

# 6.863J Natural Language Processing

## Lecture 9: Writing grammars; feature-based grammars

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### The Menu Bar

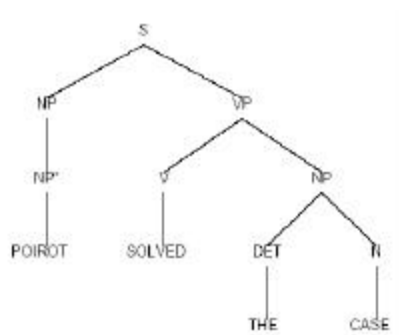
- **Administrivia:**
  - Schedule alert: Lab 3 out; due next Weds.
  - Lab time today, tomorrow
  - Please read notes3.pdf!!  
englishgrammar.pdf (on web)
- *Agenda:*
  - Building grammars – basics to complex
  - Limits of context-free grammars: the trouble with tribbles
  - Foundation for the laboratory

# Grammars for natural languages

- Where do the rules come from?
- Roughly: read them off of parse trees...
- A “rule-based”, construction-based point of view
- Take ‘surface’ phrase patterns (mostly)
- But we still want to map to an *underlying* ‘logical’ form
- How do we start out?

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## Reading rules from parse trees...



$S \rightarrow NP VP$

$VP \rightarrow V NP$

$NP \rightarrow Det N$

$NP \rightarrow N^*$

Can't we get a computer to do this?

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## Key elements – part 1

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- Establish basic phrase types: S, VP, NP, PP, ...
- Where do these come from???

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## What *kinds* of phrases are there?

---

- Noun phrases, verb phrases, adjectival phrases ("green with envy"), adverbial phrases ("quickly up the hill"), prepositional phrases ("off the wall"), etc.
- In general: *grounded* on lexical items
- Shows us the *constraints* on context-free rules for *natural grammars*
- Example:

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## Phrase types are constrained by lexical projection

Verb Phrase →	Verb	Noun Phrase
“is-a”	(“kick the ball”)	
Prepositional Phrase →	Preposition	Noun Phrase
	(“on the table”)	
Adjective Phrase →	Adjective	Prep. Phrase
	(“green with envy”)	

Etc. ... what is the pattern?

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## Function-argument relation

XP → X arguments, where X = Noun, Verb, Preposition, Adjective (all lexical categories in the language)

Like function-argument structure  
(so-called “Xbar theory”)

Constrains what grammar rules *cannot* be:

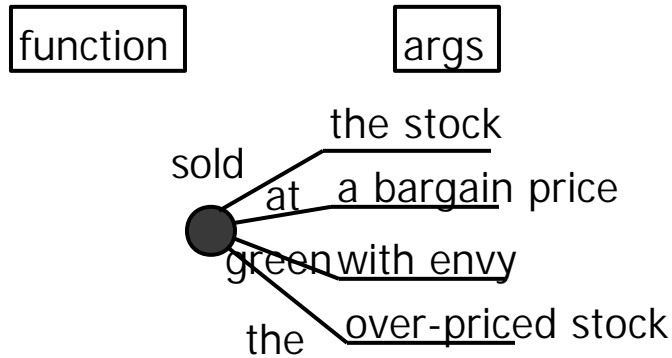
Verb Phrase → Noun Noun Phrase

or even

Verb Phrase → Noun Phrase Verb Noun Phrase

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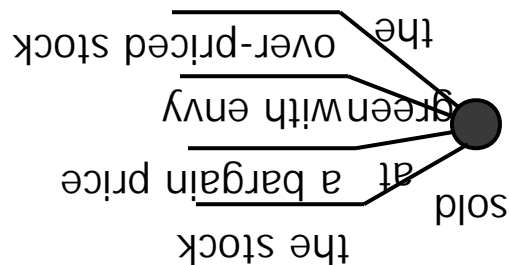
## English is function-argument form



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## Other languages are the mirror-inverse: arg-function

This is like Japanese



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## Key elements – part 2

- Establish *verb subcategories*
- What are these?
  - Different verbs take different # arguments
  - 0, 1, 2 arguments ('complements')
  - Poirot thought; Poirot thought the gun; Poirot thought the gun was the cause.
  - Some verbs take certain sentence complements:
    - *I know who John saw/? I think who John saw*
  - propositional types:
    - Embedded questions: *I wonder whether...*
    - Embedded proposition: *I think that John saw Mary*

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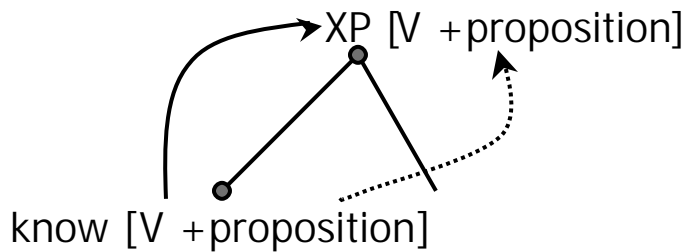
## Key elements

- Subtlety to this
- Believe, know, think, wonder, ...
  - ? I believe why John likes ice-cream
  - I know why John likes ice-cream
  - I believe that John likes ice-cream
  - I believe (that) John likes ice-cream
- # args, type: Verb subcategories
- How many subcategories are there?
- What is the structure?

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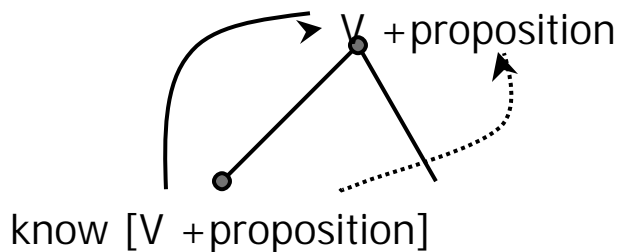
## Idea for phrases

- They are based on 'projections' of words (lexical items) – imagine features 'percolating' up



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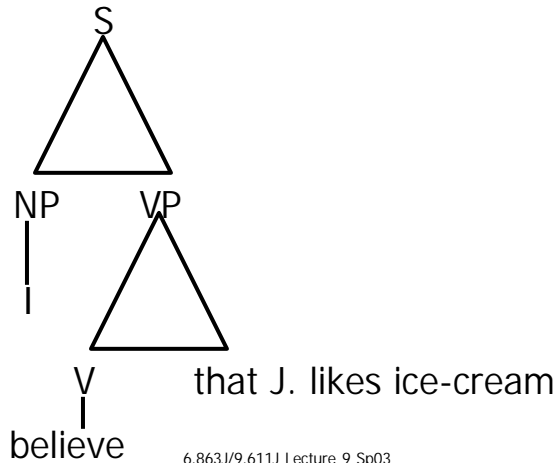
## Heads of phrases



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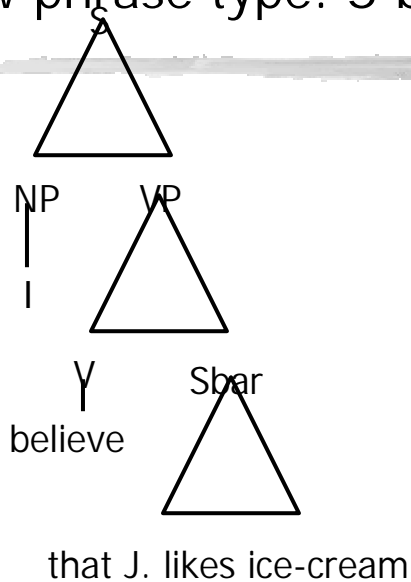
## The parse structure for 'embedded' sentences

I believe (that) John likes ice-cream



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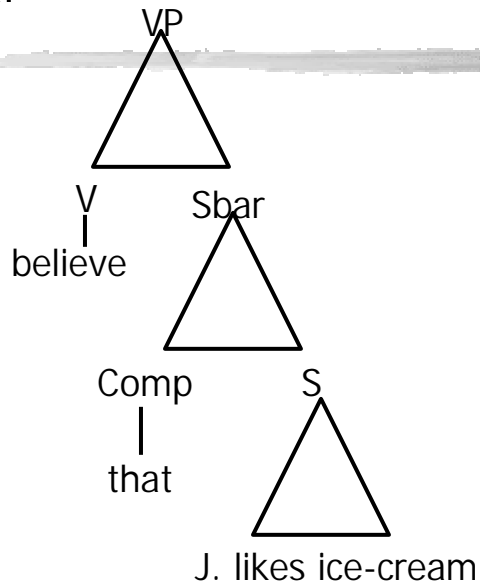
## New phrase type: S-bar



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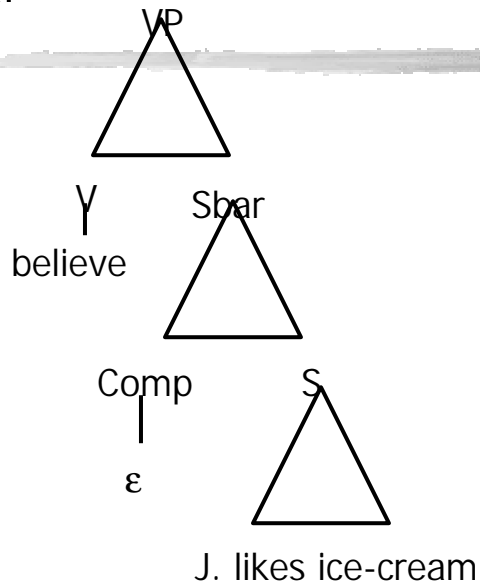


# Sbar



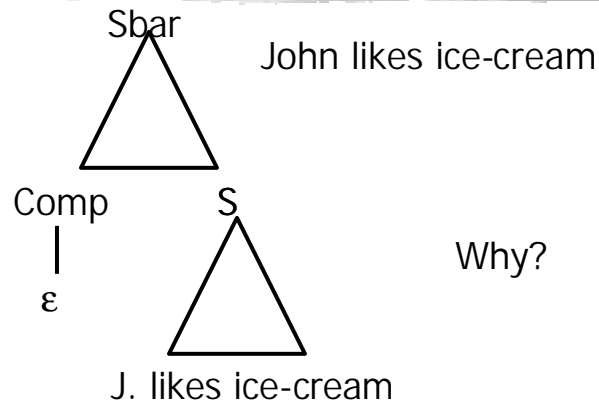
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# Sbar



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In fact, true for all sentences...



Why?


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What rules will we need?

- (U do it..)

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## Verb types - continued



- What about:

Clinton admires honesty/Honesty admires  
Clinton

How do we encode these in a CFG?

Should we encode them?

- Colorless green ideas sleep furiously
- Revolutionary new ideas appear  
infrequently

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## Features



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## The trouble with tribbles

morphology of a single word:

Verb[head=thrill, tense=present, num=sing, person=3,...] → thrills

projection of features up to a bigger phrase

VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] → V[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] NP  
provided  $\alpha$  is in the set TRANSITIVE-VERBS

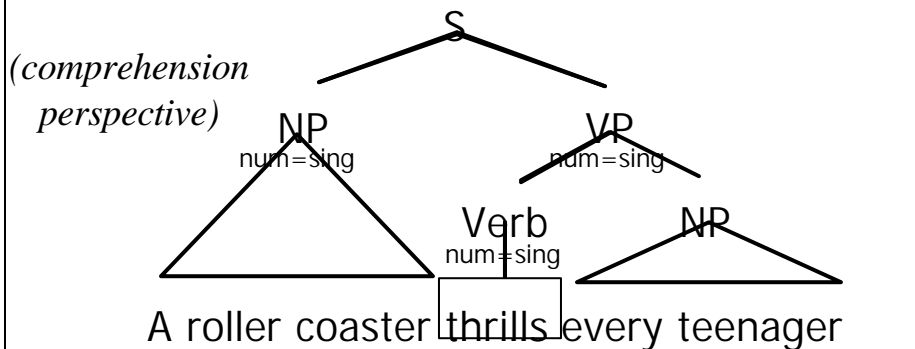
agreement between sister phrases:

S[head= $\alpha$ , tense= $\beta$ ] → NP[num= $\gamma$ ...] VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...]  
provided  $\alpha$  is in the set TRANSITIVE-VERBS

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## 3 Common Ways to Use Features

Verb[head=thrill, tense=present, num=sing, person=3,...] → thrills  
VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] → V[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...] NP  
S[head= $\alpha$ , tense= $\beta$ ] → NP[num= $\gamma$ ...] VP[head= $\alpha$ , tense= $\beta$ , num= $\gamma$ ...]



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# CFG Solution

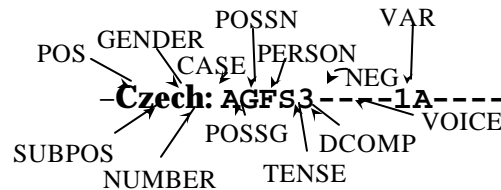
- Encode constraints into the non-terminals
  - Noun/verb agreement
    - $S \rightarrow SgS$
    - $S \rightarrow PlS$
    - $SgS \rightarrow SgNP\ SgVP$
    - $SgNP \rightarrow SgDet\ SgNom$
  - Verb subcategories:
    - $IntransVP \rightarrow IntransV$
    - $TransVP \rightarrow TransV\ NP$

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Problems with this – how much info?

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# Agreement gets complex...



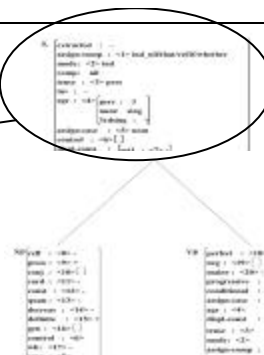
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```

S<_ extracted : =
assign-comp : <1> ind_nil/that/rel/if/whether
mode: <2> ind
comp: nil
tense : <3> pres
inv : =
agr : <4> [ pers : 3
           num: sing
           3rdsing : + ]
assign-case : <5> nom
control : <6> [ ]
displ-const : [set1 : <7> - ]
    
```

- Lots of features (tense, number, person, gender, vowels, commas, wh, etc...)

**Hein!**



He

has

gone

- Sorry, that's just how language is ...
- You know too much to write it down easily!

## Other sentence types

- Questions:
  - Will John eat ice-cream?
  - Did John eat ice-cream?
- How do we encode this?

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## `Empty' elements or categories

- Where surface phrase is displaced from its canonical syntactic position
- Examples:
  - The ice-cream was eaten vs.
  - John ate the ice-cream
  - What did John eat?
  - What did Bill say that that John thought the cat ate?
  - For What x, did Bill say... the cat ate x
  - Bush is too stubborn to talk to
  - Bush is too stubborn [x to talk to Bush]
  - Bush is too stubborn to talk to the Pope
  - Bush is too stubborn [Bush to talk to the Pope]

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## More interesting clause types

- Apparently “long distance” effects: ‘displacement’ of phrases from their ‘base’ positions
- 1. So-called ‘wh-movement’:  
*What did John eat ?*
- 2. Topicalization (actually the same)  
*On this day, it snowed two feet.*
- 3. Other cases: so-called ‘passive’:  
*The eggplant was eaten by John*
- How to handle this?

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## We can think of this as ‘fillers’ and ‘gaps’

- Filler= the displaced item
- Gap = the place where it belongs, as argument
- Fillers can be NPs, PPs, S’s
- Gaps are *invisible*- so hard to parse! (we have to guess)
- Can be complex:  
*Which book did you file\_\_\_ without\_\_\_ reading\_\_\_ ?*  
*Which violins are these sonatas difficult to play\_\_\_ on*

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## Gaps ("deep" grammar!)

- Pretend "kiss" is a pure transitive verb.
- Is "the president kissed" grammatical?
  - If so, what type of phrase is it?

- the sandwich that
  - I wonder what
  - What else has
- the president kissed e  
Sally said the president kissed e  
Sally consumed the pickle with e  
Sally consumed e with the pickle

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## Gaps

- Object gaps:
  - ~~the sandwich~~ that
  - I wonder ~~what~~
  - ~~What else~~ has
- the president kissed e  
Sally said the president kissed e  
Sally consumed the pickle with e  
Sally consumed e with the pickle

[how could you tell the difference?]

- Subject gaps:
  - ~~the sandwich~~ that
  - I wonder ~~what~~
  - ~~What else~~ has
- e kissed the president  
Sally said e kissed the president

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## Gaps

- All gaps are really the same – a missing XP:
  - the sandwich that
  - I wonder what
  - What else has
- } the president kissed e  
Sally said the president kissed e  
Sally consumed the pickle with e  
Sally consumed e with the pickle  
e kissed the president  
Sally said e kissed the president

Phrases with missing NP:  
X[missing=NP]  
or just X/NP for short

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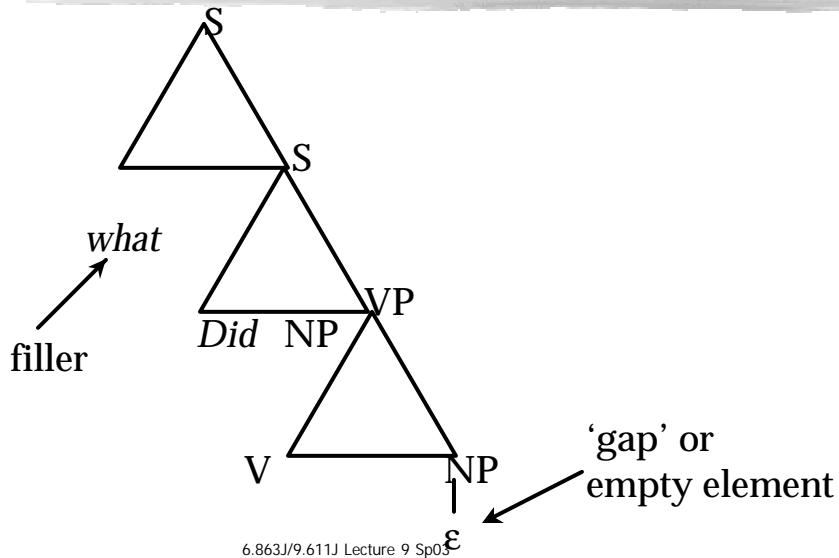
## Representation & computation questions again

- How do we *represent* this displacement?  
(difference between underlying & surface forms)
- How do we *compute* it? (I.e., parse sentences that exhibit it)
- We want to recover the *underlying* structural relationship because this tells us what the predicate-argument relations are – *Who did what to whom*
- Example: *What did John eat* → For which x, x a thing, did John eat x?
- Note how the eat-x predicate-argument is established

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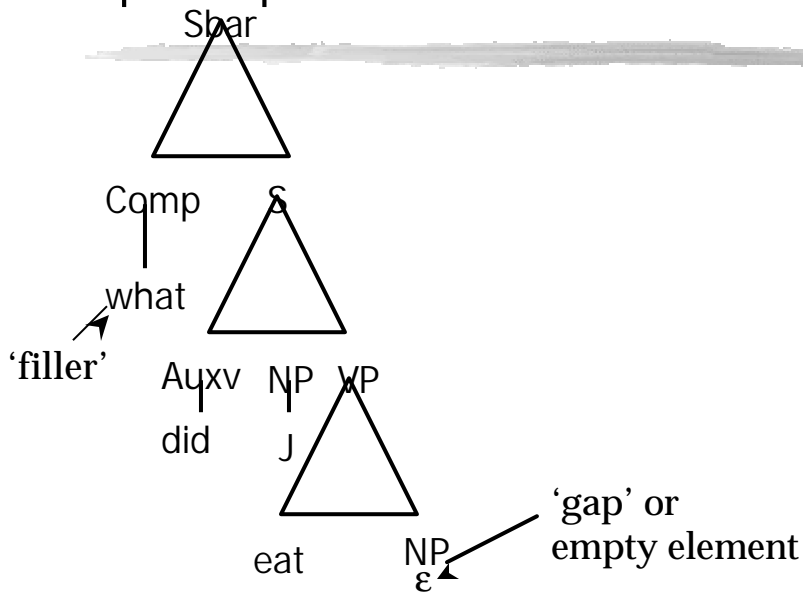
## Representations with gaps

- Let's first look at a tree with gaps:



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## Crisper representation:



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## Fillers can be arbitrarily far from gaps they match with...

- What did John say that Mary thought that the cat ate\_\_\_\_?

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## Fillers and gaps

- Since 'gap' is NP going to empty string, we could just add rule,  $NP \rightarrow \epsilon$
- But this will *overgenerate* why?
- We need a way to distinguish between
  - What did John eat
  - Did John eat
- How did this work in the FSA case?

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## So, what do we need

- A rule to expand NP as the empty symbol; that's easy enough:  $NP \rightarrow \epsilon$
- A way to make sure that NP is expanded as empty symbol iff there is a gap (in the right place) before/after it
- A way to link the filler and the gap
- We can do all this by futzing with the nonterminal names: Generalized Phrase Structure Grammar (GPSG)

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## Still other 'missing' elements

- John promised Mary \_\_\_\_ to leave
- John promised Mary [John to leave]
- Known as 'control'
  
- John persuaded Mary [\_\_\_\_ to leave]
- John persuaded Mary [Mary to leave]

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## Limits of CFGs

- Agreement (A cat sleeps. Cats sleep.)

$S \rightarrow NP VP$

$NP \rightarrow Det Nom$

But these rules overgenerate, allowing,  
e.g., \*A cat sleep...

- Subcategorization (Cats dream. Cats eat cantaloupe.)

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$VP \rightarrow V$

$VP \rightarrow V NP$

But these also allow \*Cats dream  
cantaloupe.

- We need to constrain the grammar rules to enforce e.g. number agreement and subcategorization differences
- We'll do this with feature structures and the constraint-based unification formalism

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# CFG Solution

- Encode constraints into the non-terminals
  - Noun/verb agreement
    - $S \rightarrow \text{SgS}$
    - $S \rightarrow \text{PlS}$
    - $\text{SgS} \rightarrow \text{SgNP SgVP}$
    - $\text{SgNP} \rightarrow \text{SgDet SgNom}$
  - Verb subcat:
    - $\text{IntransVP} \rightarrow \text{IntransV}$
    - $\text{TransVP} \rightarrow \text{TransV NP}$

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- But this means huge proliferation of rules...
- An alternative:
  - View terminals and non-terminals as complex objects with associated features, which take on different values
  - Write grammar rules whose application is constrained by tests on these features, e.g.
    - $S \rightarrow \text{NP VP}$  (only if the NP and VP agree in number)

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## Design advantage

- Decouple skeleton syntactic structure from lexicon
- We'll explore later, for now...

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## Feature Structures

- Sets of feature-value pairs where:
  - Features are atomic symbols
  - Values are atomic symbols or feature structures
  - Illustrated by attribute-value matrix

$$\begin{bmatrix} Feature_1 & Value_1 \\ Feature_2 & Value_2 \\ \dots & \dots \\ Feature_n & Value_n \end{bmatrix}$$

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- Number feature

$$\begin{bmatrix} Num & SG \end{bmatrix}$$

- Number-person features

$$\begin{bmatrix} Num & SG \\ Pers & 3 \end{bmatrix}$$

- Number-person-category features

$$(3sgNP) \begin{bmatrix} Cat & NP \\ Num & SG \\ Pers & 3 \end{bmatrix}$$

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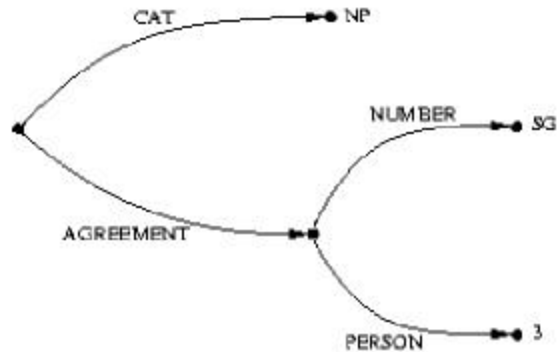
- How do we define 3pINP?
- How does this improve over the CFG solution?
- Feature values can be feature structures themselves
  - Useful when certain features commonly co-occur, e.g. number and person

$$\begin{bmatrix} Cat & NP \\ Agr & \begin{bmatrix} Num & SG \\ Pers & 3 \end{bmatrix} \end{bmatrix}$$

- Feature path: path through structures to value  
(e.g.  
Agr → Num → SG

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# Graphical Notation for Feature Structures



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## Reentrant Structures

- Feature structures may also contain features that share some feature structure as a value

$$\left[ \begin{array}{l} \text{Cat } S \\ \text{Head } \left[ \begin{array}{l} \text{Agr } 1 \left[ \begin{array}{l} \text{Num } SG \\ \text{Pers } 3 \end{array} \right] \\ \text{Subj } \left[ \text{Agr } 1 \right] \end{array} \right] \end{array} \right]$$

- Numerical indices indicate the shared values

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# Operations on Feature Structures

- What will we need to do to these structures?
  - Check the compatibility of two structures
  - Merge the information in two structures
- We can do both using unification
- We say that two feature structures can be unified if the component features that make them up are compatible
  - [Num SG] U [Num SG] = [Num SG]
  - [Num SG] U [Num PL] fails!
  - [Num SG] U [Num []] = [Num SG]

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- $$[\text{Num SG}] \cup [\text{Pers 3}] = \begin{bmatrix} \text{Num SG} \\ \text{Pers 3} \end{bmatrix}$$
- Structures are compatible if they contain no features that are **in**compatible
- Unification of two feature structures:
  - Are the structures compatible?
  - If so, return the union of all feature/value pairs
- A failed unification attempt

$$\begin{bmatrix} \text{Agr 1} \begin{bmatrix} \text{Num SG} \\ \text{Pers 3} \end{bmatrix} \\ \text{Subj} \begin{bmatrix} \text{Agr} \quad 1 \end{bmatrix} \end{bmatrix} \cup \begin{bmatrix} \text{Agr} \begin{bmatrix} \text{Num PL} \\ \text{Pers 3} \end{bmatrix} \\ \text{Subj} \begin{bmatrix} \text{Agr} \begin{bmatrix} \text{Num PL} \\ \text{Pers 3} \end{bmatrix} \end{bmatrix} \end{bmatrix}$$

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# Features, Unification and Grammars

- How do we incorporate feature structures into our grammars?
  - Assume that constituents are objects which have feature-structures associated with them
  - Associate sets of unification constraints with grammar rules
  - Constraints must be satisfied for rule to be satisfied
- For a grammar rule  $\beta_0 \rightarrow \beta_1 \dots \beta_n$ 
  - $\langle \beta_i \text{ feature path} \rangle = \text{Atomic value}$
  - $\langle \beta_i \text{ feature path} \rangle = \langle \beta_j \text{ feature path} \rangle$

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- To enforce subject/verb number agreement

$S \rightarrow NP VP$

$\langle NP \text{ NUM} \rangle = \langle VP \text{ NUM} \rangle$

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# Agreement in English

- We need to add PERS to our subj/verb agreement constraint

This cat likes kibble.

S → NP Vp

<NP AGR> = <VP AGR>

Do these cats like kibble?

S → Aux NP VP

<Aux AGR> = <NP AGR>

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- Det/Nom agreement can be handled similarly

These cats

This cat

NP → Det Nom

<Det AGR> = <Nom AGR>

<NP AGR> = <Nom AGR>

- And so on for other constituents and rules

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# Head Features

- Features of most grammatical categories are copied from head child to parent (e.g. from V to VP, Nom to NP, N to Nom, ...)

- These normally written as 'head' features, e.g.

VP → V NP

<VP HEAD> = <V HEAD>

NP → Det Nom

<NP HEAD> = <Nom HEAD>

<Det HEAD AGR> = <Nom HEAD AGR>

Nom → N

<Nom HEAD> = <N HEAD>

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# Subcategorization

- Recall: Different verbs take different types of argument

- Solution: SUBCAT feature, or subcategorization frames

e.g.

*ORTH want*  
*CAT V*

*HEAD*  $\left[ \text{SUBCAT} \left\langle \left[ \text{CAT NP} \right], \left[ \text{CAT VP} \right] \right\rangle \left[ \text{HEAD} \left[ \text{VFORM INF} \right] \right] \right]$

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- But there are many phrasal types and so many types of subcategorization frames, e.g.
  - believe
  - believe [VPrep in] [NP ghosts]
  - believe [NP my mother]
  - believe [Sfin that I will pass this test]
  - believe [Swh what I see] ...
- Verbs also subcategorize for subject as well as object types ([<sub>Swh</sub> What she wanted] seemed clear.)
- And other p.o.s. can be seen as subcategorizing for various arguments, such as prepositions, nouns and adjectives (It was clear [Sfin that she was exhausted])

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- NB: p.o.s. that subcategorize similarly define rough classes e.g. verb categories like transfer verbs and subcat frame relationships within verb classes are called alternations
  - George gave Martha a letter [NP NP]
  - George gave a letter to Martha [NP PP]

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# Long-Distance Dependencies

- What happens when a verb's arguments are not in the VP?
  - What meals does the restaurant serve?  
Wh-NP fills a slot in serve  
S --> wh-NP Aux NP VP
- How to solve?
  - Gap list: GAP feature (filler: what meals) passed up from phrase to phrase in parse tree -- complicated mechanism
  - Even bigger problem for representations such as FSAs and Ngrams

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# How can we parse with feature structures?

- Unification operator: takes 2 features structures and returns **either** a merged feature structure or *fail*
- Input structures represented as DAGs
  - Features are labels on edges
  - Values are atomic symbols or DAGs
- Unification algorithm goes through features in one input DAG<sub>1</sub> trying to find corresponding features in DAT<sub>2</sub> – if all match, success, else fail

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# Unification and Chart Parsing

- Goal:
  - Use feature structures to provide richer representation
  - Block entry into chart of ill-formed constituents
- Changes needed to Earley
  - Add feature structures to grammar rules, e.g.  
S  $\rightarrow$  NP VP  
<NP HEAD AGR> = <VP HEAD AGR>  
<S HEAD> = <VP HEAD>
  - Add field to states containing DAG representing feature structure corresponding to state of parse, e.g.  
S  $\rightarrow$  • NP VP, [0,0], [], DAG

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- Add new test to Completer operation
  - Recall: Completer adds new states to chart by finding states whose • can be advanced (i.e., category of next constituent matches that of completed constituent)
  - Now: Completer will only advance those states if their feature structures unify
- New test for whether to enter a state in the chart
  - Now DAGs may differ, so check must be more complex
  - Don't add states that have DAGs that are more specific than states in chart: is new state subsumed by existing states?

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# Summing Up

- Feature structures encoded rich information about components of grammar rules
- Unification provides a mechanism for merging structures and for comparing them
- Feature structures can be quite complex:
  - Subcategorization constraints
  - Long-distance dependencies
- Unification parsing:
  - Merge or fail
  - Modifying Earley to do unification parsing