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Computer Vision and Applications

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Lecture 15: Fitting and Segmentation

Readings: F&P Ch 15.3-15.5,16

Last time: "Segmentation and Clustering (Ch. 14)"

- Supervised->Unsupervised Category Learning needs segmentation
- K-Means
- Mean Shift
- Graph cuts
- Hough transform















Today "Fitting and Segmentation (Ch. 15)"

- Robust estimation
- EM
- Model Selection
- RANSAC

(Maybe "Segmentation I" and "Segmentation II" would be a better way to split these two lectures!)











Robust Statistics

- Recover the best fit to the majority of the data.
- Detect and reject outliers.





































Estimating Flow

Minimize:

$$E(\mathbf{a}) = \sum_{\mathbf{x} \in R} \rho(\mathbf{I}_{x} u(\mathbf{x}; \mathbf{a}) + \mathbf{I}_{u} v(\mathbf{x}; \mathbf{a}) + \mathbf{I}_{t}, \sigma)$$

Parameterized models provide strong constraints:

* Hundred, or thousands, of constraints.

* Handful (e.g. six) unknowns.

Can be very accurate (when the model is good)!















Alternative View * There are two things going on simultaneously. * We don't know which constraint lines correspond to which motion. * If we knew this we could estimate the multiple motions. - a type of "segmentation" problem * If we knew the segmentation then estimating the motion would be easy.





Missing variable problems

- A missing data problem is a statistical problem where some data is missing
- There are two natural contexts in which missing data are important:
- terms in a data vector are missing for some instances and present for other (perhaps someone responding to a survey was embarrassed by a question)
- an inference problem can be made very much simpler by rewriting it using some variables whose values are unknown.

Missing variable problems

- In many vision problems, if some variables were known the maximum likelihood inference problem would be easy
 - fitting; if we knew which line each token came from, it would be easy to determine line parameters
 - segmentation; if we knew the segment each pixel came from, it would be easy to determine the segment parameters
 - fundamental matrix estimation; if we knew which feature corresponded to which, it would be easy to determine the fundamental matrix
 - etc.

Strategy

- For each of our examples, if we knew the missing data we could estimate the parameters effectively.
- If we knew the parameters, the missing data would follow.

This suggests an iterative algorithm:

- obtain some estimate of the missing data, using a guess at the parameters;
- 2. now form a maximum likelihood estimate of the free parameters using the estimate of the missing data. 49























































Issues with EM

- Local maxima
 - $-\,$ can be a serious nuisance in some problems
 - no guarantee that we have reached the "right" maximum
- Starting
 - k means to cluster the points is often a good idea







Choosing parameters

- What about the noise parameter, and the sigma for the line?
 - several methods
 - from first principles knowledge of the problem (seldom really possible)
 - play around with a few examples and choose (usually quite effective, as precise choice doesn't matter much)
 - notice that if $k_{\rm n}$ is large, this says that points very seldom come from noise, however far from the line they lie
 - · usually biases the fit, by pushing outliers into the line
 - rule of thumb; its better to fit to the better fitting points, within reason; if this is hard to do, then the model could be a problem



- In weighted scenario, additional models will not necessarily reduce the total error.
- The optimal number of models is a function of the σ parameter how well we expect the model to fit the data.
- Algorithm: start with many models. redundant models will collapse.



















































RANSAC

- Iterate:
 - Sample
 - Fit
 - Test
- · Keep best estimate; refit on inliers



RANSAC applications

- · Fundamental Matricies
 - estimate F from 7 points
 - test agreement with all other points
- Direct motion
 - estimate affine (or rigid motion) from small match
 - see what other parts of image are consistent
- ...

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Fitting and Probabilistic Segmentation

- · Robust estimation
- EM
- Model Selection
- RANSAC

[Slides from Micheal Black and F&P]