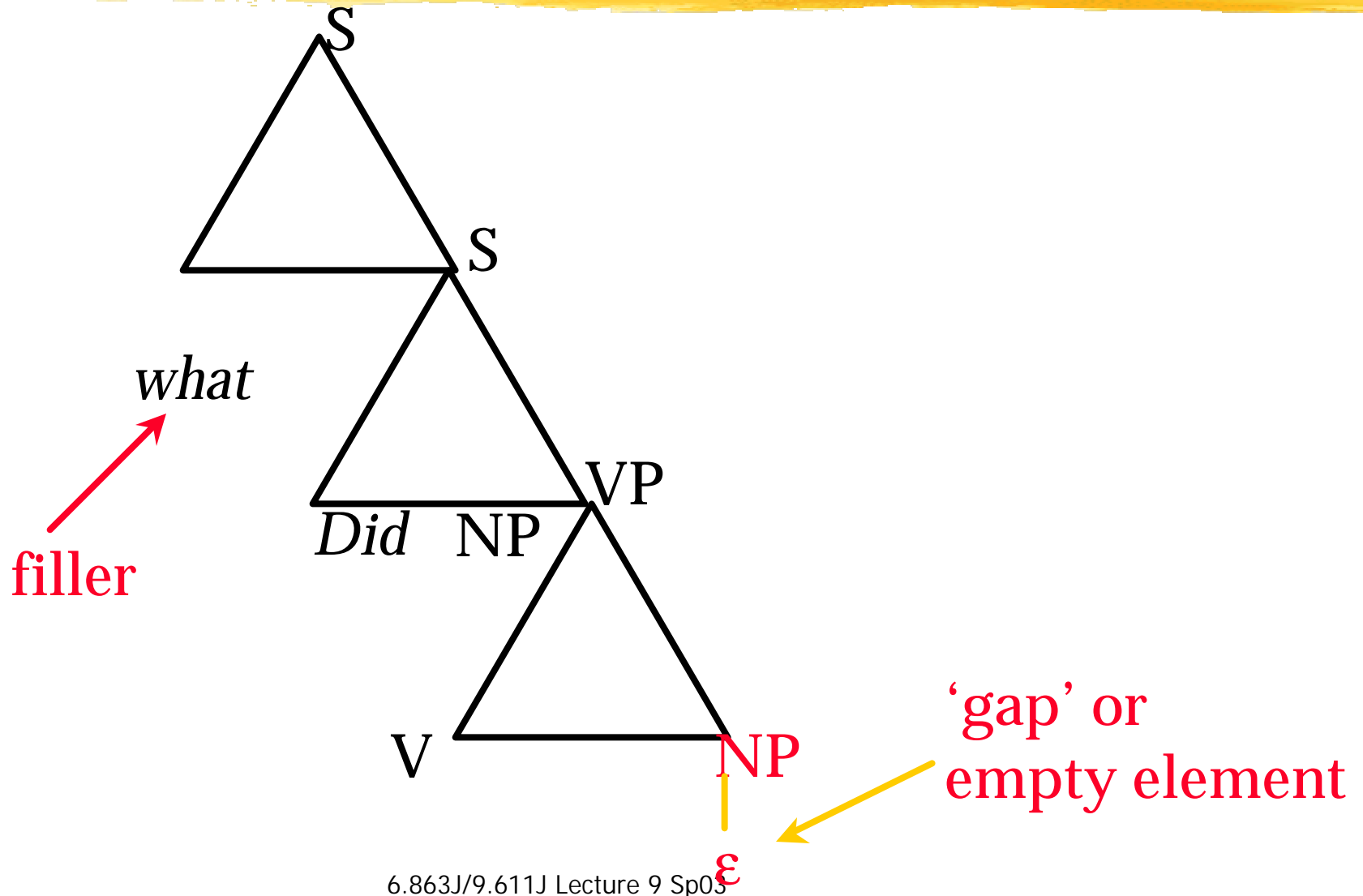
# Representation & computation questions again

- How do we *represent* this displacement?  
(difference between underlying & surface forms)
- How do we *compute* it? (I.e., parse sentences that exhibit it)
- We want to recover the *underlying* structural relationship because this tells us what the predicate-argument relations are – *Who did what to whom*
- Example: *What did John eat* → For which x, x a thing, did John eat x?
- Note how the eat-x predicate-argument is established

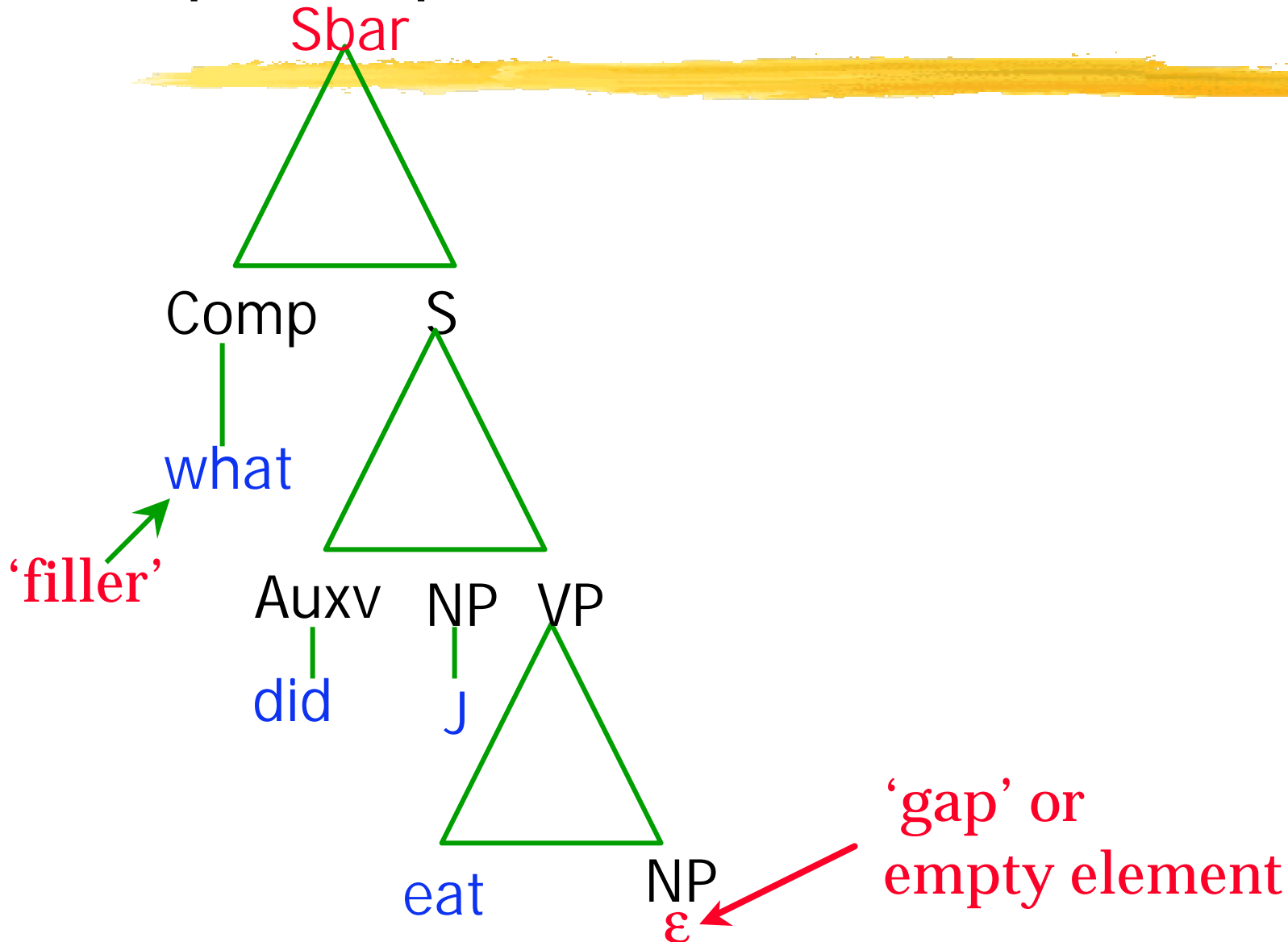


# Representations with gaps

- Let's first look at a tree with gaps:



# Crisper representation:



# Fillers can be arbitrarily far from gaps they match with...

- What did John say that Mary thought that the cat ate\_\_\_\_?

# Fillers and gaps



- Since 'gap' is NP going to empty string, we could just add rule,  $NP \rightarrow \epsilon$
- But this will *overgenerate* why?
- We need a way to distinguish between
  - What did John eat
  - Did John eat
- How did this work in the FSA case?

# So, what do we need



- A rule to expand NP as the empty symbol; that's easy enough:  $NP \rightarrow \epsilon$
- A way to make sure that NP is expanded as empty symbol iff there is a gap (in the right place) before/after it
- A way to link the filler and the gap
- We can do all this by futzing with the nonterminal names: Generalized Phrase Structure Grammar (GPSG)

# Still other 'missing' elements



- John promised Mary \_\_\_\_ to leave
- John promised Mary [John to leave]
- Known as 'control'
  
- John persuaded Mary [\_\_\_\_ to leave]
- John persuaded Mary [Mary to leave]

# Limits of CFGs



- **Agreement** (A cat sleeps. Cats sleep.)

$S \rightarrow NP VP$

$NP \rightarrow Det Nom$

But these rules **overgenerate**, allowing,  
e.g., \*A cat sleep...

- **Subcategorization** (Cats dream. Cats eat cantaloupe.)

$VP \rightarrow V$

$VP \rightarrow V NP$

But these also allow \*Cats dream  
cantaloupe.

- We need to constrain the grammar rules to enforce e.g. number agreement and subcategorization differences
- We'll do this with feature structures and the constraint-based unification formalism



# CFG Solution



- Encode constraints into the non-terminals
  - Noun/verb agreement
    - $S \rightarrow SgS$
    - $S \rightarrow PIS$
    - $SgS \rightarrow SgNP\ SgVP$
    - $SgNP \rightarrow SgDet\ SgNom$
  - Verb subcat:
    - $IntransVP \rightarrow IntransV$
    - $TransVP \rightarrow TransV\ NP$

- But this means huge proliferation of rules...
- An alternative:
  - View terminals and non-terminals as complex objects with associated features, which take on different values
  - Write grammar rules whose application is constrained by tests on these features, e.g.  
 $S \rightarrow NP VP$  (only if the NP and VP agree in number)

# Design advantage



- Decouple skeleton syntactic structure from lexicon
- We'll explore later, for now...

# Feature Structures

- Sets of **feature-value pairs** where:
  - Features are atomic symbols
  - Values are atomic symbols or feature structures
  - Illustrated by **attribute-value matrix**

$$\begin{bmatrix} Feature_1 & Value_1 \\ Feature_2 & Value_2 \\ \dots & \dots \\ Feature_n & Value_n \end{bmatrix}$$

- Number feature

$$\begin{bmatrix} Num & SG \end{bmatrix}$$

- Number-person features

$$\begin{bmatrix} Num & SG \\ Pers & 3 \end{bmatrix}$$

- Number-person-category features

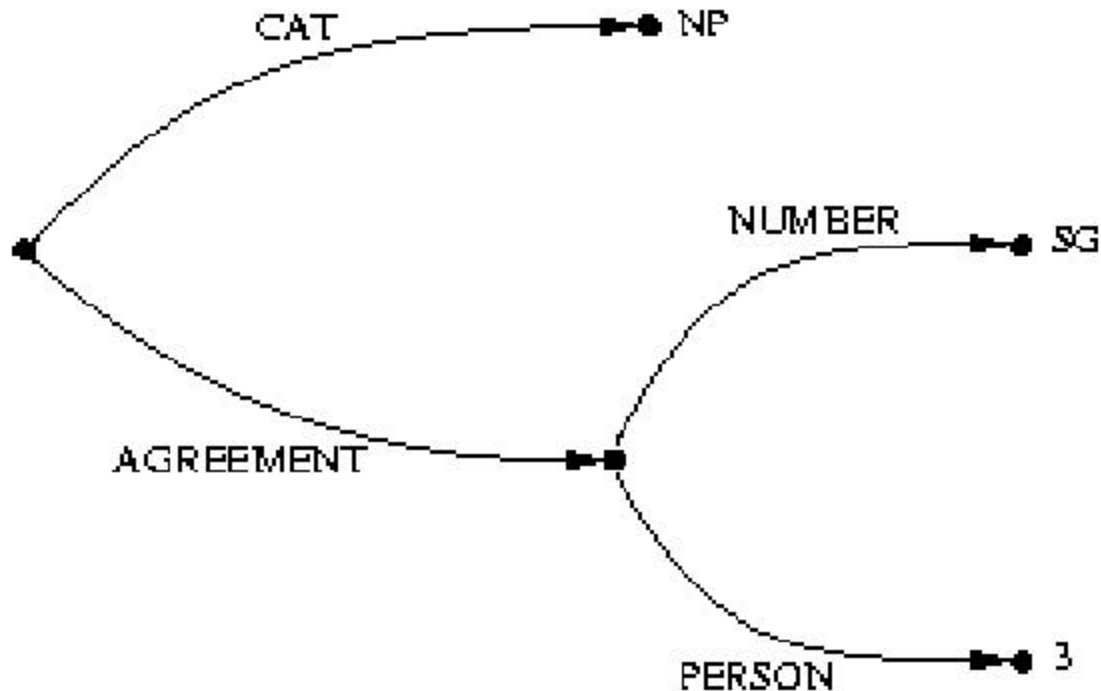
$$(3sgNP) \begin{bmatrix} Cat & NP \\ Num & SG \\ Pers & 3 \end{bmatrix}$$

- How do we define 3pINP?
- How does this improve over the CFG solution?
- Feature values can be feature structures themselves
  - Useful when certain features commonly co-occur, e.g. number and person

$$\left[ \begin{array}{cc} \textit{Cat} & \textit{NP} \\ \textit{Agr} & \left[ \begin{array}{cc} \textit{Num} & \textit{SG} \\ \textit{Pers} & 3 \end{array} \right] \end{array} \right]$$

- Feature path: path through structures to value  
(e.g.  
Agr → Num → SG

# Graphical Notation for Feature Structures



# Reentrant Structures

- Feature structures may also contain features that share some feature structure as a value

$$\left[ \begin{array}{l} \textit{Cat} \ S \\ \\ \textit{Head} \left[ \begin{array}{l} \textit{Agr} \ 1 \ \left[ \begin{array}{l} \textit{Num} \ SG \\ \textit{Pers} \ 3 \end{array} \right] \\ \textit{Subj} \ \left[ \textit{Agr} \ 1 \ \right] \end{array} \right] \end{array} \right]$$

- Numerical indices indicate the shared values



# Operations on Feature Structures



- What will we need to do to these structures?
  - Check the **compatibility** of two structures
  - **Merge** the information in two structures
- We can do both using **unification**
- We say that two feature structures **can be unified** if the component features that make them up are **compatible**
  - $[\text{Num SG}] \cup [\text{Num SG}] = [\text{Num SG}]$
  - $[\text{Num SG}] \cup [\text{Num PL}]$  fails!
  - $[\text{Num SG}] \cup [\text{Num } []] = [\text{Num SG}]$

- $[\text{Num SG}] \cup [\text{Pers 3}] = \begin{bmatrix} \text{Num SG} \\ \text{Pers 3} \end{bmatrix}$
- Structures are compatible if they contain no features that are **in**compatible
- Unification of two feature structures:
  - Are the structures compatible?
  - If so, return the union of all feature/value pairs

- A failed unification attempt
 
$$\begin{bmatrix} \text{Agr } 1 \begin{bmatrix} \text{Num SG} \\ \text{Pers 3} \end{bmatrix} \\ \text{Subj } \begin{bmatrix} \text{Agr} & 1 \end{bmatrix} \end{bmatrix} \cup \begin{bmatrix} \text{Agr } \begin{bmatrix} \text{Num PL} \\ \text{Pers 3} \end{bmatrix} \\ \text{Subj } \begin{bmatrix} \text{Agr } \begin{bmatrix} \text{Num PL} \\ \text{Pers 3} \end{bmatrix} \end{bmatrix} \end{bmatrix}$$

# Features, Unification and Grammars

- How do we incorporate feature structures into our grammars?
  - Assume that constituents are objects which have feature-structures associated with them
  - Associate sets of unification constraints with grammar rules
  - Constraints must be satisfied for rule to be satisfied
- For a grammar rule  $\beta_0 \rightarrow \beta_1 \dots \beta_n$ 
  - $\langle \beta_i \text{ feature path} \rangle = \text{Atomic value}$
  - $\langle \beta_i \text{ feature path} \rangle = \langle \beta_j \text{ feature path} \rangle$

- To enforce subject/verb number agreement

$S \rightarrow NP VP$

$\langle NP \text{ NUM} \rangle = \langle VP \text{ NUM} \rangle$

# Agreement in English



- We need to add PERS to our subj/verb agreement constraint

This cat likes kibble.

$S \rightarrow NP V_p$

$\langle NP \text{ AGR} \rangle = \langle VP \text{ AGR} \rangle$

Do these cats like kibble?

$S \rightarrow Aux NP VP$

$\langle Aux \text{ AGR} \rangle = \langle NP \text{ AGR} \rangle$

- Det/Nom agreement can be handled similarly

These cats

This cat

NP  $\rightarrow$  Det Nom

$\langle \text{Det AGR} \rangle = \langle \text{Nom AGR} \rangle$

$\langle \text{NP AGR} \rangle = \langle \text{Nom AGR} \rangle$

- And so on for other constituents and rules

# Head Features

- Features of most grammatical categories are copied from **head** child to parent (e.g. from V to VP, Nom to NP, N to Nom, ...)
- These normally written as 'head' features, e.g.

VP → V NP

<VP HEAD> = <V HEAD>

NP → Det Nom

<NP→ HEAD> = <Nom HEAD>

<Det HEAD AGR> = <Nom HEAD AGR>

Nom → N

<Nom HEAD> = <N HEAD>

# Subcategorization

- Recall: Different verbs take different types of argument
  - Solution: SUBCAT feature, or **subcategorization frames**

e.g.

$$\left[ \begin{array}{ll} ORTH & want \\ CAT & V \\ HEAD & \left[ SUBCAT \left\langle [CAT \ NP], \left[ \begin{array}{l} CAT \ VP \\ HEAD [VFORM \ INF] \end{array} \right] \right\rangle \right] \end{array} \right]$$



- But there are many phrasal types and so many types of subcategorization frames, e.g.
  - believe
  - believe [VPrep in] [NP ghosts]
  - believe [NP my mother]
  - believe [Sfin that I will pass this test]
  - believe [Swh what I see] ...
- Verbs also subcategorize for subject as well as object types ([<sub>Swh</sub> What she wanted] seemed clear.)
- And other p.o.s. can be seen as subcategorizing for various arguments, such as prepositions, nouns and adjectives (It was clear [Sfin that she was exhausted])

- NB: p.o.s. that subcategorize similarly define rough classes e.g. verb categories like **transfer verbs** and subcat frame relationships within verb classes are called **alternations**
  - George gave Martha a letter [NP NP]
  - George gave a letter to Martha [NP PP]

# Long-Distance Dependencies



- What happens when a verb's arguments are not in the VP?
  - What meals does the restaurant serve?  
Wh-NP fills a slot in serve  
S --> wh-NP Aux NP VP
- How to solve?
  - Gap list: GAP feature (filler: what meals) passed up from phrase to phrase in parse tree -- complicated mechanism
  - Even bigger problem for representations such as FSAs and Ngrams

# How can we parse with feature structures?

- Unification operator: takes 2 features structures and returns ***either*** a merged feature structure or *fail*
- Input structures represented as DAGs
  - Features are labels on edges
  - Values are atomic symbols or DAGs
- Unification algorithm goes through features in one input  $DAG_1$  trying to find corresponding features in  $DAT_2$  – if all match, success, else fail

# Unification and Chart Parsing

- Goal:
  - Use feature structures to provide richer representation
  - Block entry into chart of ill-formed constituents
- Changes needed to Earley
  - Add feature structures to grammar rules, e.g.  
 $S \rightarrow NP VP$   
 $\langle NP \text{ HEAD AGR} \rangle = \langle VP \text{ HEAD AGR} \rangle$   
 $\langle S \text{ HEAD} \rangle = \langle VP \text{ HEAD} \rangle$
  - Add field to states containing DAG representing feature structure corresponding to state of parse, e.g.  
 $S \rightarrow \bullet NP VP, [0,0], [], DAG$

- Add new test to Completer operation
  - Recall: Completer adds new states to chart by finding states whose • can be advanced (i.e., category of next constituent matches that of completed constituent)
  - Now: Completer will only advance those states if their feature structures unify
- New test for whether to enter a state in the chart
  - Now DAGs may differ, so check must be more complex
  - Don't add states that have DAGs that are more specific than states in chart: is new state subsumed by existing states?

# Summing Up



- Feature structures encoded rich information about components of grammar rules
- Unification provides a mechanism for merging structures and for comparing them
- Feature structures can be quite complex:
  - Subcategorization constraints
  - Long-distance dependencies
- Unification parsing:
  - Merge or fail
  - Modifying Earley to do unification parsing