The Power of the Dark Side:
Using Cast Shadows for Visually-Guided Touching

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A humanoid robot needs to be able to operate safely in human workspaces, preferably without extensive calibration. We consider the problem of directing a robot arm towards, across, and away from an unmodeled surface without damaging it. For this task we make use of a powerful resource: the shadow cast by the robot’s own body. We show that the cast shadow of the arm on the surface can be detected by a camera and used to derive a time-to-contact estimate. This estimate, when combined with the 2D tracked location of the arm’s endpoint in the camera image, is sufficient to allow 3D control relative to the surface. We show that the same method can detect either cast shadows or reflections, allowing the robot to operate correctly over water, mirrors, or other reflective materials. Such scenarios, along with low-texture surfaces, are cases in which stereo vision – the more commonly used depth cue in robotics – might fail and is worth augmenting. We draw on the literature of computer graphics and virtual reality to argue that for manipulation, sensitivity to shadows and interreflection will be of similar importance to stereo vision as a depth cue when attempting to touch an object. In computer vision, shadows are generally treated as a nuisance, but that doesn’t mean roboticists should do the same.

Keywords: humanoid robotics; shadows; time to contact; depth perception; manipulation

1. Introduction

Shadows have long been a bane of computer vision, creating illusory objects and obscuring true object boundaries. Much energy has been devoted to developing the means to detect shadows automatically, not because they are considered valuable in themselves, but because they need to be distinguished from true objects\(^1\). On the other hand, researchers in computer graphics and virtual reality have struggled to render shadows in order to increase realism and aid depth perception\(^2\). Robotics draws on all these fields, so should we be fans or foes of shadows?

In this paper we observe that in visually-guided reaching, perception of the shadow(s) cast by a robot arm is potentially very useful. As the arm approaches a surface, the shadow that it casts rushes to meet it. This gives an indication of
the arm’s proximity to the surface. If we track this approach, we can estimate a “time-to-contact” for touching. This is analogous to the time-to-contact quantity derived from optic flow for navigation\cite{3,4}. We demonstrate directing an arm to touch a target using information from a single camera. This is done by driving the arm to simultaneously reduce the visual error between the endpoint and the target and the visual error between the endpoint’s shadow and the target. When both these errors are zero, the endpoint is at the target in 3D space. We use a tactile sensor in the arm’s endpoint to verify contact.

Section 2 introduces Coco, the gorilla-like robot upon which this work is implemented (see Figure 1). Section 3 reviews in brief the literature on shadows and their role in human depth perception, making the case that they are important to the perception of contact and are an very strong cue, particularly when combined with motion. Section 4 discusses the particular method proposed for detecting cast shadows of the arm, using the fact that the robot is in control of the arm and can move it to its advantage. Section 5 uses the detected shadow as the basis for a controller, which drives the arm from point to point on a surface, rising away from and falling towards the surface at the beginning and end of the trajectory. Section 6 looks more closely at estimating the time-to-contact from shadow information. We close with discussion and proposals for future work.

2. The robot

The platform used is the robot Coco designed by Morse\cite{5} (see Figure 1). Coco is a gorilla-like robot, with two legs and two arms. Each leg has two degrees of freedom (DOF), one in the knee and one in the hip. Each arm has three DOF, one in the elbow and two in the shoulder. The neck has two DOF. This robot has a mass of 10 kg. Each arm is 312 mm long, the legs are 110 mm long and the body is $310 \times 345 \times 100$ mm. The arm can be used to walk and to interact with the environment. The motor control is performed by five Agile MAX2000 motor control boards. Each board drives 3 motors and is controlled across an RS232 serial port.
In the tip of the arm there is a force sensor with a resolution of 120 mV/kg and a limit of 0.5 kg.

The vision system consists of a Sony camcorder with a resolution of $720 \times 480$ pixels and controllable zoom and focus. The control is done by a custom board that interfaces the LANC port of the camera to a RS232 port. The camera connects to an offboard computer running Linux through its IEEE 1394 (Firewire) interface. This computer runs the vision system described in the remainder of this paper, and communicates via TCP/IP with a second computer charged with motor control and interfacing with the motor control boards.

3. The role of shadows in human perception of depth

Many cues play a role in the human perception of depth, including occlusions, stereopsis, motion parallax, shadows (attached or cast), interreflections, perspective effects, etc. Over the centuries these cues have become better understood in art; the idea of perspective, for example, first gained currency in the 15th century. In this century, the need to understand depth perception has grown in urgency as researchers in computer graphics and virtual reality strive for increasing realism. Stereopsis has proven to be an important cue; shadows and interreflections have also proven effective, and in some cases match stereopsis in power\(^6\,7,8,2\). Moving shadows can profoundly influence the interpretation of a scene, in some cases overruling other depth cues such as apparent size\(^9\,10\). Apparent shadow motion can give a very strong sense of object motion even in the absence of any other cue\(^11\). Shadows help in the perception of spatial relationships in computer-generated images\(^12\). Shadows and interreflections are particularly important for giving a strong impression of object contact in computer graphics\(^13\).

There is speculation that the cast shadow of the hand may be integrated into the body schema, in a manner somewhat analogous to the extension of the schema to include tools\(^14\). There is some evidence that the processing of shadows in the brain, which can impact on object recognition performance, is at least partially done without conscious awareness\(^15\).

In computer vision, shadows cannot be ignored. Much work has been devoted to detecting them, even if only for the purposes of discounting them\(^16\) (for a review, see Prati et al\(^1\)). Less common is work to utilize shadows. In computer graphics, it was realized that the cast shadow of a known object (a long stick) could be used to recover the shape of an object the shadow passed over, in a manner analogous to (but cheaper than) active illumination methods that scan lines of light across the scene\(^17\). Shadow has also been used to recover body pose in video of moving people\(^18\). There is a great deal of work on ‘shape from shadow’ which is generally concerned with shading rather than cast shadows.

To summarize, shadows have a demonstrable and significant impact on the ability of humans to perceive depth and adjacency, and to judge whether an object and a surface are in contact. We wish to import that advantage into robotics,
rather than continue to rely only on stereo vision for depth perception. Shadows and stereopsis have somewhat complementary properties; stereo is at its best when depth changes are sharp, while shadows are easiest to track when depth changes are relatively smooth. The error in stereo measurements grows with distance from the camera, while the error in shadow measurements grows with distance from the surface. Shadows (and reflections) are detectable even in the absence of texture, or with reflective surfaces, situations that can confuse stereo. We believe that combining stereopsis and shadows could lead to a more robust system for manipulation. In this paper we seek to show the benefits of shadows on their own, but that should not be read as a belief that shadows are better than stereo.

4. Detecting cast shadows of the arm

What properties of a cast shadow can be used to reveal its presence? The most obvious property of a cast shadow is that the surface it is cast on becomes darker than it otherwise would be. In a single image, this is not very helpful, since we do not know how dark different surfaces should be, and the appearance of surfaces varies for many reasons other than shadows. In a video stream, this property is more helpful, since we can watch for moving patches of darkness, or compare against an image of the background without the arm or its shadow present.

For this work, two methods are used for detecting regions of illumination change, labeled static and dynamic. The static method is based on building a background model of the workspace while holding the arm to the side, then looking for novel regions of illumination change relative to that model when the arm swings into
action. This method can detect very weak shadows, and operates just as well when the arm is stationary as when it is moving. The dynamic method specifically looks for moving regions of illumination change, by comparing the current image from the camera with one from half a second ago. This gives better localization of the shadow of the endpoint (the fastest moving part of the arm) while the robot is in motion, but is useless when the robot is stationary.

The first step in finding the cast shadow is to find the endpoint of the arm itself, as a reference. The endpoint of the arm is tracked at 30Hz. In each frame, a small window (1/25 of the image area) around the last known position of the endpoint is scanned for the dominant local orientation within ±5° of the arm’s last known orientation. It is assumed this dominant orientation will be due to the edges of the arm and the highlights running along its length. The tracked position of the arm is then updated to the center of mass of the pixels that are at the dominant orientation, with a small constant offset in the direction of the orientation. When iterated, this procedure drives the tracked position out along the arm to the endpoint, and pulls it back in if it begins to drift. The tracking procedure makes minimal assumptions about the endpoint. The tracker is initialized using an appearance model of the arm and an assumption that the arm is initially in an area with good contrast with the background.

Once the position of the endpoint is known, the vision system waits for an opportunity to build a background model. This is provided by simply swinging the endpoint to the side, out of the way. The background model is simply a snapshot
of the scene. When the arm swings back into action, static and dynamic shadow cues are combined by simple summation of grayscale pixel differences with the reference images. To speed shadow detection, we make some simplifying assumptions: we assume there will be a shadow below the arm in visual coordinates, and some component (even if very faint, and not the main shadow) will be vertically underneath the arm. Figure 2 shows a range of scenarios that meet this assumption. Given that assumption, we simply scan down from the endpoint, looking for a peak of illumination change. The shadow (or reflection – see Figure 3) we find will in general not be of the forearm. We could trace from this starting point to find the shadow, but choose not to do so, since the distance to this point from the endpoint is as good as any as a measure of shadow distance.

5. Reaching across a surface

Shadow detection allows us to design a controller for reaching across from one point to another on a surface. A control loop designed to maintain the distance of the cast shadow from the arm served to keep the arm at a constant ‘cruising’ height. At the beginning of the trajectory the arm rises away from the surface, as judged using shadows, to avoid scraping across the surface. At the end of the trajectory the arm sinks towards the surface (see Figure 4).

Which motor combinations move towards the surface? This just needs to be known qualitatively, and doesn’t need to be exact – errors can be absorbed into the closed loop visual errors. A very crude kinematic model for the workspace can be constructed by making small exploratory movements and measuring the amount of change caused in 2D endpoint location and shadow distance by displacements in each of the degrees of freedom. Coco’s arm has three degrees of freedom – a hinge joint at the elbow ($\theta_1$) and a differential pair at the shoulder ($\theta_2$ and $\theta_3$). To control the arm, virtual axes are used that correspond very roughly with extension away from the body ($m_1$) rising towards the head ($m_2$) and drawing inwards towards the
chest \((m_3)\), which are related to the physical axes as follows:

\[
\begin{align*}
\theta_1 &= m_1 \\
\theta_2 &= m_1 + m_2 + m_3 \\
\theta_3 &= m_1 - m_2 + m_3
\end{align*}
\]

Drawing inwards towards the chest \((m_3)\) is achieved by driving the differential shoulder motors \(\theta_2\) and \(\theta_3\) in lock-step. Rising towards the head \((m_2)\) is similar, but now the differential motors are driven in opposition. Extension of the arm \((m_1)\) is achieved by moving the elbow joint, then compensating at the shoulder by the same angle to keep the endpoint moving out along a ray from the shoulder.

We wish to be able to move the endpoint of the arm, detected in visual coordinates, towards a target also defined in visual coordinates, while controlling the height of the arm above a surface (estimated from the behavior of the arm’s shadow). When the robot’s gaze is directed downwards at a workspace, the virtual axes correspond very approximately to variables we would like to control. Changing \(m_2\) (rotation towards the head) is approximately what we need to control depth, whereas \(m_1\) and \(m_3\) will have a big impact on moving the position of the arm across the image while having a lesser impact on its depth.

Since we can also recover the projected angle of the arm in the image, which for the geometry of this robot is an approximate indicator of rotation towards the chest \((m_3)\), desired visual displacements can be expressed in terms of desired visual rotation and extension of the arm. These quantities can be controlled coarsely using \(m_2\) and \(m_3\). We label the three visual control quantities as \(v_1\) (desired visual extension of the arm), \(v_2\) (desired visual distance to shadow), and \(v_3\) (desired visual rotation of the arm). To discover the relationship between the observed variables and the control variables, the robot makes exploratory movements that start small, then grow until it sees significant changes in at least one of the observed variables.

The result of this exploration will be somewhat dependent on the geometry of the surface and the location of the arm – here is the result of a typical run:

\[
\begin{bmatrix}
\Delta v_1 \\
\Delta v_2 \\
\Delta v_3
\end{bmatrix} = \begin{bmatrix}
8.1 & 6.3 & -4.4 \\
8.4 & 10.8 & -7.1 \\
3.9 & 1.9 & 11.3
\end{bmatrix} \begin{bmatrix}
\Delta m_1 \\
\Delta m_2 \\
\Delta m_3
\end{bmatrix}
\]

Note that \(\Delta m_1\) has its strongest influence on \(\Delta v_1\), \(\Delta m_2\) has its strongest influence on \(\Delta v_2\), and \(\Delta m_3\) has its strongest influence on \(\Delta v_3\), which corresponds to the general intuition. We can invert this relationship to produce a reasonable controller:

\[
\begin{bmatrix}
\Delta m_1 \\
\Delta m_2 \\
\Delta m_3
\end{bmatrix} = \begin{bmatrix}
0.31 & -0.18 & 0.01 \\
-0.28 & 0.25 & 0.05 \\
-0.06 & 0.02 & 0.08
\end{bmatrix} \begin{bmatrix}
\Delta v_1 \\
\Delta v_2 \\
\Delta v_3
\end{bmatrix}
\]
In this section we evaluate and quantify the accuracy of shadow detection for predicting the time to contact as the robot arm approaches a surface. The principle used to estimate the time to contact is depicted in figure 5. We can estimate the time to contact using the following equation.

\[ tc = \frac{Y_{\text{contact}} - Y_{\text{threshold}}}{\text{slope}} \]  

where \( tc \) is time to contact, \( \text{slope} \) is the rate of change of the shadow distance, \( Y_{\text{contact}} \) is the distance at which the arm makes contact with the surface, \( Y_{\text{threshold}} \)
is any distance from which we can predict the time to contact.

This equations holds if the rate of change of the distance between the arm and shadow is roughly constant. We expect this to be true if the illumination is constant and the arm moves at constant velocity. To test these assumptions we ran the following experiment. We direct the robot to drive its arm approximately downwards using the \( m_2 \) virtual axis described in section 5. The robot detects that it touches the surface using the touch sensor in the endpoint of its arm.

Figure 6 shows the outcome of one such trajectory. We can observe that as the robot moves its arm towards the surface the distance between the shadow and the arm is reduced.

One complication shown in the figure is that when the shadow is too close to the arm (around 70 pixels), the shadow merges with the arm and cannot be reliably localized. At this point cues such as shadow darkness and crispness should be used, but are not yet available. However, time to collision still can be computed with good precision. Under the same light conditions we ran the experiment starting at different positions. The results are shown to the right in Figure 6. In this figure we observe that the difference between \( Y_{\text{contact}} \) from the first experiment (54.1) and the current one (53.3) is very small. This supports the assumption that we can reliably and accurately compute time to contact for a given value of slope.

Next, we performed experiments with different surfaces and/or illumination conditions. The results are shown in Figures 7 and 8.

More experiments were done in a given scenario to address the consistency of the \( Y_{\text{contact}} \) threshold and its effect in the time to contact estimation.

We performed 10 runs with fixed illumination and surface while varying the initial arm position. For each run we fitted a line using the distance points whose value were above 70 pixels. This value (70 pixels) is the threshold above which the
Fig. 8. The surface used in this experiment has a different texture than in Figures 6 and 7.

detection of the shadow is reliable. We can observe this threshold in figure 5 labeled as $Y_{\text{threshold}}$. From the line fitted to the data we obtained its slope. Consequently, the only remaining parameter required to determine the time to contact according to equation 1 is $Y_{\text{contact}}$.

$Y_{\text{contact}}$ is obtained in each one of the experiments when the touch sensor detects a contact. These results are presented in table 1. Due to the variability of the behavior of the touch sensor, we can observe that $Y_{\text{contact}}$ is quite noisy. Therefore, we computed its average to use in equation 1.

The time to contact obtained for each of the experiments has a very small standard deviation, which shows that the method is applicable in practice, and
suggest that the time estimation is more accurate than the touch sensor readings can confirm. The computation can be done very quickly since the slope obtained from a set of data can also be obtained on-line with a few points.

7. Conclusions and future directions

This work is part of a larger project to build a robot capable of manipulating unfamiliar objects in an unstructured environment. This is a very challenging task since perceptual uncertainty translates directly into clumsy motion. For example, if the robot estimates the location and orientation of a surface incorrectly, then there is a limit to what can be salvaged by clever control algorithms.

Our goal is to give our robot the perceptual abilities it needs to actively resolve ambiguity in its environment, when the passive vision algorithms it uses fail. Previous work in our group showed how manipulation could be used to detect object boundaries experimentally. In that work, shadows were dealt with as a nuisance. Now we want to make them a positive benefit. In this paper, we showed that shadows cast by the arm make a fine depth cue. The shadow detection mechanism could and should be extended to further evaluate the shadow, and not just report its gross position. Over important parameters include size, darkness, and the crispness of its outline. For example, as the arm approaches the surface, darkness and crispness increase dramatically. This should permit an independent measure of time to collision which can take over when gross position begins to give little information.

We are also making an effort to exploit object shadows (see Figure 9). Since our camera has controllable zoom and focus, we can look very closely at the boundary of objects, and confirm the existence of shadows that indicate a point at which we
might be able to lift the object.

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References

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